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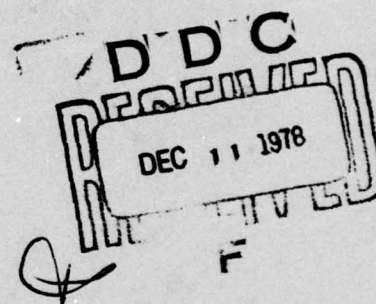
LEVEL II



**PHOTOMETRIC METHODS FOR THE ANALYSIS  
OF HUMAN KINEMATIC RESPONSES TO  
IMPACT ENVIRONMENTS**

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OCTOBER 1978

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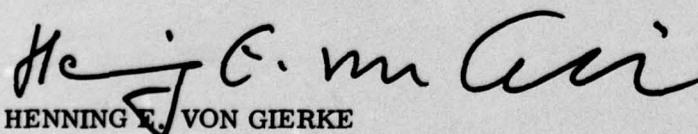
The experiments reported herein were conducted according to the "Guide for the Care and Use of Laboratory Animals," Institute of Laboratory Animal Resources, National Research Council.

The voluntary informed consent of the subjects used in this research was obtained as required by Air Force Regulation 80-33.

This report has been reviewed by the Information Office (OI) and is releasable to the National Technical Information Service (NTIS). At NTIS, it will be available to the general public, including foreign nations.

This technical report has been reviewed and is approved for publication.

FOR THE COMMANDER



HENNING E. VON GIERKE

Director

Biodynamics and Bioengineering Division  
Aerospace Medical Research Laboratory

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20. ABSTRACT (Continue on reverse side if necessary and identify by block number) This report presents the processes, procedures, and techniques developed to evaluate the biodynamic response of body segments to laboratory simulations of aircraft crash and escape system environments. These simulations were conducted on the test facilities, principally the Vertical Drop Tower, the Horizontal Impulse Accelerator, and the Square Wave Impact System, located at the Aerospace Medical Research Laboratory, Impact Branch (presently known as Biomechanical Protection Branch), Wright-Patterson Air Force			

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Base, Ohio, by personnel of that Branch.

The processes described were developed to determine the time histories of coordinate locations of anthropometric points during the impact and immediately post impact phases during which the anthropometric points demonstrated planar or nonplanar motion.

Coordinate systems were defined for each of the various test facilities. Reference points were marked with fiducials and their coordinates were surveyed. Body segments of the subjects were defined by fiducials affixed to anthropometric points which were measured prior to each test. The tracks of these points were recorded on high speed (500 fps) 16mm motion picture cameras throughout each test event. The film frame coordinates of the points were digitized and electronically processed to define the time-seat coordinate position history of the motion for linear and angular displacement, velocity, and acceleration analysis.



## PREFACE

The data reduction processes described herein were developed and implemented for the benefit of the Aerospace Medical Research Laboratory, Wright-Patterson Air Force Base, Ohio, under Contract F33615-73-C-4157, which was partially funded by the Department of Transportation, National Highway Traffic Safety Administration, under Interagency Agreement DOT-HS-017-1-017-IA. This contract was monitored initially by Capt John T. Shaffer and later by Maj John P. Kilian of the Impact Branch (presently known as Biomechanical Protection Branch), Aerospace Medical Research Laboratory.

University of Dayton personnel who made major contributions to the program include W. J. Hovey, Project Supervisor, H. T. Mohlman and R. C. Reboulet, Research Mathematicians, and P. A. Graf, Research Technician.

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## SECTION I

### INTRODUCTION

Accelerations of less than one second duration occur in a variety of aerospace environments including escape system and aircraft and surface vehicle crash environments. The 6570th Aerospace Medical Research Laboratory (AMRL), Bionics and Biodynamics Division, Impact Branch (BBI) has been engaged in the conduct of experimental tests to assess the effectiveness of a variety of restraint systems and protective devices by evaluating biomechanical responses of manikins, primates, and humans to exposure to laboratory simulations of these environments. The biomechanical responses to such exposure were evaluated from strategically located and oriented monitoring devices, such as accelerometers and load cells whose outputs were recorded on magnetic tape, and high-speed motion picture cameras mounted offboard and onboard the test vehicles.

The reduction of electronically recorded data was accomplished in routine fashion using accepted methods to derive the Gadd Severity Index (SI) and/or Head Injury Criterion (HIC) from triaxial acceleration time-histories. While these are recognized indicators of the probability of injury resulting from exposure to an impact environment, they do not describe the motion of body segments other than at the point, or points monitored. To adequately describe the responsive motion of the many body segments, quantitative analysis of time displacement data of the anthropometric points defining the various body segments was required. The photometric system designed and implemented to satisfy this requirement was an integrated data acquisition, data reduction system.

Data were recorded on at least three 16mm cameras mounted offboard, or in a combination of offboard and onboard, depending on the environment being simulated. If vehicle accelerations were not to exceed a peak acceleration of 20g, two



cameras were mounted onboard the vehicle with two others mounted offboard. If peak vehicle accelerations in excess of 20g were anticipated, all cameras were mounted offboard.

When the photo instrumentation plan specified that all cameras be offboard, one or two primary data cameras (depending on the vehicle displacement during the event), were mounted normal to the plane of principal predicted motion. Two other cameras were mounted such that their optical axes were mutually perpendicular to the optical axis of the primary data camera.

When the photo instrumentation plan required the onboard/offboard combination, the two onboard cameras were located and oriented with respect to a vehicle coordinate system. The locations and orientations of these cameras varied from one test program to another depending on the size of the test subjects, type of predicted motion, etc., with principal consideration being given to the fact that all tracked points had to be observed by both cameras throughout the entire event. Of the offboard cameras one was located with its optical axis normal to the plane of principal motion and the other was located such that its optical axis was aligned parallel, or as nearly parallel as practical, to the axis of vehicle motion.

Prior to each test, fiducials, one-inch diameter circles with alternating black and yellow quadrants, were applied in accordance with the recommended practice, SAE J138 (see Figures B1 and B3). After the subject was adjusted to the initial position, the locations of the applied fiducials were measured and recorded. Reference fiducials, installed on the test fixture and surveyed at initiation of a test series, were checked prior to each test to determine if any required replacement.

The data reduction phase of the system involved digitizing the film plane coordinates of the reference fiducials and tracking fiducials, time synchronizing of film frames, calculation of conversion factors, and electronic data processing.

The projected film frame coordinates were digitized, frame by frame, using a Producers' Service Corporation model PVR film analyzer interfaced to a type 35 teletype terminal (TTY). The TTY generated a listing and punched paper tape of formatted digital values.

The digitized data were transmitted from the TTY tape reader to the computer via voice quality telephone line. The data file was edited to correct format or characters as required then saved on disk file and copied to punched cards which served as the permanent file.

The system contained three processing programs. HIFPD was used to process planar motion of points as observed by a camera mounted normal to the plane of motion. This program was initially written to yield time histories of coordinate points relative to the test vehicle and of the test vehicle relative to the range. It was shortly thereafter modified to derive relative linear and angular velocities and accelerations of the points and to prepare plots of these data.

Program SLED was designed to take data digitized from two camera views, synchronize the data timewise, and solve for the most likely points of intercept of up to four pairs of rays in a three-dimensional rectilinear coordinate system. The successful operation of this program required precise determination of the coordinates of the focal point of each camera and the azimuth, elevation, and roll angles of each of the cameras. Physical measurements of these parameters proved inadequate, thus the third program in the system, POOCH, was developed.

Program POOCH is used to derive the location and orientation of a camera and a factor including the focal length of the camera lens and the magnification of the projector. It optimizes these parameters based upon the surveyed coordinates of up to 20 reference points.

The cameras were operated at a nominal film speed of 500 frames per second, with exposure time of 0.4 msec to 0.8 msec depending upon predicted maximum velocities of tracked points and illumination intensity. Film timing and camera synchronization were provided for by the use of pulsed LED's, driven by a common pulse generator at a rate of 100 pulses per second, recorded on one side of the film just beyond the edge of the image frame. Due to the location of the LED in the film path, any given pulse was recorded 11 to 13 frames behind the coincident image frame, depending on the size of the film slack loop between the supply reel and the film gate. To minimize the error due to this variance, a synchronizing pulse, recorded on the electronic data recording system, was used to fire a strobe light, the flash of which was observed by all cameras.



## SECTION 2

### ANALYSIS OF DATA FROM ONE CAMERA

Horizontal Impact Facility Photometric Data Analysis Program (HIFPD) is a digital computer program developed to analyze the Hyge Impact Facility Photometric data for Impact Branch of the Biodynamics and Bionics Division of the 6570th AMRL. The program was compiled and executed on the CDC computers at Wright-Patterson Air Force Base. The standard CALCOMP plot package is used to plot data and thus must be attached to load and execute the program.

This program inputs the code sheet data and program control parameters described in Appendix A and a maximum of 300 (MAXN) frames of X, Z position data for the range, sled, hip, knee, shoulder, elbow, head point 1 and head point 2 for ITYPE = 0 or range, sled, head point 1 and head point 2 for ITYPE = 1. The data card format are also described in Appendix A.

The program computes the following four types of data as requested by the program control parameters:

(a) The input data versus frame number and the frame to frame differences are printed in counts. The range difference is subtracted from the frame to frame differences for each of the seven parameters. The only value of this difference data would be to spot errors in the data.

(b) The displacements (X and Z) of the hip, knee, shoulder, elbow, head point 1 and head point 2 relative to the sled are computed, and a moving eleven point (NP = 11) quadratic least square fit is used to smooth the data. These data are also plotted, if requested on the test setup card.

(c) The angles in radians between the shoulder and hip and between the head point 1 and head point 2 are computed using the above smoothed data. The angular velocity is computed in

radians per second using a moving 11 point quadratic fit of the angle versus time data (computes derivative of least squares equation). The angular acceleration is computed using a moving eleven point quadratic fit of the velocity versus time data. These data are also plotted as requested on the test setup card.

(d) The linear velocity and acceleration data for any combination of the eight variables are computed as requested on the test setup card. For example, the linear velocity and acceleration of the head pt 1 relative to the range, sled relative to the range or the head pt 1 relative to the sled can all be computed. Note that range relative to some other parameter cannot be computed. To compute these linear velocity and acceleration data, the X and Z displacements are computed for the variable of interest relative to the reference variable. A moving eleven point (NP = 11) quadratic least square smoothing function is applied to both the X and Z time histories. The resultant displacement in feet is computed from this smoothed data. A moving eleven point quadratic fit is applied to this resultant data to obtain the velocity in feet per second and a second eleven point quadratic fit is applied to the velocity data to obtain the acceleration data in feet per second squared and in G's. These data are printed and plotted as requested on the test setup card.

The three external files used by this program are the input file (unit 5) used to read all code sheet and data cards, the output file (unit 6) used to print all output, and TAPE7 (unit 7) used to generate the plotter tape. A magnetic tape must be requested with TAPE7 as the local file name.

The following sections of this report present a general description of the main program and all subroutines except the CALCOMP plot routines. Flow charts are also included for each routine. Appendix C contains a complete listing of the program source deck and Appendix D contains a sample run complete with all input and output data (including CALCOMP plots).

## 2.1 PROGRAM HIFPD

This main routine controls all input, output, and computations requested by the test setup card parameters. All subroutines required to smooth the data, compute derivatives, and plot results are called by this routine. All program diagnostics resulting from errors in setup or data card formats are printed by this routine.

### Method

The program reads the code sheet control cards described in Appendix A and initializes the program print and plot control parameters. The program reads the card code, frame number, and X and Z axis data for four (ITYPE = 1) or eight (ITYPE = 0) variables (index J) for each frame (index I) in the test. Frame number and card code are checked for input errors; errors in input cause diagnostics to be printed and the test to be terminated. If more than MAXN frames are read, diagnostics are printed and all frames beyond MAXN are omitted from the analysis. The T(I) time data are computed from the frame number as follows:

$$T(I) = IFR(I)/DT$$

where IFR(I) is the frame number and DT is the number of frames per second. If setup card parameter IRX is greater than zero, the sign of all X axis data are changed. After all data are read, a summary page is printed listing all types of analyses to be computed, printed, and plotted for this test.

When program control parameter IPR  $\geq 0$ , all raw input X and Z axis data are printed in counts. The frame to frame difference data are computed and printed for all J variables from frames 1 equal 2 to N as follows:

$$XD(1) = X(I,1) - X(I-1, 1)$$

$$XD(J) = X(I,J) - X(I-1,J) - XD(1).$$



XD(1) is the range difference from the 1<sup>th</sup> frame and XD(J) is the variable minus range difference for the J<sup>th</sup> variable and the 1<sup>th</sup> frame. The above are also computed and printed for the Z axis data.

All X and Z axis data are adjusted for shifts in the range reference reading and then converted from counts to feet:

$$H1 = X(I,1) - X(1,1)$$

$$H2 = Z(I,1) - Z(1,1)$$

$$X(I,J) = (X(I,J) - H1) * CAL(J)$$

$$Z(I,J) = (Z(I,J) - H2) * CAL(J)$$

where CAL(J) is the calibration factor for the J<sup>th</sup> variable (J = 2 to 8).

When program control parameters IPC < 2 or IPA < 2, X and Z axis motion relative to the sled are computed for variables 3 to 8 ( or 7 and 8 for ITYPE = 1):

$$XD(I) = X(I,J) - X(I,2)$$

$$ZD(I) = Z(I,J) - Z(I,2).$$

Subroutine SM is called to compute a moving eleven point (NP = 11) quadratic least square fit to smooth the X and Z axis data. The smoothed data are stored in arrays XX(I,JJ) and ZZ(I,JJ) where JJ = J-2. As a result of the eleven point smoothing, five frames are lost at the beginning and end of the test data; this is true each time the data are smoothed by subroutine SM or derivatives are computed by subroutine DERIV1. If parameter IPC < 2, these smoothed data relative to the sled are printed; if IPC < 1, subroutine CPLT is called to generate a CALCOMP plot of X versus Z for all variables (J = 3 to 8).

The angle between the shoulder and the hip is computed for each frame using the above smooth data when program control parameter  $IPA < 2$ . The angle in radians is computed as follows:

$$HI = ZZ(I,3) - ZZ(I,1)$$

$$H2 = XX(I,3) - XX(I,1)$$

$$XD(I) = \arctan (H1/H2)$$

where index 3 is shoulder data and index 1 is hip data in the XX and ZZ arrays. Angles  $XD(I)$  are adjusted by factors of  $2\pi$  to make them continuous. Subroutine DERIV1 is called to compute the angular velocity in radians per second from a moving eleven point ( $NP = 11$ ) quadratic fit of the  $XD(I)$  data and angular acceleration in radians per second squared from an eleven point quadratic fit of the velocity data. The angular data are printed and, for  $IPA = 0$ , subroutine CPLT is called to generate CALCOMP plots of the angular velocity and acceleration versus time ( $IP = 2$ ). All above angular data are computed in a similar manner for head point 1 minus head point 2 data (indices 5 and 6 in arrays XX and ZZ).

Parameter M contains the number of sets of linear velocity and acceleration data to be computed for one variable (array ID) relative to another (array IR). For example, if  $ID(1) = 3$ , and  $IR(1) = 2$ , then for set  $M = 1$  the hip motion relative to the sled is computed for all available frames.

If  $M < 0$  and  $IPL < 2$ , all data for variables  $J = 2$  to 8 are adjusted by subtracting the initial value as follows:

$$X(I,J) = X(I,J) - X(1,J)$$

$$Z(I,J) = Z(I,J) - Z(1,J)$$

where all X and Z data have previously been converted from counts to feet. For each of the M sets the following are computed:

JD = ID(K)

JR = IR(K)

DI(I) = X(I,JD) - X(I,JR)

DC(I) = Z(I,JD) - Z(I,JR)

where K is the set index (K = 1 to M). When JR is 1 above, X(I,JR) and Z(I,JR) data are deleted, because motion relative to the range has already been removed from the data (see calibration equations). Subroutine SM is called to apply the eleven point quadratic smoothing function to the DI(I) and DC(I) displacement data; the smoothed data are stored in arrays XD(I) and ZD(I). The resultant displacement RES(I) is computed as follows:

$$RES(I) = \sqrt{XD(I)^2 + ZD(I)^2}.$$

The maximum XD(I), ZD(I) and resultant and the minimum XD(I) and ZD(I) are also determined from the above data. Subroutine DERIV1 is called to compute the velocity, VEL(I), from the resultant data and the acceleration, ACC(I), from the resultant data using eleven point quadratic smoothing functions in each case. The acceleration data are converted from feet per second squared to G's:

$$ACCG(I) = ACC(I)/32.2.$$

All the above displacement, velocity and acceleration data are printed versus time. Also, if IPL = 0, subroutine CPLT is called (IP - 3) to plot the velocity in feet per second and the acceleration in G's versus time in seconds.

After all tests are analyzed, the CALCOMP plot subroutine PLOTE is called to terminate the CALCOMP plot routines.



A flow chart for this routine is shown in Figure 1 and a sample test complete with all input and output is listed in Appendix D.

<u>Error Diagnostics:</u>	YES
<u>Subroutines Required:</u>	CPLT, DERIV1, SM, PLOTS, and PLOTE (PLOTS and PLOTE are part of the CALCOMP plot package.)
<u>COMMON Required:</u>	The COMMON variables actually used to transfer data are described in subroutine CPLT. Many of the blank COMMON variables in this routine are in COMMON only to reduce required compilation storage.
<u>Program Length:</u>	5342 <sub>8</sub>
<u>Labeled Common Length:</u>	23 <sub>8</sub>
<u>Blank Common Length:</u>	12616 <sub>8</sub>
<u>CM Required to Load Program:</u>	Approximately 50000 <sub>8</sub>

#### 2.1.1 Subroutine CPLT (T,Y, Z, IP)

Subroutine CPLT generates a CALCOMP plot of: (a) X versus Z displacement with respect to the sled for all available parameters, (b) time versus angular velocity and acceleration, or (c) time versus linear velocity and acceleration depending on the value of parameter IP. The standard CALCOMP plot package is required to load and execute the program.

##### Method

For parameter IP = 1, CPLT generates one composite plot of X versus Z displacement for variable motion with respect to the sled. All X and Z scaling are set by CPLT independent of the data and are defined as follows.

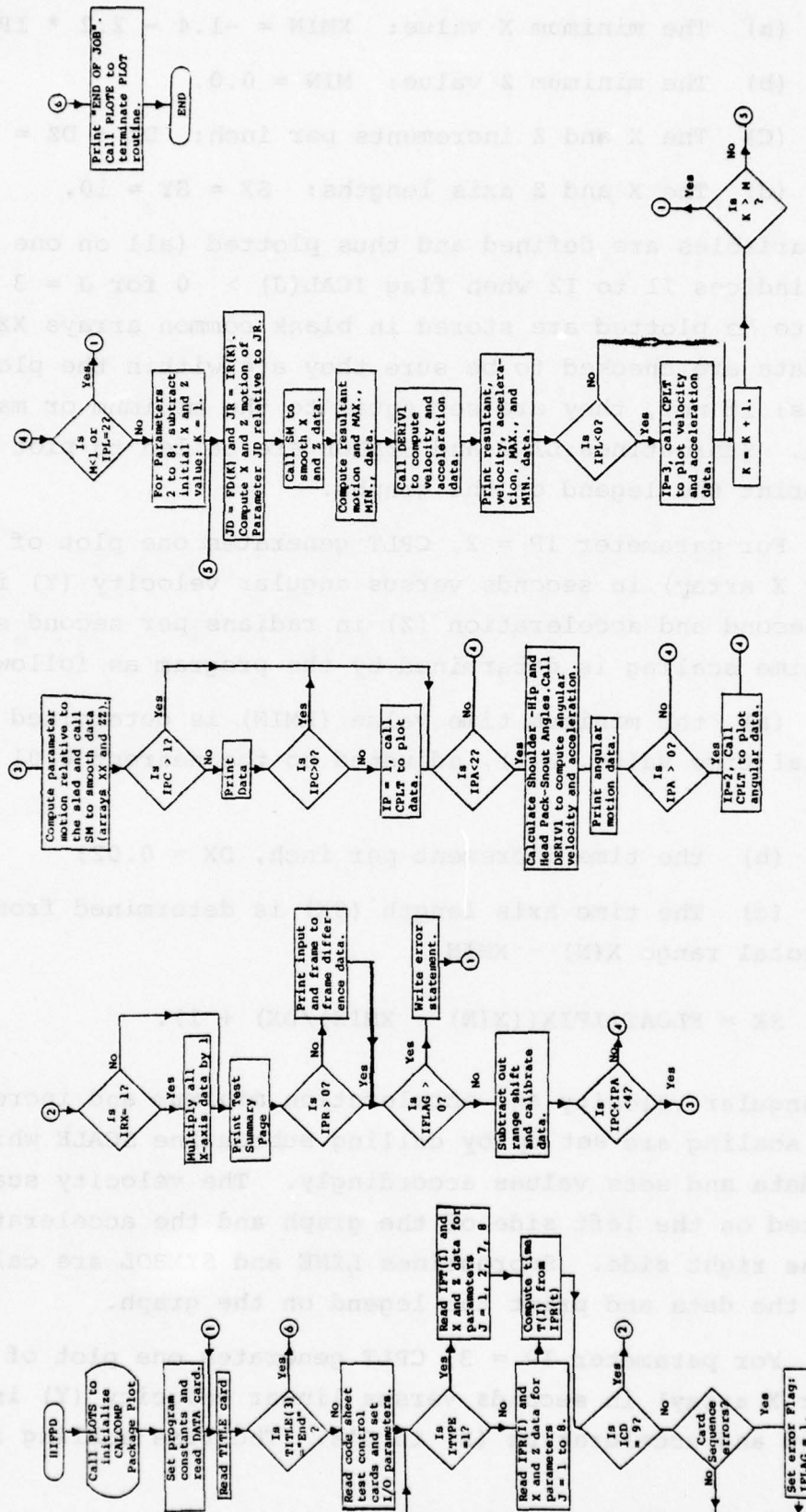


Figure 1. HIFPD Flow Chart.

- (a) The minimum X value:  $XMIN = -1.4 - 2.2 * IRX$ .
- (b) The minimum Z value:  $MIN = 0.0$ .
- (c) The X and Z increments per inch:  $DX = DZ = 0.4$ .
- (d) The X and Z axis lengths:  $SX = SY = 10$ .

The variables are defined and thus plotted (all on one graph) from indices I1 to I2 when flag ICAL(J) > 0 for J = 3 to 8. Data to be plotted are stored in blank common arrays XX and ZZ. All data are checked to be sure they are within the plot scale values; if not, they are set equal to the minimum or maximum value. Subroutines LINE and SYMBOL are called to plot the data and print the legend on the graphs.

For parameter IP = 2, CPLT generates one plot of time (T or X array) in seconds versus angular velocity (Y) in radians per second and acceleration (Z) in radians per second squared. The time scaling is determined by the program as follows:

- (a) the minimum time value (XMIN) is determined from the initial time value, X(1), adjusted to the nearest 0.01 less than X(1);

- (b) the time increment per inch,  $DX = 0.02$ ;

- (c) The time axis length (SX) is determined from DX and the total range  $X(N) - XMIN$

$$SX = \text{FLOAT}(\text{IFIX}((X(N) - XMIN)/DX) + 1).$$

The angular velocity and acceleration minimum and increment per inch scaling are set up by calling subroutine SCALE which checks the data and sets values accordingly. The velocity scale is printed on the left side of the graph and the acceleration scale on the right side. Subroutines LINE and SYMBOL are called to plot the data and print the legend on the graph.

For parameter IP = 3, CPLT generates one plot of time (T or X array) in seconds versus linear velocity (Y) in feet per second and acceleration (Z) in G's. The time scaling is



computed as per  $IP = 2$  above. The velocity and acceleration are plotted using the same ordinate scale. The ordinate length  $SX$  is always 10 inches. The minimum value,  $YMIN$ , and the increment per inch,  $DY$ , are determined from the data.  $DY$  will always be 10, 20, or 30 depending on the total range required. If the total range is greater than 300, some of the data will be lost. All data are checked to be sure they are within the scale values; if not, they are set equal to the maximum or minimum value. Subroutine  $LINE$  is called to plot the data and subroutines  $SYMBOL$  and  $NUMBER$  are called to print the legend on the graph.

A flow chart for this routine is shown in Figure 2 and sample graphs are shown in Appendix D.

Error Diagnostics: NONE

Subroutines Required:  $AXIS$ ,  $LINE$ ,  $NUMBER$ ,  $PLOT$ ,  $SCALE$ , and  $SYMBOL$  (all are in the standard  $CALCOMP$  plot package).

Argument List:

- $T$  - array of time data points in velocity and acceleration plots.
- $Y$  - array of velocity data points.
- $Z$  - array of acceleration data points.
- $IP$  - flag which determines the type of graph
  - 1 - composite plot of variable displacement with respect to the sled
  - 2 - angular velocity and acceleration
  - 3 - linear velocity and acceleration

Blank and Labeled COMMON Variables:

- $JD$  - integer used to print parameter name in legend
- $JR$  - integer used to print parameter name in legend
- $N$  - number of data points used in velocity and acceleration plots
- $NP$  - number of points used in least square fit

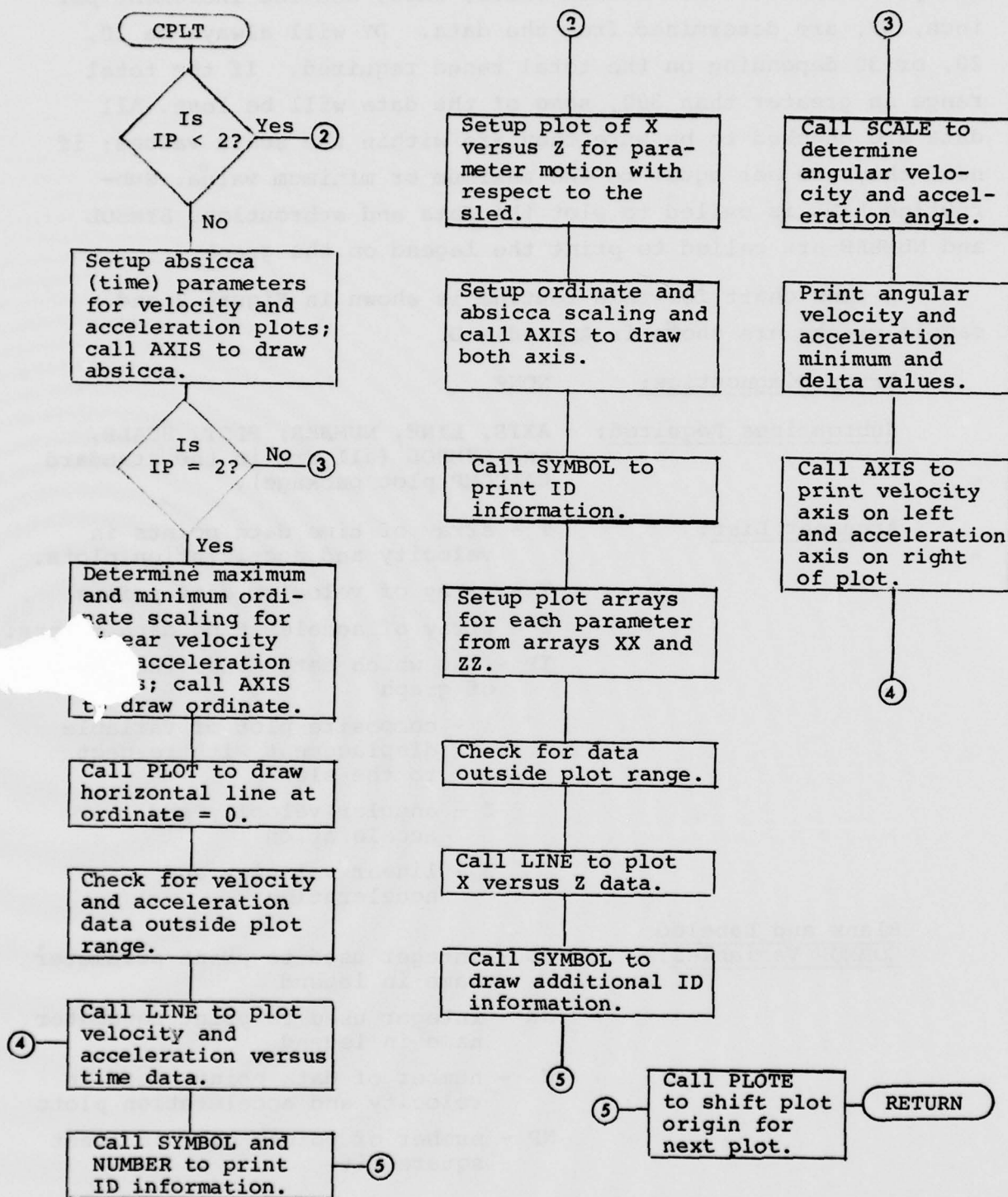


Figure 2. CPLT Flow Chart.

I1 - first point used in composite plot  
 I2 - last point used in composite plot  
 XX - array of X axis displacement data  
 ZZ - array of Z axis displacement data  
 ICAL - flag array which identifies defined data  
     ICAL(J) = 0 - J<sup>th</sup> variable undefined  
     ICAL(J) = 1 - J<sup>th</sup> variable is defined  
 HEADL - array containing variable names used in legend  
 TEST - test identification used in legend  
 IRX - flag used to setup composite plot X axis scale

Subroutine Length: 1363<sub>8</sub>

Labeled Common Length: 23<sub>8</sub>

Blank Common Length: 3456<sub>8</sub>

#### 2.1.2 Subroutine XM(X, Y, YC, N, NP)

Subroutine SM is a smoothing routine which computes a quadratic least square fit of NP dependent variable data points (Y) to compute each smoothed data point (YC). Since NP data points are used to compute each smoothed point, M data points are lost at the beginning and end of array YC, where

$$M = (NP - 1)/2.$$

#### Method

The first (MM) and last (NN) array indices for which YC(I) are computed are determined as follows:

$$MM = M + 1$$

$$NN = N - M$$



where M is defined above and N is the number of original displacement points in array Y. Subroutine QLSQ is called to compute the  $C_1$ ,  $C_2$ , and  $C_3$  coefficients for each of the I smoothed points which are then computed as follows:

$$YC(I) = C_1 * X(I)^2 + C_2 * X(I) + C_3.$$

A flow chart for this routine is shown in Figure 3.

Error Diagnostics: NONE

Subroutines Required: QLSQ

Argument List:

- X = array of independent variable
- Y = array of dependent variable
- YC = array of smoothed dependent variable data
- N = number of original displacement versus time data points
- NP = number of points used to compute each smoothed data point

Subroutine Length: 113<sub>8</sub>

### 2.1.3 Subroutine DERIV1 (X, YP, N, NP, ID)

Subroutine DERIV1 computes the derivative (YP) of the dependent variable Y. A quadratic least square fit of NP points is used to compute each derivative point; thus K points are lost at the beginning and end of array UP:

where

$$\begin{aligned} K &= M + M * ID, \\ M &= (NP - 1)/2, \\ ID &= 1 \text{ for first derivative, and} \\ ID &= 2 \text{ for second derivative.} \end{aligned}$$

Note that for ID = 1, array Y contains displacement data which have already been smoothed using a quadratic least square fit over NP points; thus, M points have already been lost from the original displacement data. For ID = 2, array Y contains first derivative (velocity) data which starts at array location  $Y(2*M + 1)$ .

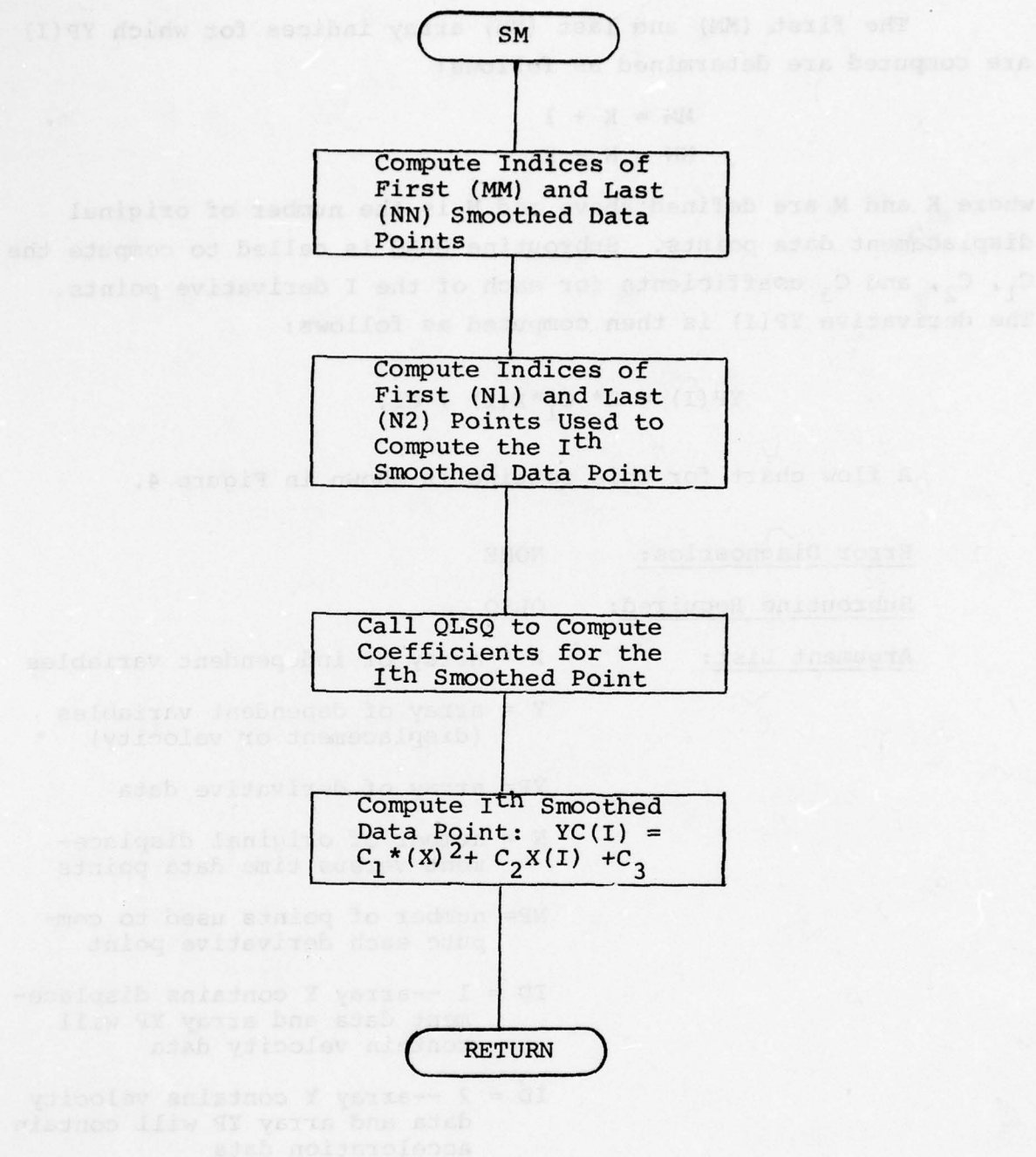


Figure 3. SM Flow Chart.

### Method

The first (MM) and last (NN) array indices for which YP(I) are computed are determined as follows:

$$MM = K + 1$$

$$NN = N - K$$

where K and M are defined above and N is the number of original displacement data points. Subroutine QLSQ is called to compute the  $C_1$ ,  $C_2$ , and  $C_3$  coefficients for each of the I derivative points. The derivative YP(I) is then computed as follows:

$$YP(I) = 2 * C_1 * X(I) + C_2.$$

A flow chart for this routine is shown in Figure 4.

Error Diagnostics: NONE

Subroutine Required: QLSQ

Argument List:

- X = array of independent variables
- Y = array of dependent variables  
(displacement or velocity)
- YP= array of derivative data
- N = number of original displacement versus time data points
- NP= number of points used to compute each derivative point
- ID = 1 --array Y contains displacement data and array YP will contain velocity data
- ID = 2 --array Y contains velocity data and array YP will contain acceleration data

Subroutine Length: 117<sub>8</sub>



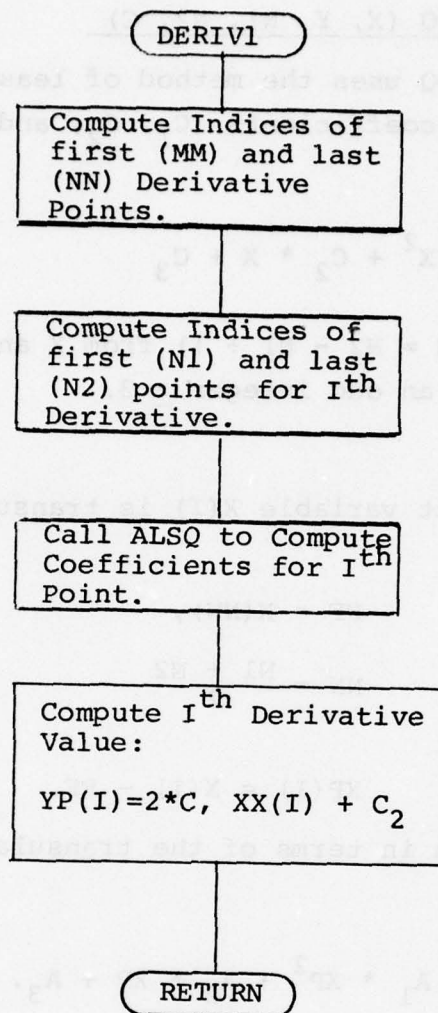


Figure 4. DERIV1 Flow Chart.

#### 2.1.4 Subroutine QLSQ (X, Y, N1, N2, C)

Subroutine QLSQ uses the method of least squares to compute the quadratic coefficients ( $C_1$ ,  $C_2$ , and  $C_3$ ) for an equation of the form:

$$Y = C_1 * X^2 + C_2 * X + C_3$$

for FN data points ( $FN = N2 - N1 + 1$ ) from X and Y array indices N1 to N2. FN must be an odd integer  $\geq 3$ .

##### Method

The independent variable  $X(I)$  is translated by a factor FF, where

$$FF = X(NN),$$

$$NN = \frac{N1 + N2}{2}$$

and

$$XP(I) = X(I) - FF.$$

The quadratic equation in terms of the translated independent variable is

$$Y = A_1 * XP^2 + A_2 * XP + A_3.$$

The least square residuals are a minimum when the following equations are satisfied:

$$A_1 * \sum XP^4 + A_2 * \sum XP^3 + A_3 * \sum XP^2 = \sum XP^2 * Y$$

$$A_1 * \sum XP^3 + A_2 * \sum XP^2 + A_3 * \sum XP = \sum XP * Y$$

$$A_1 * \sum XP^2 + A_2 * \sum XP + A_3 * FN = \sum Y$$

where summations of XP and Y are computed for index I equal N1 to N2. Determinants are used to solve the above system of equations for the coefficients  $A_1$ ,  $A_2$ , and  $A_3$ . The  $C_1$ ,  $C_2$ , and  $C_3$  coefficients are computed from  $A_1$ ,  $A_2$ , and  $A_3$  as follows:

$$C_1 = A_1$$

$$C_2 = A_2 - 2 * A_1 * FF$$

$$C_3 = A_3 + A_1 * FF^2 - A_2 * FF.$$

A flow chart for this routine is shown in Figure 5.

Error Diagnostics: NONE

Subroutines Required: NONE

Argument List: X = array of independent variables  
 Y = array of dependent variables  
 N1 = index of first point used in fit  
 N2 = index of last point used in fit  
 C = array containing quadratic coefficients.

Subroutine Length: 134<sub>8</sub>

## 2.2 DATA PREPARATION FOR INPUT TO HIFPD

Preparation of data for input to HIFPD consists of editing and digitizing. The editing function provides film frame-to-time conversion and film frames coordinates to plane of motion coordinates conversion factors. The digitizing function provides the frame-by-frame "reading" of the projected film frame coordinates. The references, or "standards," required to process the data are film time reference pulses and surveyed fiducials in two planes normal to the optical axis of the camera.

Timing of the film frames was accomplished by calculating the average film speed over a span of approximately 150 frames. The procedure employed to determine the average film speed is described in Appendix B, Paragraph 3.2.



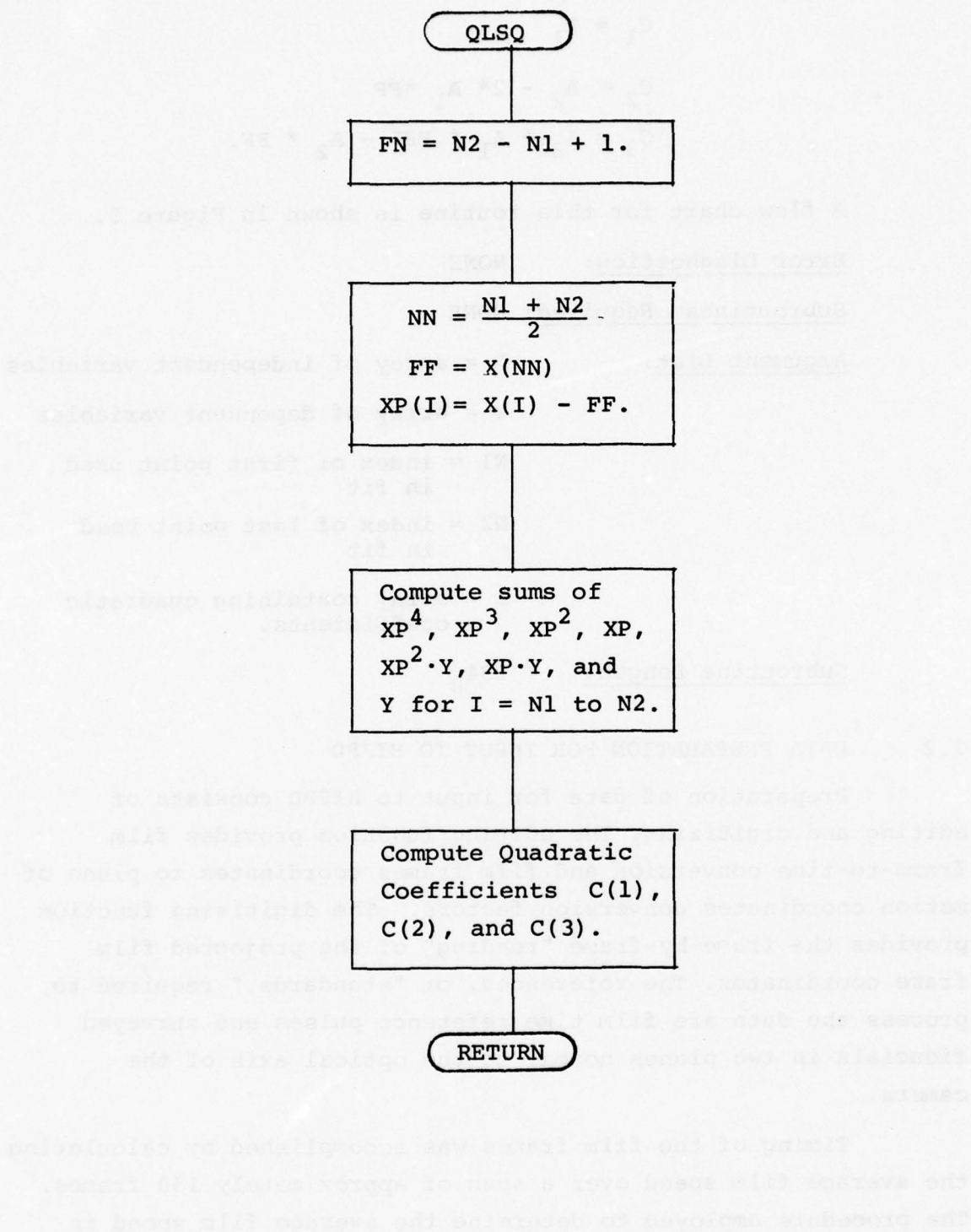


Figure 5. QLSQ Flow Chart.

The first frame in which the stroboscopic flash was observed was defined as  $t = 0$ . The strobe, initiated by a time synchronizing pulse which was also recorded on the magnetic tape recordings, actually gives  $t_0$  indication within 2.0 milliseconds accuracy at the nominal film speed of 500 frames per second with a  $140^\circ$  shutter. Since the flash is not observed in film frame -0001 and is observed in film frame 0000, it is apparent that it was initiated between the closing of the shutter on film frame -0001 and the closing of the shutter on film frame 0000. During most tests, the intensity of the first observed flash would indicate that it was initiated between the closing of the shutter on frame -0001 and the opening of the shutter on frame 000. If this is the case, the  $t_0$  indication could be considered to be accurate to 1.2 milliseconds, i.e.,:

$$\frac{360^\circ - 140^\circ}{360^\circ} \times 2 \text{ msec} = 1.22 \text{ msec.}$$

Determination of conversion constants to be applied to the digitized readings of the anthropometric points on the subject required that the following be known.

- a. The distance, normal to the plane of symmetry of the subject, from that plane to the left edge of the seat pan.
- b. The distance, normal to the plane of symmetry of the subject from that plane, to the lexan panel above the side edge of the sled deck.
- c. The distances, normal to the plane of symmetry of the subject, from that plane to the anthropometric points to be tracked.
- d. That the optical axis of the primary camera was normal to the plane of symmetry of the subject.
- e. The distances, between centers, of the fiducials mounted on the edge of the seat pan and of the fiducials mounted on the lexan panel.

The coordinates of the reference fiducials on the seat pan and the lexan panel were digitized five times. The readings of these coordinates were then averaged and the digital distance between the averaged coordinates of each pair was calculated. Dividing each of these digital distances by the corresponding measured dimension between fiducials yielded conversion constants, in terms of "counts per foot", in two planes normal to the optical axis. Having determined these conversion constants, and having measured the distance between the parallel planes in which the fiducials lay, the distance along the optical axis from the focal point of the lens to each of these planes and the plane of symmetry could then be calculated.

Prior to each test run the breadth of the subject was measured at each tracking fiducial location with an anthropometer. Assuming that each subject was symmetrical, the distance from the plane of symmetry to each tracking fiducial was defined as one-half the measured breadth of the subject of each fiducial location. Conversion constants for each plane parallel to the plane of symmetry, thus normal to the optical axis in which a tracking fiducial lay were then calculated by similar triangles.

The actual digitization of the photometric data was accomplished on a Producers Service Corporation model PVR film analyzer. The magnification factor of the projector was approximately 19.6, giving a projected frame image of 8 x 5.8-inches. The optical encoders were coupled to the reading cross-hairs through drive wires in such a manner that a displacement of either crosshair of one-inch caused the associated optical encoder to increase or decrease the reading by one thousand count.

The operator located the first frame in which the synchronizing flash was observed and reset the frame counter to 0000. The optical center of the film frame was found by



numerically bisecting the vertical and horizontal dimensions of the frame image. The operator then positioned the crosshairs over the range reference fiducial and depressed the record switch causing the frame number and coordinates of the fiducial to be punched into paper tape and typed on the carriage of the teletype terminal. He then proceeded to position the crosshairs over the seat reference fiducial. Again, depressing the record switch caused the coordinates to be recorded on the listing and the paper tape. In this manner he would proceed to each of the other points mentioned in Section 2.1, recording their coordinates, until all readings had been extracted from that frame.

After advancing the film to the next frame, the operator would check the coordinates of the range and seat fiducials. If the frame-to-frame variation of these coordinates exceeded  $\pm 10$  counts he would again locate the optical center of the film frame image before proceeding.

This procedure was repeated for each film frame until the subject appeared to have attained a static position after the impact.

The resulting paper tape was read into file on the CYBER 74 at the ASD computer center from the teletype terminal via data modem on a voice quality line, and the file was edited and corrected when necessary. At this time the control and title data were added to the file. This file was then copied on the card punch and printer as a time saving measure in case the disk file should be accidentally purged.

At this point the program HIFPD could have been attached and executed; however, the normal procedure was to obtain the card files and submit them in the batch mode on an overnight schedule. This permitted the connect time to be used for read-in and editing of additional data files.

A typical standard practice procedure detailing the data preparation is given in Appendix B.

### SECTION 3

#### ANALYSIS OF DATA FROM TWO CAMERAS

Tracking of objects moving through the space of a three-dimensional coordinate system, using analysis of phototheodolite recordings, has been accomplished with a great degree of accuracy for many years. The recognized requirements to accomplish these analyses are quite simple, viz., cameras at two or more tracking stations with precisely synchronized shutters, time for frame signal numbers, azimuth and elevation indicators, and relatively massive mounted systems having provision for leveling and plumbing the cameras. Additionally, the locations of the camera mounts must be accurately surveyed.

When one attempts to track the motion of several points with respect to a three-dimensional coordinate system on a moving vehicle, all the simplicity of the large tracking range disappears, and an entirely new set of problems confront the investigator. Camera weight must be kept to a minimum and light-weight, rigid mounting systems must be devised. Actual shutter synchronization is not practical at the high film transport speeds necessary to record the motion. The precise locations and orientations of the cameras are subject to change, not only from test to test, but even during a test.

To solve the above mentioned problems, two processes were developed, one to accurately determine the location and orientation of a camera with respect to the coordinate system, and the second to track the coordinates of identified points with respect to the origin of the coordinate system.

The processing programs developed to accomplish these solutions, "POOCH" and "SLED" respectively, are described in the following discussions.

### 3.1 CAMERA LOCATION AND ORIENTATION

The value of a program which can determine the location, orientation, and focal length of a camera by examination of the film frame images of a set of accurately surveyed object prints is rather obvious. Regardless of the care exercised, if a large enough amount of camera data is taken, sooner or later a camera will be jarred or moved or a set of camera data will be misplaced or mislabeled, or a camera mounted aboard a moving vehicle may vibrate on its mount and one may wish to do a frame by frame correction of the camera position and orientation.

There are seven unknowns to be determined in this problem. They are the location of the camera focal point ( $xx$ ,  $yy$ ,  $zz$ ), the camera focal length ( $ff$ ), and azimuth angle ( $th$ ) and the elevation angle ( $ph$ ) of the camera optical axis, and the angle ( $\alpha$ ) by which the camera is tilted from horizontal about its optical axis.

Before proceeding with the main theme, a comment must be made regarding the relationship between camera focal length and the distance of the camera from the scene. There is a misconception that if a camera of one focal length is used to photograph a scene, a camera of a shorter focal length will photograph precisely the same scene if taken somewhat closer. That is not true in general. It is true only in the case that every point of the scene being photographed lies in a plane normal to the optical axes of the two cameras.

Although not physically correct, one loses nothing mathematically by assuming that the film frame is interposed between the camera focal point and the scene and that film frame images are created by light rays emanating from the object points and passing through the film to the camera focal point. See Figure 6.



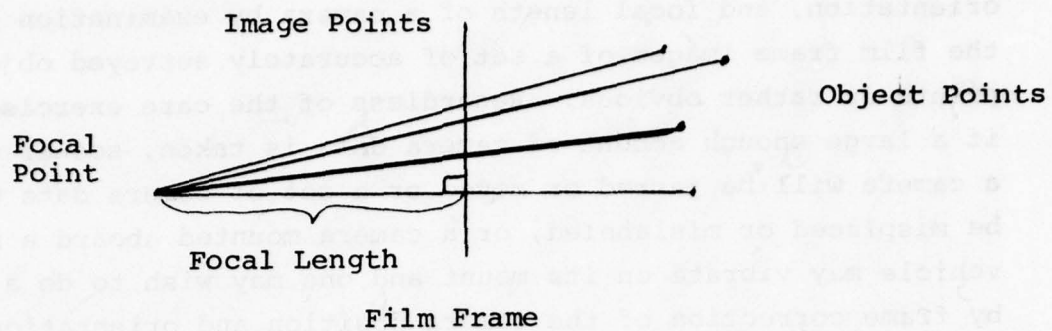


Figure 6.

Assume first that a camera of focal length  $ff$  lies at a distance  $d$  from a scene composed of two object points at heights  $h_a$  and  $h_b$  above its optical axis. See Figure 7.

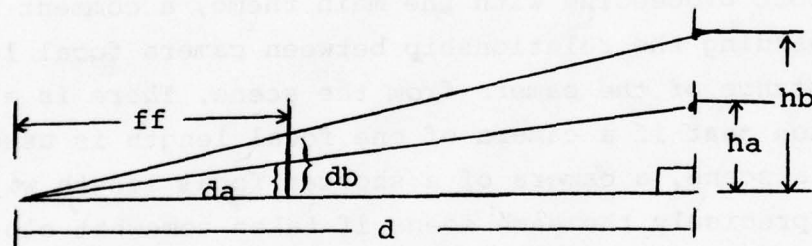


Figure 7.

Both object points lie in a plane normal to the camera optical axis. By similar triangles

$$\frac{d}{ff} = \frac{h_a}{d_a} = \frac{h_b}{d_b}$$

If  $k > 0$ , by the equation

$$\frac{kd}{kff} = \frac{d}{ff}.$$

It is obvious a camera at distance  $kd$  from the object points with a focal length of  $kff$  gives exactly the same image points at the original camera at distance  $d$  with focal length  $ff$ . Thus, if the object points are all in a plane normal to the camera optical axis, it is impossible to determine from the image and object point locations both the camera focal length and its distance from the scene.

If the two object points have different spacings along the camera optical axis, the situation is quite different. See Figure 8.

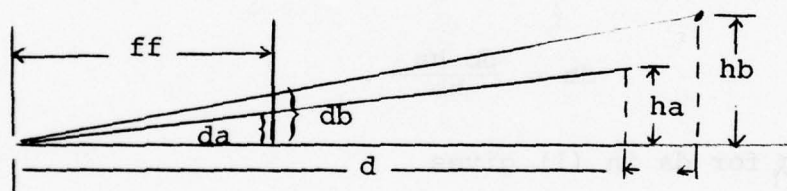


Figure 8.

In Figure 8 the project of the two object points on the camera optical axis are spaced a distance  $e$  apart where  $e$  is known and  $e \neq 0$ .  $da$ ,  $db$ ,  $ha$ , and  $hb$  are known.  $ff$  and  $d$  are unknown.

Again by similar triangles

$$(1) \quad \frac{d}{ha} = \frac{ff}{da}$$

$$(2) \quad \frac{d + e}{hb} = \frac{ff}{db}$$

From (1)  $d = \frac{ha \, ff}{da}$ .

Substituting in (2)  $\frac{\frac{ha \, ff}{da} + e}{hb} = \frac{ff}{db}$ .

or  $\frac{ha \, ff + da \, e}{da \, hb} = \frac{ff}{db}$

or  $db \, ha \, ff + da \, db \, e = da \, hb \, ff.$

$$(3) \quad (da \, hb - db \, ha) \, ff = da \, db \, e.$$

Now if it is assumed that  $da \, hb - db \, ha = 0$ , we get

$$db = \frac{db \, ha}{hb}.$$

Substituting for  $da$  in (1) gives

$$\frac{d}{ha} = \frac{ff}{\left(\frac{db \, ha}{hb}\right)} = \frac{hb \, ff}{db \, ha}.$$

or  $\frac{ff}{db} = \frac{ha}{hb} \frac{d}{ha} = \frac{d}{hb}.$

But (2) is  $\frac{ff}{db} = \frac{d + e}{hb}.$

Therefore,  $\frac{ff}{db} = \frac{d + e}{hb} = \frac{d}{hb}$

$$\frac{e}{hb} = 0$$

$e = 0$  contrary to the problem statement.



da db e

$$(4) \quad ff = \frac{da \, db \, c}{da \, hb - db \, ha} \cdot$$

Substituting for  $ff$  in (1) gives

$$(5) \quad d = \frac{ha}{da} ff = \frac{ha \, db \, e}{da \, hb - db \, ha}$$

and we have in (4) and (5) unique solutions for both  $\delta f$  and

However, two object points with different spacings along the camera optical axis are not sufficient to locate the camera because the camera may be rotated in space about an axis between two object points without disturbing any of the geometrical relationships in Figure 8. See Figure 9.

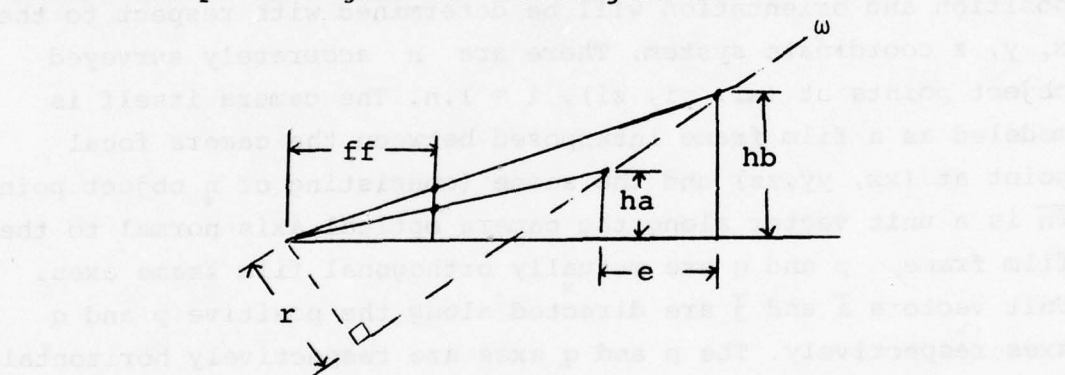


Figure 9.

Figure 9 shows the axis of rotation  $\omega$  and the radius of the circle the camera focal point can describe in space. A third object point lying on the axis between the first two object points does not help to locate the camera. To be of help the third object point must lie at a distance from the line passing through the other two object points. The conclusion is then that in order to completely locate, orient, and determine the focal length of a camera, one requires an absolute minimum of three accurately surveyed object points forming a nondegenerate triangle whose plane was not normal to the camera optical axis when the picture was taken.

With the minimum of three object points, small reading errors can easily distort the solution. In practice it is best to have at least five to eight object points with a good spread normal to the camera optical axis and significant differences in spacing along the optical axis.

The above discussion demonstrating the necessity of at least three object points is in no way indicative of the solution scheme used in the camera location program. The analysis used in the program will now be discussed.

### 3.1.1 Mathematical Models

The problem is modeled or indicated in Figure 10. The principal coordinate system is a right hand mutually orthogonal  $x y z$  coordinate system. Unit vectors  $\bar{e}$ ,  $\bar{n}$ , and  $\bar{h}$  are directed along the positive  $x$ ,  $y$ , and  $z$  axis respectively. The camera position and orientation will be determined with respect to the  $x, y, z$  coordinate system. There are  $n$  accurately surveyed object points at  $(x_i, y_i, z_i)$ ,  $i = 1, n$ . The camera itself is modeled as a film frame interposed between the camera focal point at  $(x_f, y_f, z_f)$  and the scene (consisting of  $n$  object points).  $\bar{f}_n$  is a unit vector along the camera optical axis normal to the film frame.  $p$  and  $q$  are mutually orthogonal film frame axes. Unit vectors  $\bar{i}$  and  $\bar{j}$  are directed along the positive  $p$  and  $q$  axes respectively. The  $p$  and  $q$  axes are respectively horizontal and vertical with respect to the film frame. Throughout this report  $ff$  will be referred to as the camera focal length, but it is actually the product of the true camera focal length and the magnification of the film frame reader. To each of the object points  $(x_i, y_i, z_i)$ ,  $i=1, n$  corresponds to a film frame image point with known film frame coordinates  $(p_i, q_i)$ ,  $i=1, n$ . The unit vectors  $\bar{f}_n$ ,  $\bar{i}$ , and  $\bar{j}$  form a mutually orthogonal right hand set, i.e.,  $\bar{j} = \bar{f}_n \times \bar{i}$ .

To reiterate, the unknowns in this problem are the location of the camera focal point  $(x_f, y_f, z_f)$ , the focal length  $ff$ , the azimuth angle,  $\theta$ , and the elevation angle,  $\phi$ , of the camera optical axis, and the angle,  $\gamma$ , by which the camera is

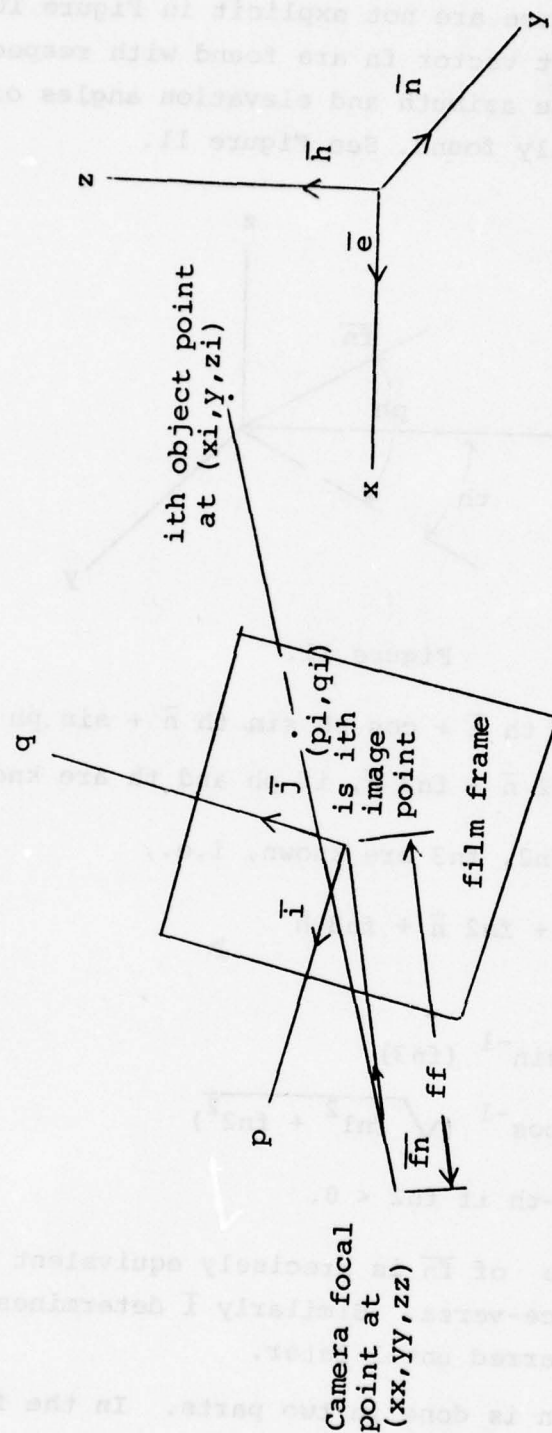


Figure 10.



tilted from horizontal about its optical axis. Of these seven unknowns, the last three are not explicit in Figure 10. If the components of the unit vector  $\bar{f}_n$  are found with respect to the  $x y z$  system, then the azimuth and elevation angles of the camera optical axis are easily found. See Figure 11.

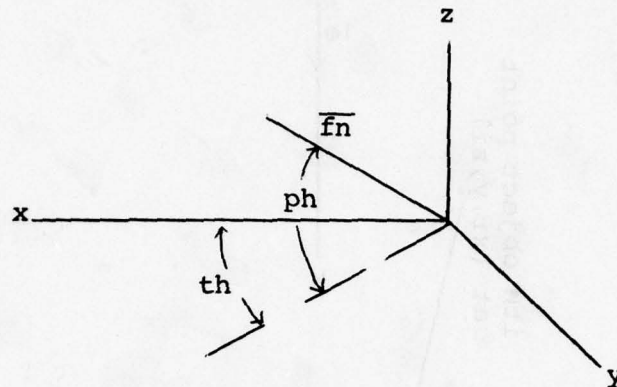


Figure 11.

$$\begin{aligned}\bar{f}_n &= \cos ph \cos th \bar{e} + \cos ph \sin th \bar{n} + \sin ph \bar{h} \\ &= fn1 \bar{e} + fn2 \bar{n} + fn3 \bar{h}, \text{ if } ph \text{ and } th \text{ are known.}\end{aligned}$$

Similarly, if  $fn1$ ,  $fn2$ ,  $fn3$  are known, i.e.,

$$\bar{f}_n = fn1 \bar{e} + fn2 \bar{n} + fn3 \bar{h}$$

Then

$$ph = \sin^{-1} (fn3)$$

$$th = \cos^{-1} (\sqrt{fn1^2 + fn2^2})$$

$$th = -th \text{ if } fn2 < 0.$$

Therefore, knowledge of  $\bar{f}_n$  is precisely equivalent to knowledge of  $th$  and  $ph$  and vice-versa. Similarly  $\bar{I}$  determines  $\gamma$  but the details will be deferred until later.

The solution is done in two parts. In the first part the unknowns  $xx, yy, zz$ , and  $ff$  are found. The angle subtended at the camera focal point by the  $i$ th and  $j$ th image points is  $\gamma_{ij}$  ( $j \neq i$ ). See Figure 12.

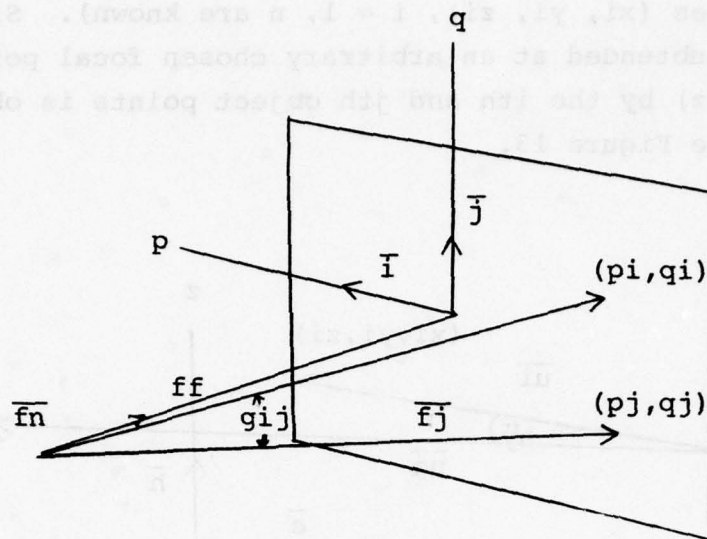


Figure 12.

Although the components of the unit vectors  $\bar{f}_n$ ,  $\bar{i}$ , and  $\bar{j}$  are not known at present with respect to the xyz system, it is known that they form a right hand mutually orthogonal set. So vectors  $\bar{f}_i$  and  $\bar{f}_j$  to the ith and jth image points may be written:

$$\bar{f}_i = ff \bar{f}_n + p_i \bar{i} + q_i \bar{j}$$

$$\bar{f}_j = ff \bar{f}_n + p_j \bar{i} + q_j \bar{j}$$

Then the angle  $g_{ij}$  subtended by  $\bar{f}_i$  and  $\bar{f}_j$  at the camera focal point is:

$$g_{ij} = \cos^{-1} \left( \frac{\bar{f}_i \cdot \bar{f}_j}{|\bar{f}_i| |\bar{f}_j|} \right)$$

$$g_{ij} = \cos^{-1} \left\{ \frac{ff^2 + p_i p_j + q_i q_j}{(ff^2 + p_i^2 + q_i^2)^{1/2} (ff^2 + p_j^2 + q_j^2)^{1/2}} \right\}$$

and the only unknown appearing in the equation for  $\ddot{h}_y$  is  $ff$ . (All image point coordinates  $(p_i, q_i)$ ,  $i = 1, n$  and all object point coordinates  $(x_i, y_i, z_i)$ ,  $i = 1, n$  are known). Similarly, the angle  $\ddot{h}_y$  subtended at an arbitrary chosen focal point location  $(xx, yy, zz)$  by the  $i$ th and  $j$ th object points is obtained as follows. See Figure 13.

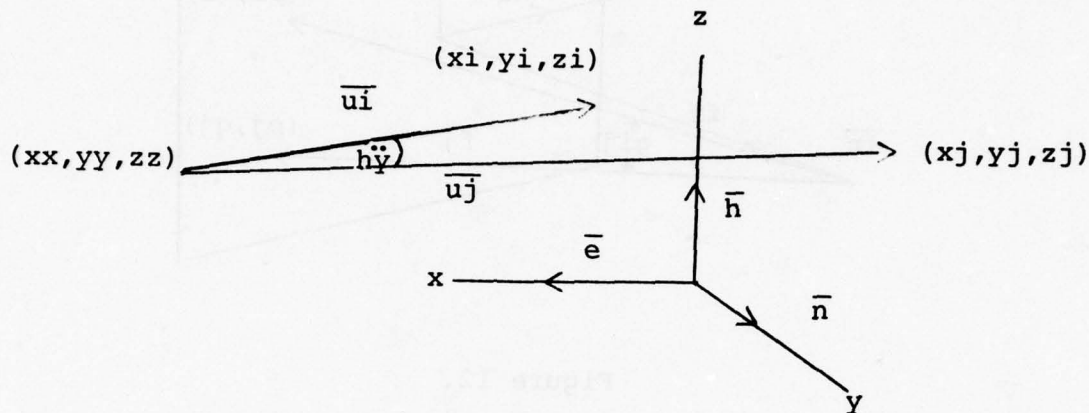


Figure 13.

$$\ddot{h}_y = \cos^{-1} \left( \frac{\overline{u_i} \cdot \overline{u_j}}{|\overline{u_i}| |\overline{u_j}|} \right)$$

where

$$\overline{u_i} = (x_i - xx) \bar{e} + (y_i - yy) \bar{n} + (z_i - zz) \bar{h}$$

$$\overline{u_j} = (x_j - xx) \bar{e} + (y_j - yy) \bar{n} + (z_j - zz) \bar{h}$$

$$\ddot{h}_y = \cos^{-1} \left\{ \frac{(x_i - xx)(x_j - xx) + (y_i - yy)(y_j - yy) + (z_i - zz)(z_j - zz)}{[(x_i - xx)^2 + (y_i - yy)^2 + (z_i - zz)^2]^{1/2} [(x_j - xx)^2 + (y_j - yy)^2 + (z_j - zz)^2]^{1/2}} \right\}$$

and the only unknowns in the  $\ddot{h}_y$  equation are  $xx$ ,  $yy$ , and  $zz$ .

Thus we have

$$\ddot{g_y} = g_y (ff),$$

a function of  $ff$ , and

$$\ddot{h_y} = \ddot{h_y} (xx, yy, zz),$$

a function of focal point position. If the correct values of  $ff$ ,  $xx, yy, zz$  are inserted in these two equations, we should have

$$\ddot{g_y}(ff) = \ddot{h_y} (xx, yy, zz).$$

Define  $\text{err}_y = (\ddot{g_y} - \ddot{h_y})^2$ , and

$$\text{err}_y = \text{err}_y (ff, xx, yy, zz).$$

Then the total error  $\text{err}$  taken over all possible pairs of points is, for an arbitrary choice of  $ff, xx, yy, zz$

$$\text{err} = \sum_{i=1}^{n-1} \sum_{j=1}^n \text{err}_{ij} (= \text{err}(ff, xx, yy, zz)).$$

Then we should have at the correct values  $ff, xx, yy, zz$   $\text{err} = 0$ .

Due to the film frame reading errors, errors in the surveyed object points, lens distortion,  $\text{err} \neq 0$  at the correct value of  $ff, xx, yy, zz$ , but it will attain a relative minimum there. Let  $fp$  and  $fq$  be numbers chosen so as to be generous bounds on the true focal length  $ff$ .  $0 < fp < ff < fq$ . Let  $(xq, yq, zq)$  be the  $x y z$  values that minimize  $\text{err} (fq, x, y, z)$ , that is,  $\text{err} (fq, xq, yq, zq)$  is the smallest value of  $\text{err}$  that can be obtained for focal length of  $fq$ . Similarly, let  $\text{err} (fp, xp, yp, zp)$  be the minimum of  $\text{err}$  for focal length  $fp$ . As one would expect, the optimized position of the focal point is closer to the scene for the smaller value of focal length. See Figure 14.



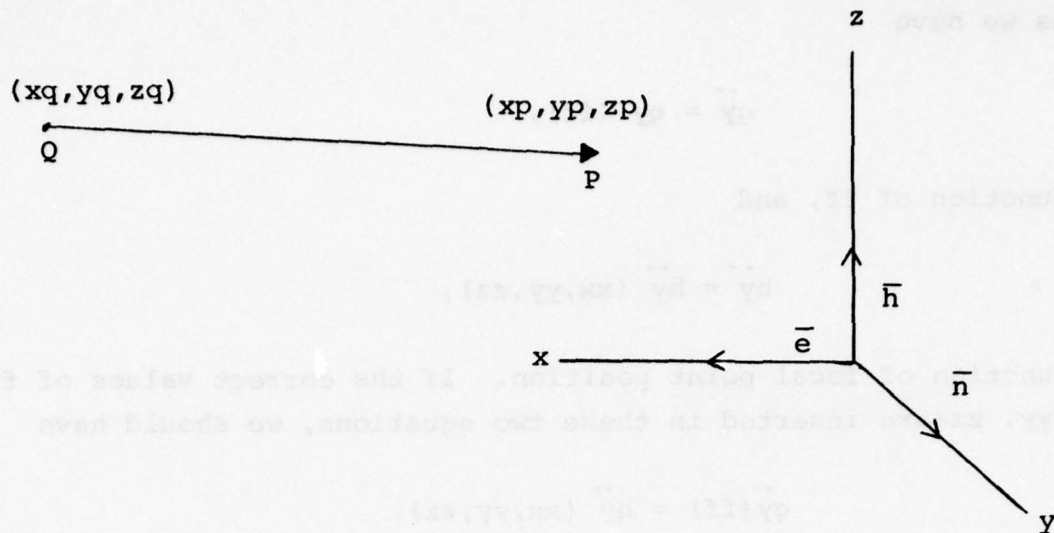


Figure 14.

Let  $f_s$  be any focal length value such that  $f_p < f_s < f_q$ . Let  $(x_s, y_s, z_s)$  be that point that minimizes  $\text{err}$ , i.e.,  $\text{err}(f_s, x_s, y_s, z_s)$  is a minimum for focal length  $f_s$ . Then the following proportions furnish excellent estimates of  $x_s, y_s$ , and  $z_s$  for a given focal length  $f_s$ .

$$\frac{x_s - x_p}{x_q - x_p} = \frac{f_s - f_p}{f_q - f_p}$$

$$\frac{y_s - y_p}{y_q - y_p} = \frac{f_s - f_p}{f_q - f_p}$$

$$\frac{z_s - z_p}{z_q - z_p} = \frac{f_s - f_p}{f_q - f_p}.$$

In other words, as  $f_s$  varies from  $f_p$  to  $f_q$ , it is very nearly true that the point  $(x_s, y_s, z_s)$  moves a proportional amount of the distance from  $p$  to  $q$  along the line segment. Solving the equation for  $(x_s, y_s, z_s)$  gives

$$x_s = x_p + (x_q - x_p) \frac{f_s - f_p}{f_q - f_p}$$

$$y_s = y_p + (y_q - y_p) \frac{f_s - f_p}{f_q - f_p}$$

$$z_s = z_p + (z_q - z_p) \frac{f_s - f_p}{f_q - f_p} .$$

The application of these equations will be discussed shortly.

A graph of the minimized value of err versus focal length has the form illustrated in Figure 15.

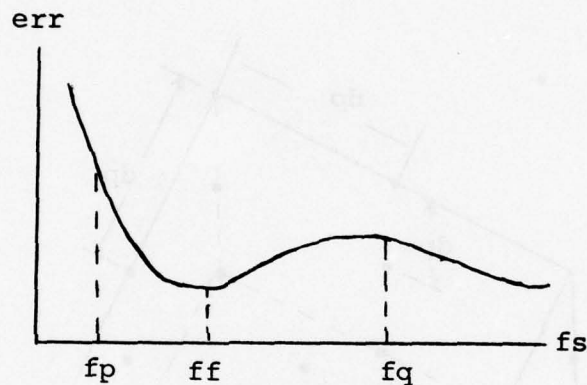


Figure 15.

The relative minimum of err for  $f_s$   $[f_p, f_q]$  occurs at  $ff$ . Of course as  $f_s \rightarrow \infty$ , both the scene and the film frame shrink to points with respect to the camera focal point, so err will approach the  $f_s$  axis asymptotically from above.

When data is input to the program, rough estimates of  $ff$ ,  $xx$ ,  $yy$ ,  $zz$  are read in. Also input are two generous bounds on  $ff$ ,  $f_p$ , and  $f_q$  where  $0 < f_p < ff < f_q$ . The first step is to locate the points P and Q. Assume we are searching for point P in Figure 14, that point  $(x_p, y_p, z_p)$  that makes err  $(f_p, x_p, y_p, z_p)$  a minimum for focal length  $f_p$ .

A cube of 27 points is centered at the input point  $(xx, yy, zz)$ . See Figure 16. The cube's edges are parallel to the principal coordinate system axes and it has edge length  $2 dp$  where  $dp$  is an internally defined value. Err  $(fp, x, y, z)$  is computed at each of the cube points. Then  $(xx, yy, zz)$  are set equal to the coordinates of that point that resulted in the smallest value of err. Then a new cube is constructed centered on a new point  $(xx, yy, zz)$  and the process repeated. Ultimately a cube is found whose center point gives the smallest value of

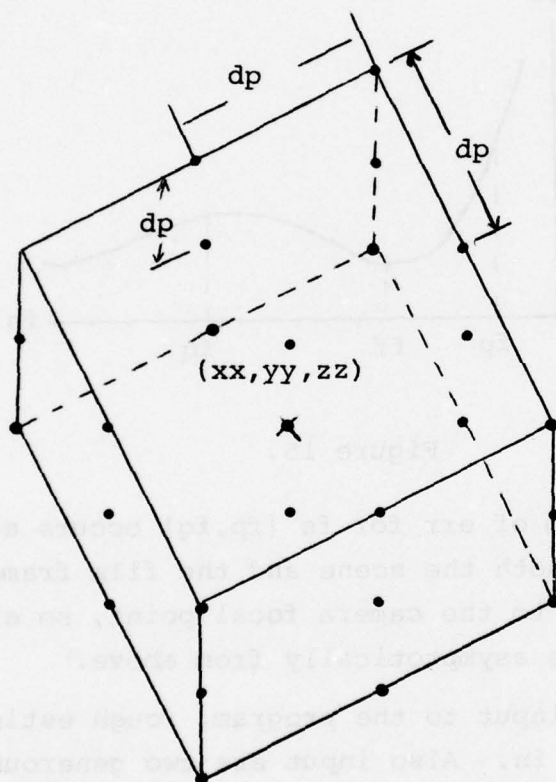


Figure 16.

err. This cube then contains the optimum point.  $dp$  is then reduced to a tenth of its previous value, a new smaller cube centered on the minimum point is constructed and the whole process is repeated again. This iterative process is terminated when  $dp$  falls below a certain test value. Then  $(xp, yp, zp)$  is set equal to the coordinates of the last minimum point determined. This is the process used to determine for  $ff = fp$ , and  $ff = fq$  the best camera focal point locations  $(xp, yp, zp)$  and  $(xq, yq, zq)$  respectively. The above process is capable of moving the focal point many feet through space from a grossly inaccurate first estimate to the final optimizing point. But this iteration is quite time consuming. For example, if 20 cubes are required to locate an optimum point, it requires the computation of  $err$  at  $20 \times 27 = 540$  points. And if there are, say, 9 object points, there are  $\frac{9 \times 8}{2} = 36$  values of  $h\dot{y}$  and  $g\dot{y}$  that must be computed, differenced, squared, and added for each computation of  $err$ . For this reason, the above process is not used to make the final determination of the focal length. Rather for each value of focal length  $fs$  used in this determination, a very nearly optimum point for optimizing  $err$  is gotten from the three proportions mentioned earlier on page 38.

$$xs = xp + \frac{fs - fp}{fq - fp} (xq - xp)$$

$$ys = yp + \frac{fs - fp}{fq - fp} (yq - yp)$$

$$zs = zp + \frac{fs - fp}{fq - fp} (zq - zp).$$

Then  $err$  is minimized at  $fs$  by checking points very close to  $(xs, ys, zs)$  by a simpler, faster process to be described shortly. To find the correct value of  $ff$  we set

$$dist = (fq - fp) / 6.0.$$

Then  $fs$  is set equal to  $fq + i \text{ dist}$ ,  $i = 0, 1, 2, \dots, 6$  in succession and the minimum error values  $err$  found for each  $fs$ .



Say it occurs at  $fs = fso$ . Then we redefine  $fq = fso + dist$  and  $fp = fso - dist$ , set  $dist = (fq - fp) / 6.0$  and go through the same process all over again. This is continued until  $dist$  falls below a present value. Then  $ff$  is set equal to the last  $fs$  computed and  $(xx, yy, zz)$  to the last optimized value of  $(xs, ys, zs)$ . This is the final step in solving for these first four of the seven unknowns in this problem.

In order to construct the routine which is used to optimize the initial values of  $(xs, ys, zs)$  gotten from the three equations above, reference must be made to Figure 17.

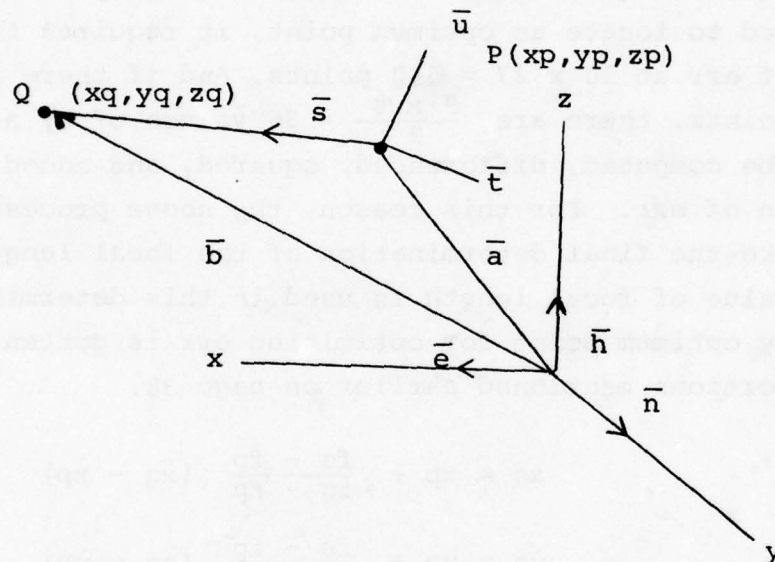


Figure 17.

$$\vec{a} = f_p \vec{e} + y_p \vec{n} + g_p \vec{h}$$

$$\vec{b} = x_q \vec{e} + y_q \vec{n} + z_q \vec{h}.$$

The unit vectors defined as follows are the directions in space along which the iterative procedure searches in order to optimize the initial values of  $(xs, ys, zs)$  to find the minimum value of  $err$  for focal length  $fs$ .

$$\bar{s} = \frac{\bar{b} - \bar{a}}{|\bar{b} - \bar{a}|}$$

$$\bar{t} = \frac{\bar{h} \times \bar{s}}{|\bar{h} \times \bar{s}|}$$

$$\bar{u} = \bar{s} \times \bar{t}.$$

Defined in this way,  $\bar{s}$ ,  $\bar{t}$ , and  $\bar{u}$  form a right hand set of mutually orthogonal unit vectors with  $\bar{s}$  lying along the line segment between points p and q. A maximum of six computations of err are required for each iteration as opposed to the 27 required for the cube search. The order in which the points are tried is indicated in Figure 18.

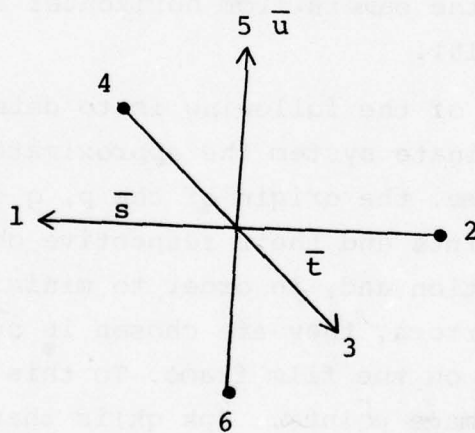


Figure 18.

The value of err is known at the junction of  $\bar{s}$ ,  $\bar{t}$ , and  $\bar{u}$  (referred to as the center point). The points 1 through 6 are tried in order. If the value of err at any of points 1 through 6 is smaller than that at the center point, the next step will be in the same direction. For example, if point 3 should be the first point to yield a smaller value of err than that at the center point, the routine will continue to step in the  $\bar{t}$  direction so long as successively smaller values of err are obtained.

Similarly as for the cube search, when all of points 1 through 6 yield a higher value of err than that at the center point, the step size is reduced and the whole process repeated. This continues until the step distance falls below a certain present value.

The location of the camera focal point and its focal length have now been found to be  $(xx, yy, zz)$  and  $ff$  respectively. As mentioned previously, the determination of the components of the unit vectors  $\bar{f}_n$  and  $\bar{i}$  with respect to the principal coordinate system is equivalent to finding the azimuth and elevation of the optical axis and the tilt angle of the camera from horizontal about the optical axis (refer to Figure 10).

The whole point of the following is to determine with respect to the principal coordinate system the approximate location of the center of the film frame, the origin of the  $p, q$  film frame coordinate system. Three image points and their respective object points are required to get a solution and, in order to minimize the effects of reading and other errors, they are chosen in such a way as to form a large triangle on the film frame. To this end, three sorts are performed on the image points.  $(pk, qk)$  is that point farthest from the film frame origin.  $(pl, ql)$  is that point farthest from  $(pk, qk)$ .  $(pm, qm)$  is that point the sum of whose distances from  $(pk, qk)$  and  $(pl, ql)$  is the greatest. See Figure 19.

The vectors from the camera focal point to the  $k$ th,  $l$ th, and  $m$ th image points are respectively:

$$\overline{skc} = ff \overline{fn} + pk \overline{i} + qk \overline{j}$$

$$\overline{slc} = ff \overline{fn} + pl \overline{i} + ql \overline{j}$$

$$\overline{smc} = ff \overline{fn} + pm \overline{i} + qm \overline{j}$$

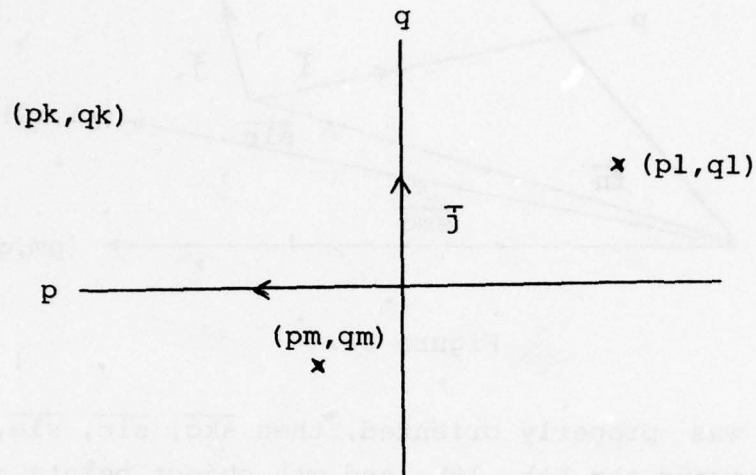


Figure 19.

where these three vectors have been written in terms of their components with respect to these as-yet-unknown unit vectors,  $\overline{fn}$ ,  $\overline{i}$ ,  $\overline{j}$  of the camera coordinate system. The vector magnitudes are

$$dfk = (ff^2 + pk^2 + qk^2)^{1/2}$$

$$dfl = (ff^2 + pl^2 + ql^2)^{1/2}$$

$$dfm = (ff^2 + pm^2 + qm^2)^{1/2}$$

See Figure 20.



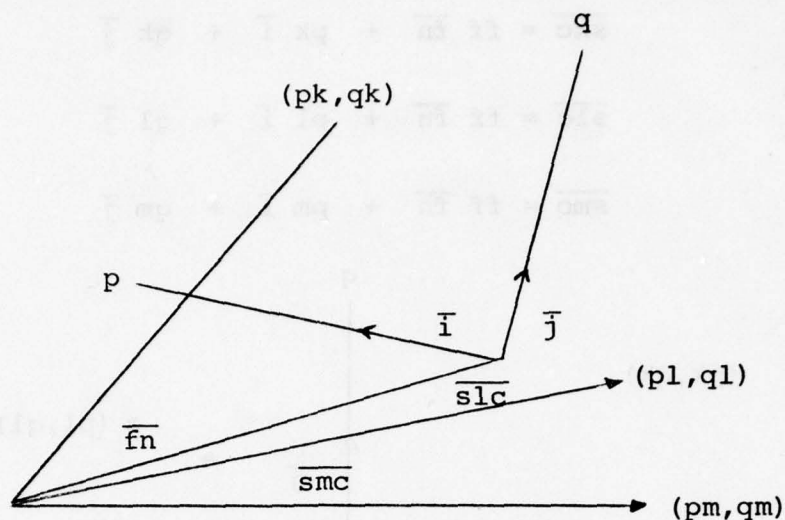


Figure 20.

If the camera was properly oriented, then  $\overline{skc}$ ,  $\overline{sic}$ ,  $\overline{sle}$ , and  $\overline{sme}$  should point toward the  $k$ th,  $l$ th, and  $m$ th object points respectively. Unit vectors  $\overline{nfa}$ ,  $\overline{nfb}$ , and  $\overline{nfc}$  pointing at the  $k$ th,  $l$ th, and  $m$ th object points respectively obtained as follows:

$$\overline{fa} = (x_k - x_x) \overline{e} + (y_k - y_y) \overline{n} + (z_k - z_z) \overline{h}$$

$$\overline{fb} = (x_l - x_x) \overline{e} + (y_l - y_y) \overline{n} + (z_l - z_z) \overline{h}$$

$$\overline{fc} = (x_m - x_x) \overline{e} + (y_m - y_y) \overline{n} + (z_m - z_z) \overline{h}$$

$$d_{am} = / \overline{fa} / = [(x_h - x_x)^2 + (y_k - y_y)^2 + (z_k - z_z)^2]^{1/2}$$

$$d_{bm} = / \overline{fb} / = [(x_l - x_x)^2 + (y_l - y_y)^2 + (z_l - z_z)^2]^{1/2}$$

$$d_{cm} = / \overline{fc} / = [(x_m - x_x)^2 + (y_m - y_y)^2 + (z_m - z_z)^2]^{1/2}$$

$$\overline{nfa} = \overline{fa} / d_{am}$$

$$\overline{nfb} = \overline{fb} / d_{bm}$$

$$\overline{nfc} = \overline{fc} / d_{cm}.$$

Multiplying these unit vectors by the magnitudes of  $\overline{s_{kc}}$ ,  $\overline{s_{lc}}$ , and  $\overline{s_{mc}}$  gives  $\overline{s_k}$ ,  $\overline{s_l}$ , and  $\overline{s_m}$  below

$$\overline{s_k} = dfk \overline{n_{fa}}$$

$$\overline{s_l} = dfl \overline{n_{fb}}$$

$$\overline{s_m} = dfm \overline{n_{fc}}.$$

The vectors  $\overline{s_k}$ ,  $\overline{s_l}$ , and  $\overline{s_m}$  so defined are known with respect to the principal program coordinate system. More over, they are very nearly equal to  $\overline{s_{kc}}$ ,  $\overline{s_{lc}}$ , and  $\overline{s_{mc}}$ ; that is:

$$s_k \approx s_{kc}$$

$$s_l \approx s_{lc}$$

$$s_m \approx s_{mc}.$$

See Figure 21.

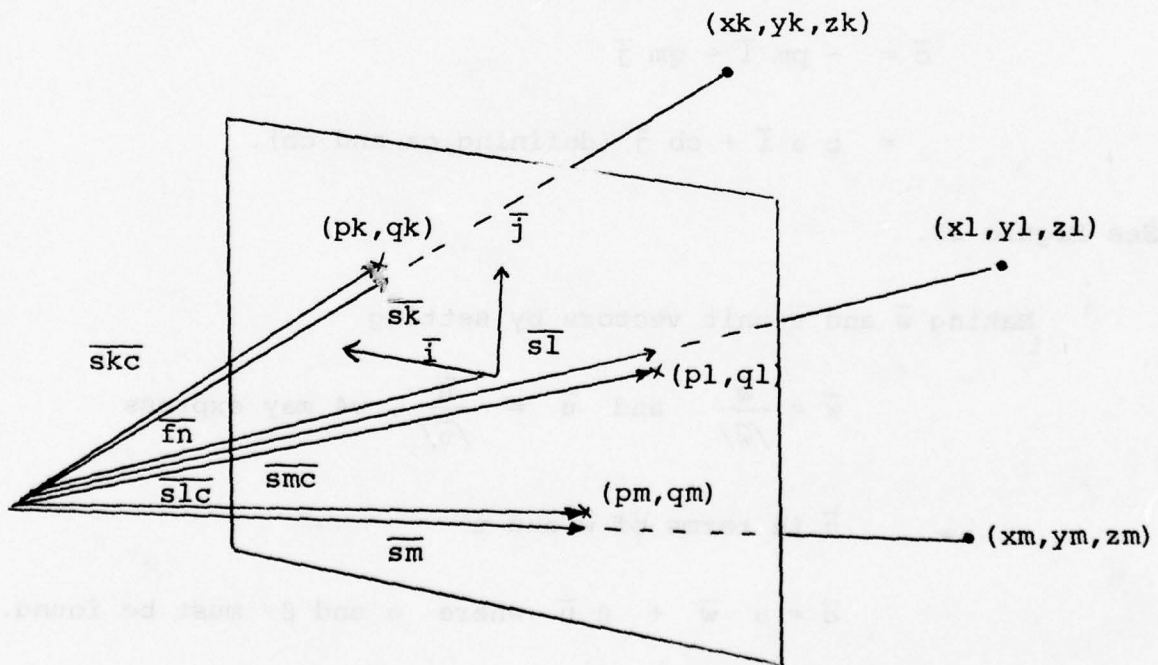


Figure 21.

Were it not for the various errors, the above equivalence would be exact and the unknown unit vectors  $\bar{f}_n$ ,  $\bar{i}$ , and  $\bar{j}$  could be solved for directly. The solution could be done anyway, but the resulting solution vectors  $\bar{f}_n$ ,  $\bar{i}$ , and  $\bar{j}$  would in general be neither unit vectors nor would they be mutually perpendicular. Of course, the resulting system could be made orthonormal algebraically, but it was not known at the time how large errors would be nor how much distortion would be produced by the errors. It was decided to take advantage of the approximate vector equivalence above in the following manner in order to determine  $\bar{f}_n$ ,  $\bar{i}$ , and  $\bar{j}$ .

Let

$$\bar{w} = \overline{skc} - \overline{smc} = (pk - pm) \bar{i} + (qk - qm) \bar{j}$$

$$\bar{u} = \overline{slc} - \overline{smc} = (pl - pm) \bar{i} + (ql - qm) \bar{j}.$$

A vector  $\bar{c}$  from the image point in to the center of the film frame is

$$\begin{aligned} \bar{c} &= -pm \bar{i} - qm \bar{j} \\ &= ca \bar{i} + cb \bar{j} \text{ (defining } ca \text{ and } cb). \end{aligned}$$

See Figure 22.

Making  $\bar{w}$  and  $\bar{u}$  unit vectors by setting

$$\bar{w} = \frac{\bar{w}}{|\bar{w}|} \quad \text{and} \quad \bar{u} = \frac{\bar{u}}{|\bar{u}|}, \text{ we may express}$$

$\bar{c}$  in terms of  $\bar{w}$  and  $\bar{u}$

$$\bar{c} = \alpha \bar{w} + \beta \bar{u} \text{ where } \alpha \text{ and } \beta \text{ must be found.}$$

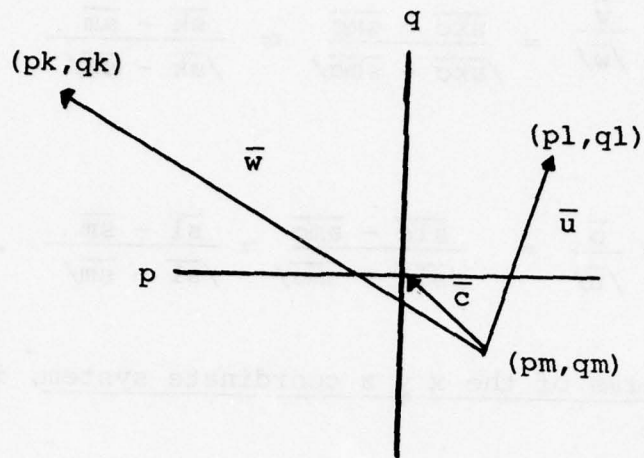


Figure 22.

Equating  $\bar{i}$  and  $\bar{j}$  components gives:

$$\alpha w_a + \beta u_a = c_a$$

$$\alpha w_b + \beta u_b = c_b$$

and

$$\alpha = \begin{vmatrix} c_a & u_a \\ c_b & u_b \end{vmatrix}$$

$$\beta = \begin{vmatrix} w_a & c_a \\ w_b & c_b \end{vmatrix}$$

where

$$\Delta = \begin{vmatrix} w_a & u_a \\ w_b & u_b \end{vmatrix}.$$



Now,

$$\bar{w} = \frac{\bar{w}}{/\bar{w}/} = \frac{\overline{skc} - \overline{smc}}{/\overline{skc} - \overline{smc}/} \approx \frac{\overline{sk} - \overline{sm}}{/\overline{sk} - \overline{sm}/}$$

and

$$\bar{u} = \frac{\bar{u}}{/\bar{u}/} = \frac{\overline{slc} - \overline{smc}}{/\overline{slc} - \overline{smc}/} \approx \frac{\overline{sl} - \overline{sm}}{/\overline{sl} - \overline{sm}/}.$$

Therefore, in terms of the x y z coordinate system, it is approximately true that

$$c = \alpha \frac{\overline{sk} - \overline{sm}}{/\overline{sk} - \overline{sm}/} + \beta \frac{\overline{sl} - \overline{sm}}{/\overline{sl} - \overline{sm}/}.$$

So a vector from the focal point to the center of the film frame is approximately:

$$\overline{cff} = \overline{sm} + \bar{c}$$

and

$$\begin{aligned} \bar{fn} &= \frac{\overline{cff}}{/\overline{cff}/} \\ &= fn\ 1\ \bar{e} + fn\ 2\ \bar{n} + fn\ 3\ \bar{h}. \end{aligned}$$

See Figure 23.

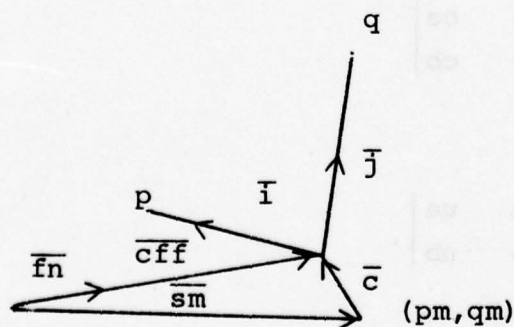


Figure 23.

Then the azimuth  $th$  and the elevation  $ph$  of the optical axis are approximately

$$th = \cos^{-1} \left[ \frac{fn \ 1}{\{(fn \ 1)^2 + (fn \ a)^2\}^{1/2}} \right]$$

$$\text{If } (fn \ 2 < 0.0), th = -th \quad (-\pi \leq th \leq \pi)$$

$$ph = \sin^{-1} (fn \ 3) \quad \left( \frac{\pi}{2} \leq ph \leq \frac{\pi}{2} \right)$$

In order to find the approximate direction of the film frame vector  $\bar{i}$  with respect to the  $x \ y \ z$  coordinate system two new unit vectors  $\bar{i}'$  and  $\bar{j}'$  are constructed. These lie in the film frame as do  $\bar{i}$  and  $\bar{j}$  and they also form with  $fn$  a right-handed trio of mutually orthogonal vectors. See Figure 24.

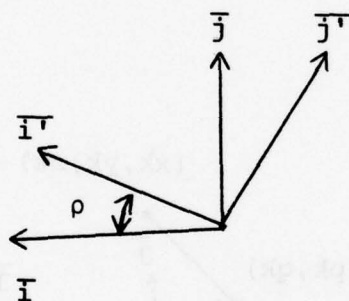


Figure 24.

In order to have a unit vector  $\bar{i}'$  which will always be well defined regardless of the orientation of the camera optical axis  $\bar{fn}$ ,  $\bar{i}'$  is derived from that component of the vector joining object points  $k$  and  $l$  that lies parallel to the film frame, that is, normal to  $\bar{fn}$ . It will be recalled that image points  $k$  and  $l$  had the greatest separation of any point pair on the film frame.  $\rho$  is the angle to be solved for once  $\bar{i}'$  and  $\bar{j}'$  have been found.



Figure 25 and the following discussion give the derivation of  $\bar{i}'$  and  $\bar{j}'$ .

$$\begin{aligned}\bar{p}ip &= (x_k - x_l) \bar{e} + (y_k - y_l) \bar{n} + (z_k - z_l) \bar{h} \\ &= \bar{p}ipa \bar{e} + \bar{p}ipb \bar{n} - \bar{p}ipc \bar{h}.\end{aligned}$$

To subtract from  $\bar{p}ip$  a vector parallel to  $\bar{f}n$  leaving a difference vector  $\bar{p}i$  normal to  $\bar{f}n$  requires the solution of the following equation for the scalar  $a$ .

$$(\bar{p}ip - a \bar{f}n) \cdot \bar{f}n = 0$$

$$\bar{p}ip \cdot \bar{f}n - a \bar{f}n \cdot \bar{f}n = 0$$

or, since  $|\bar{f}n| = (\bar{f}n \cdot \bar{f}n)^{1/2} = 1$ ,

$$a = \bar{p}ip \cdot \bar{f}n.$$

So  $\bar{p}i = \bar{p}ip - \bar{p}ip \cdot \bar{f}n \bar{f}n$  is parallel to the film frame, i.e., normal to  $\bar{f}n$ .

$$\bar{i}' = \frac{\bar{p}i}{|\bar{p}i|}$$

$$\bar{j}' = \bar{f}n \cdot \bar{i}'.$$

To find  $\rho$  the  $k$ th image and object points are used as follows. See Figure 26.

$$\bar{r} = p_k \bar{i} + q_k \bar{j}$$

$$\bar{i} = \cos \rho \bar{i}' + \sin \rho \bar{j}'$$

$$\begin{aligned}\bar{j} &= \cos \left( \rho + \frac{\pi}{2} \right) \bar{i}' + \sin \left( \rho + \frac{\pi}{2} \right) \bar{j}' \\ &= -\sin \rho \bar{i}' + \cos \rho \bar{j}'\end{aligned}$$



$\overline{fa}$  is a vector from the focal point to the impage point  $(pk, qk)$ .

$$\overline{fa} = (ff^2 + pk^2 + qk^2)^{1/2} \frac{[(xk-xx)\overline{e} + (yk-yy)\overline{n} + (zk-zz)\overline{h}]}{[(xk-xx)^2 + (yk-yy)^2 + (zk-zz)^2]^{1/2}}$$

$$\overline{fa} = faa \overline{e} + fab \overline{n} + fac \overline{h}$$

$$\overline{ff} = ff \overline{fn} - ff fn1\overline{e} + ff fn2\overline{n} + ff fn3\overline{h}$$

$$= ffa \overline{e} + ffb \overline{n} + ffc \overline{h}$$

$$\overline{r} = \overline{fa} - \overline{ff}.$$

$$\text{So } pk \overline{i} + qk \overline{j} = \overline{fa} - \overline{ff}.$$

Substituting for  $\overline{i}$  and  $\overline{j}$  their expressions in  $\overline{i}'$  and  $\overline{j}'$  gives

$$pk \cos \rho \overline{i}' + pk \sin \rho \overline{j}' - qk \sin \rho \overline{i}' + qk \cos \rho \overline{j}' = \overline{fa} - \overline{ff}$$

$\overline{fa} - \overline{ff}$  can then be written as

$$\overline{fa} - \overline{ff} = (\overline{fa} - \overline{ff}) \cdot \overline{i}' \overline{i}' + (\overline{fa} - \overline{ff}) \cdot \overline{j}' \overline{j}'$$

Equating components of  $\overline{i}'$  and  $\overline{j}'$  gives the following scalar equations in which  $\rho$  is the only unknown.

$$pk \cos \rho - qk \sin \rho = (\overline{fa} - \overline{ff}) \cdot \overline{i}' = \text{ela (defining ela)}$$

$$pk \sin \rho + qk \cos \rho = (\overline{fa} - \overline{ff}) \cdot \overline{j}' = \text{elb (defining elb)}.$$

Solving the above equations gives  $\rho$ .

Then  $\overline{i} = \cos \rho \overline{i}' + \sin \rho \overline{j}'$  where the components of  $\overline{i}'$  and  $\overline{j}'$  are known with respect to the x y z coordinate system. So we get  $\overline{i} = gia \overline{e} + gib \overline{n} + gic \overline{h}$  where the  $gia$ ,  $gib$ ,  $gic$  are obtained by substituting for  $\overline{i}'$  and  $\overline{j}'$  their expressions in  $\overline{e}$ ,  $\overline{n}$ , and  $\overline{h}$ . Then the azimuth  $\theta$  and elevation  $\phi$  of  $\overline{i}$  are found as follows:

$$\text{thi} = \cos^{-1} \left[ \frac{\text{gia}}{(\text{gia}^2 + \text{gib}^2)^{1/2}} \right]$$

If gib is less than 0.0, set thi = - thi.

$$\text{phi} = \sin^{-1} (\text{gic}).$$

The unit vectors  $\overline{\text{fn}}$  and  $\overline{\text{i}}$  obtained above complete the orientation of the camera, but they are only approximate. They depend on the values of th, ph, and  $\rho$ . The values of th, ph, and  $\rho$  found above should be very close to the correct values. To find that combination of th, ph, and  $\rho$  which best aligns all the image points we construct an error sum as follows. Due to the various errors, the point at which a ray from the focal point to an object point pierces the film frame is not identical to the image point of that object point. This is illustrated in Figure 27 for the ith image and object points.

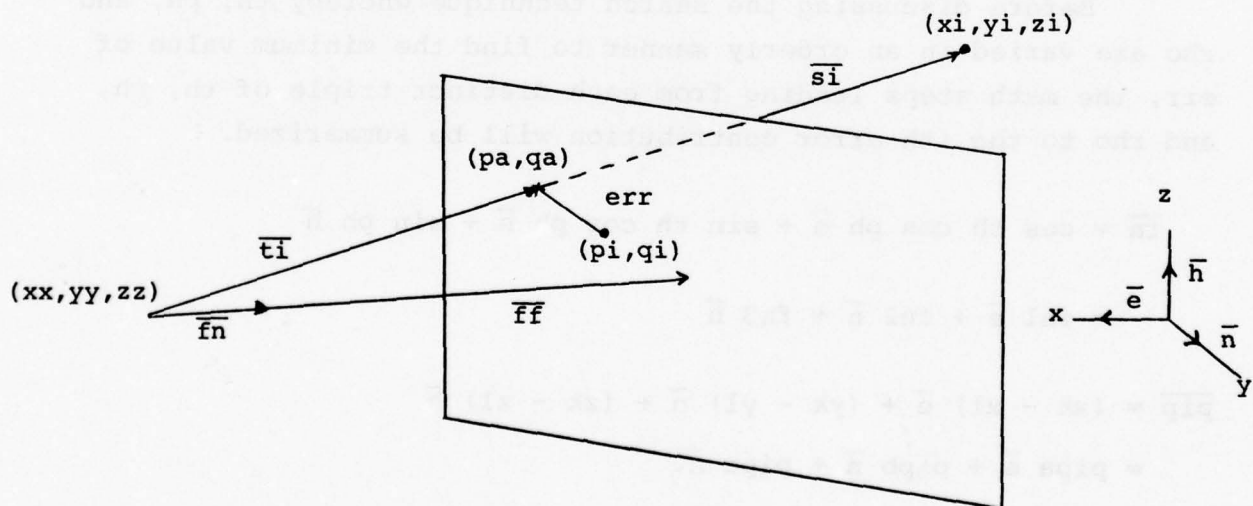


Figure 27.

Let  $(p_a, q_a)$  denote the film frame coordinates of the  $i$ th pierce point and  $erri$  be the distance between  $(p_a$  and  $q_a)$  and the  $i$ th image point at  $(p_i, q_i)$ .

$$\text{Then } erri = [(p_i - p_a)^2 + (q_i - q_a)^2]^{1/2}$$

and

$$err = \sum_{i=1}^n erri.$$

Any change in any of the three angles  $th$ ,  $ph$ , or  $\rho$  gives a new set of unit vectors  $\bar{f}_n$ ,  $\bar{i}$ ,  $\bar{j}$  and causes the coordinates of the  $i$ th pierce point  $(p_a, q_a)$  to change. That combination of  $th$ ,  $ph$  and  $\rho$  which results in the minimum value of  $err$  is considered to be the best fit. Of course, other definitions of  $err$  are possible, the most obvious being to define  $err$  as the sum of the squares of the miss distances rather than as their sum, but it was felt that this would allow one badly read image point or badly surveyed object point to have an unduly high distorting influence on the solution.

Before discussing the search technique whereby  $th$ ,  $ph$ , and  $\rho$  are varied in an orderly manner to find the minimum value of  $err$ , the math steps leading from each distinct triple of  $th$ ,  $ph$ , and  $\rho$  to the  $i$ th error contribution will be summarized.

$$\bar{f}_n = \cos th \cos ph \bar{e} + \sin th \cos ph \bar{n} + \sin ph \bar{h}$$

$$= fn1 \bar{e} + fn2 \bar{n} + fn3 \bar{h}$$

$$\bar{p}ip = (x_k - x_l) \bar{e} + (y_k - y_l) \bar{n} + (z_k - z_l) \bar{h}$$

$$= pip_a \bar{e} + pip_b \bar{n} + pip_c \bar{h}.$$

(Refer to Figure 25 and its discussion.)

$$a = \overline{p_i p} \cdot \overline{f_n} = p_{ipa} f_{n1} + p_{ipb} f_{n2} + p_{ipc} f_{n3}$$

$$\overline{p_i} = \overline{p_i p} - a \overline{f_n}$$

$$= (p_{ipa} - a f_{n1}) \overline{e} + (p_{ipb} - a f_{n2}) \overline{n} + (p_{ipc} - a f_{n3}) \overline{h}$$

$$= p_{ia} \overline{e} + p_{ib} \overline{n} + p_{ic} \overline{h}$$

$$p_{id} = \sqrt{\overline{p_i}} = (p_{ia}^2 + p_{ib}^2 + p_{ic}^2)^{1/2}$$

$$\overline{i^T} = \frac{\overline{p_i}}{\sqrt{\overline{p_i}}} = \frac{p_{ia}}{p_{id}} \overline{e} + \frac{p_{ib}}{p_{id}} \overline{n} + \frac{p_{ic}}{p_{id}} \overline{h}$$

=  $p_{ia} \overline{e} + p_{ib} \overline{n} + p_{ic} \overline{h}$  (Redefining  $p_{ia}$ ,  $p_{ib}$ ,  $p_{ic}$  to be components of the unit vector  $\overline{i^T}$ .)

$$\overline{j^T} = \overline{f_n} \times \overline{i^T}$$

$$= (f_{n2} p_{ic} - f_{n3} p_{ib}) \overline{e} + (f_{n3} p_{ia} - f_{n1} p_{ic}) \overline{n}$$

$$+ (f_{n1} p_{ib} - f_{n2} p_{ia}) \overline{h}$$

$$= p_{ja} \overline{e} + p_{jb} \overline{n} + p_{jc} \overline{h}.$$

From the discussion following Figure 26,

$$\overline{i} = \cos \rho \overline{i^T} + \sin \rho \overline{j^T}.$$

Inserting the equation  $\overline{i^T}$  and  $\overline{j^T}$  and grouping  $\overline{e}$ ,  $\overline{n}$ , and  $\overline{h}$

$$\overline{i} = (p_{ia} \cos \rho + p_{ja} \sin \rho) \overline{e} + (p_{ib} \cos \rho + p_{jb} \sin \rho) \overline{n}$$

$$+ (p_{ic} \cos \rho + p_{jc} \sin \rho) \overline{h}$$

$$= t_{ia} \overline{e} + t_{ib} \overline{n} + t_{ic} \overline{h}.$$

Similarly,  $\overline{j} = -\sin \rho \overline{i^T} + \cos \rho \overline{j^T}$

$$= (-p_{ia} \sin \rho + p_{ja} \cos \rho) \overline{e} + (-p_{ib} \sin \rho + p_{jb} \cos \rho) \overline{n}$$

$$+ (-p_{ic} \sin \rho + p_{jc} \cos \rho) \overline{h}$$

$$= t_{ja} \overline{e} + t_{jb} \overline{n} + t_{jc} \overline{h}$$



Referring now to Figure 27,

$\overline{ti}$  is the vector locating the pierce point ( $p_a, q_a$ ) due to the  $i$ th object point.  $\overline{ti}$  is a scalar multiple of  $\overline{si}$   $\overline{ti} = w \overline{si}$  where  $w$  is unknown.

The projection of  $\overline{ti}$  on  $\overline{fn}$  must equal the focal length  $ff$ .

$$\overline{ti} \cdot \overline{fn} = ff$$

or

$$w \overline{si} \cdot \overline{fn} = ff.$$

So

$$w = \frac{ff}{\overline{si} \cdot \overline{fn}}.$$

In component form

$$\overline{si} = (x_i - x_x) \overline{e} + (y_i - y_y) \overline{n} + (z_i - z_z) \overline{h}$$

and

$$w = \frac{ff}{(x_i - x_x) fn_1 + (y_i - y_y) fn_2 + (z_i - z_z) fn_3}.$$

A vector  $\overline{r}$  from the center of the film frame to the pierce point is gotten from the equation

$$\overline{r} = \overline{ti} - ff \overline{fn}.$$

See Figure 28.

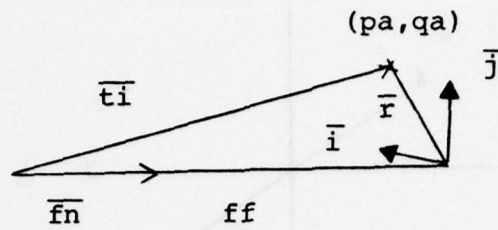


Figure 28.

In component form:

$$\begin{aligned}\bar{r} &= (w (xi - xx) - ff fn1)\bar{e} + (w (yi - yy) - ff fn2)\bar{n} \\ &+ (w (zi - zz) - ff fn3)\bar{h} \\ &= ra \bar{e} + rb \bar{n} + rc \bar{h}.\end{aligned}$$

Now since  $\bar{r}$  lies entirely in the film plane, it may be represented in terms of  $\bar{i}$  and  $\bar{j}$  components as follows:

$$\begin{aligned}\bar{r} &= \bar{r} \cdot \bar{i} \bar{i} + \bar{r} \cdot \bar{j} \bar{j} \\ &= pa \bar{i} + qa \bar{j}.\end{aligned}$$

Explicitly,

$$pa = \bar{r} \cdot \bar{i} = ra tia + rb tib + rc tic$$

$$qa = \bar{r} \cdot \bar{j} = ra tja + rb tjb + rc tjc$$

Let  $\bar{ri} = pi \bar{i} + qi \bar{j}$

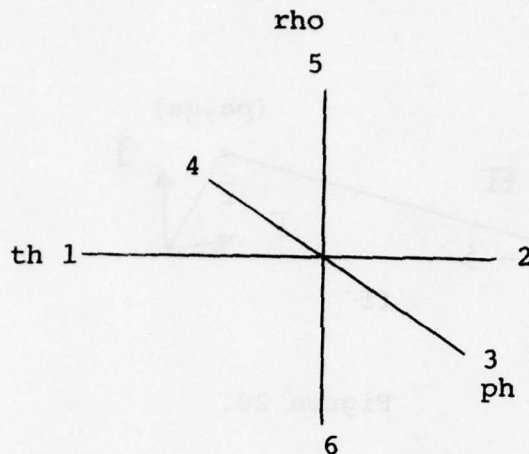


Figure 29.

Then

$$\begin{aligned} \text{erri} &= \sqrt{r_i} - \bar{r} / \\ &= [(p_i - p_a)^2 + (q_i - q_a)^2]^{1/2}. \end{aligned}$$

Then

$$\text{err} = \sum_{i=1}^m \text{erri}.$$

The scheme whereby th, ph, and rho are varied to minimize err is indicated in Figure 29.

The points numbered 1 through 6 indicate the order in which th, ph, and rho are varied. If point 1 (indicating a positive increment added to the present value of th) gives a lower err than exists at the origin, then successive increments are added to th so long as the value of err continues to fall. Points 1, 3, and 5 correspond to increases in th, ph, and rho respectively and 2, 4, and 6 to decreases. Although the axes in Figure 24 serve merely to indicate the order of variation, the procedure is precisely the same as that used to minimize err (fr, xx, ys, zs).

See Figure 18.

When  $\text{err}(\text{th}, \text{ph}, \text{rho})$  has been minimized, the final values of  $\bar{f}_n$ ,  $\bar{i}$ , and  $\bar{j}$  are computed. Also computed are the azimuth and elevation of the vector  $\bar{i}$ ,  $\text{thi}$ , and  $\text{phi}$  respectively.

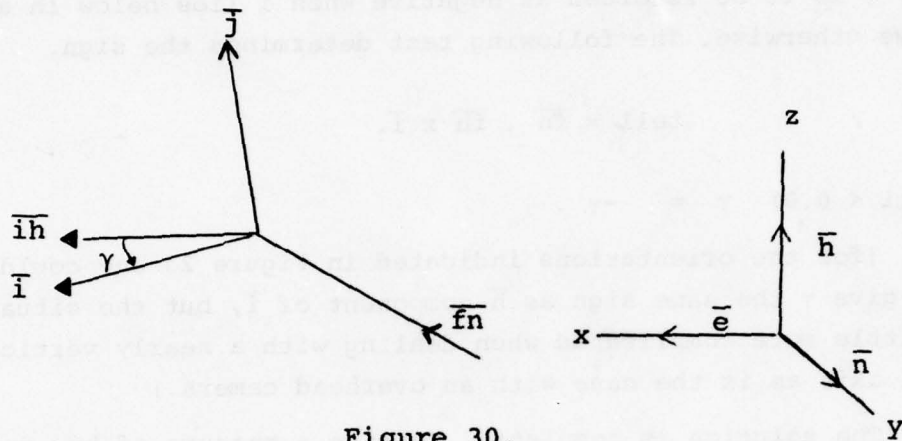


Figure 30.

At this point the camera has been located, oriented, and its focal length determined. The only one of the seven unknowns not yet solved for is the tilt angle,  $\gamma$ , of the camera from the horizontal about its optical axis. Knowing the azimuth  $\text{thi}$  and the elevation  $\text{phi}$  of the unit vector  $\bar{i}$  makes  $(\gamma)$  redundant, but it is among the output of the program, so its derivation will be given.

See Figure 30.

$\bar{i}h$  is a unit vector in the film frame which is parallel to the  $x y$  plane (i.e., horizontal) of the main coordinate system.

$$\bar{i}h = \frac{\bar{h} \times \bar{f}_n}{|\bar{h} \times \bar{f}_n|}$$

By definition of the cross product  $\bar{i}h$  is normal to both  $\bar{f}_n$  and  $\bar{h}$ . Therefore, it both lies in the film frame and is parallel to the  $xy$  plane. It is obviously a unit vector.



$$\gamma = \cos^{-1} (\bar{ih} \cdot \bar{h})$$

$\gamma$  is to be recorded as negative when  $\bar{I}$  lies below  $\bar{ih}$  and positive otherwise. The following test determines the sign.

$$\text{tell} = \bar{fn} \cdot \bar{ih} \times \bar{I}.$$

If ( $\text{tell} < 0.0$ )  $\gamma = -\gamma$ .

(for the orientations indicated in Figure 25 one could simply give  $\gamma$  the same sign as  $\bar{h}$  component of  $\bar{I}$ , but the situation is a little more complicated when dealing with a nearly vertical optical axis as is the case with an overhead camera.)

The solution is complete. To give a measure of how good the whole situation is, the following check was devised. See Figure 31.

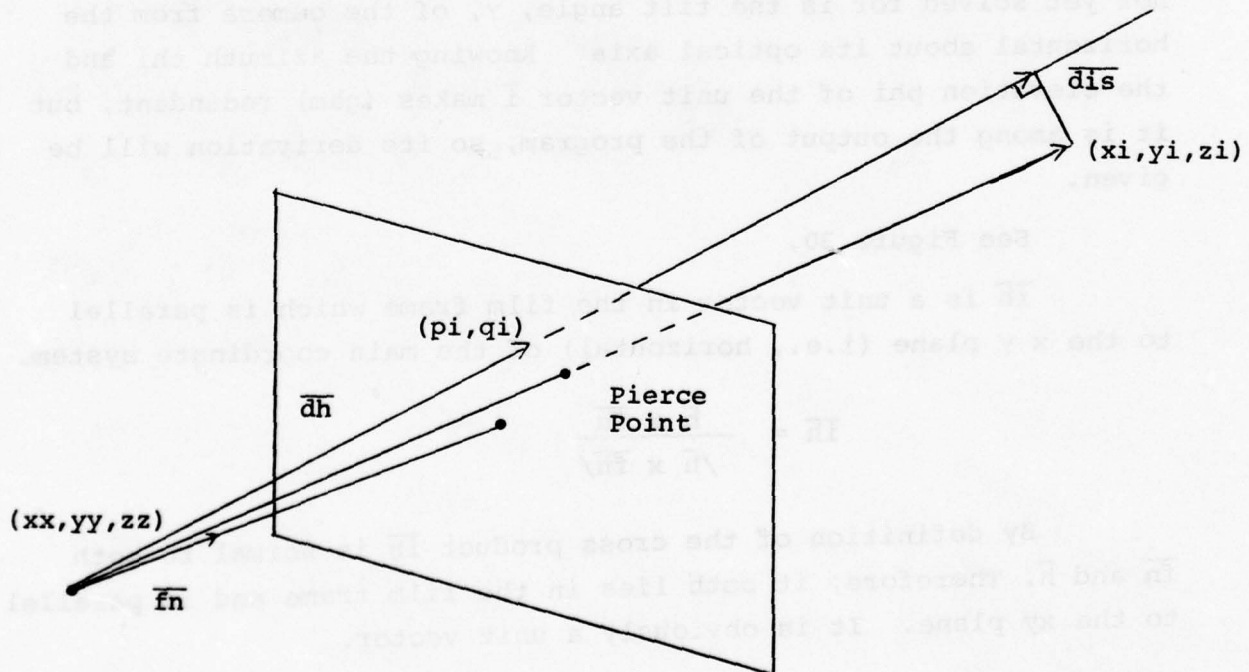


Figure 31.

A ray is extended from the camera focal point through each image point  $(p_i, q_i)$  past its corresponding object point and the distance vector  $\overline{dis}$  of the ray's nearest approach to the object point is computed. If all distances  $\overline{dis}$  so computed are of small magnitude, the fit is obviously good.

$$\begin{aligned}\overline{dh} &= ff \overline{fn} + p_i \overline{i} + q_i \overline{j} \\ &= dha \overline{e} + dhn \overline{n} + dhc \overline{h}\end{aligned}$$

where the final form is obtained by expressing  $\overline{fn}$ ,  $\overline{i}$ , and  $\overline{j}$  in terms of their components in the principal coordinate system and then grouping on the principal coordinate system unit vectors  $\overline{e}$ ,  $\overline{n}$ , and  $\overline{h}$ .

$$\begin{aligned}\overline{sh} &= (x_i - x_x) \overline{e} + (y_i - y_y) \overline{n} + (z_i - z_z) \overline{h} \\ &= sha \overline{e} + shb \overline{n} + shc \overline{h}\end{aligned}$$

$$dh = \frac{\overline{dh}}{|\overline{dh}|} \quad (\text{a unit vector in the direction of the}$$

$i$ th image point  $(p_i, q_i)$ .)

There is a scalar coefficient,  $acof$ , such that

$$acof \overline{dh} = \overline{sh} + \overline{dis}.$$

Dotting through by  $\overline{dh}$

$$acof \overline{dh} \cdot \overline{dh} = \overline{sh} \cdot \overline{dh} + \overline{dis} \cdot \overline{dh}$$

$$= \overline{sh} \cdot \overline{dh} \quad (\text{since } \overline{dis} \text{ is perpendicular to } \overline{dh})$$

$$acof = \overline{sh} \cdot \overline{dh} \text{ since } \overline{dh} \cdot \overline{dh} = 1.$$

So,  $\overline{dis} = acof \overline{dh} - \overline{sh}$  and the miss distance is  $dis$  where  $dis = |\overline{dis}|$ .

These miss distances have characteristically fallen into a range of 0.05-inches to 0.22-inches in the solutions run thus far. Good agreement in this check indicates not only that the camera data found is correct, but also that the survey of the object points and the reading of the image points were probably both quite accurate. In closing the discussion of the mathematics used, it should be mentioned that one or two grossly inaccurate image or object point locations can completely swamp out the relative minimum indicated in Figure 15.

### 3.1.2 Program POOCH

A brief discussion of the overall program operation will be given before going into input and output in detail. A reduced-size-copy of the program is included in Appendix E. Figure 32 contains a block diagram of the program.

The main program POOCH reads in and scales the data. Subroutine FIND together with its auxiliary subroutines, HORSY, REFIN, and ANGLE, computes the correct values of focal point position (xx, yy, zz) and focal length ff. FIND calls HORSY twice to locate points P and Q (shown in Figures 14 and 17). HORSY performs the 27 point cube search displayed in Figure 16. Subroutine ANGLE computes the value of err for any focal length fs and focal point location (sx, ys, zs). After points P and Q (see Figures 14 and 17) have been found, FIND uses subroutine REFIN to find the best values of focal length ff and focal point location (xx, yy, zz). REFIN performs the six point search illustrated in Figure 29. Both HORSY and REFIN use ANGLE to compute err (fx, xs, ys, zs).

Program POOCH then calls subroutine SERCH which provides approximate values of the camera orientation variables th, ph, and rho. Finally, subroutine DANG is called to optimize the approximate camera orientation produced by SERCH. DANG's auxiliary subroutine WRANG computes an error value which is the sum of the distances of all pierce points from their corresponding image points.

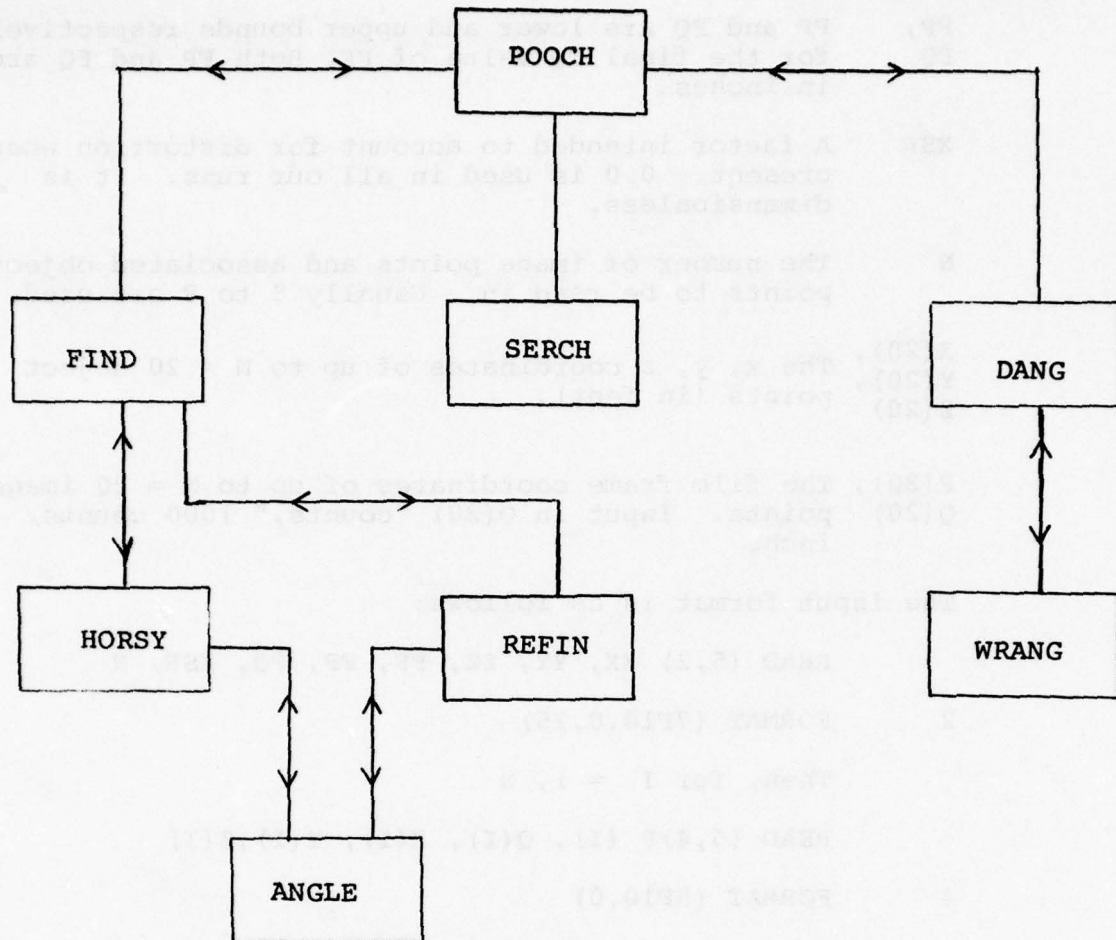


Figure 32. Block Diagram of Program POOCH.

See Figures 27 and 28 and the associated discussion.

The following list contains the variables which must be input to the program:

- |    |   |
|----|---|
| XX | The x, y, and z coordinates of the estimated camera position.   |
| YY | Input in feet.  |
| ZZ |   |
| FF | The nominal focal length of the camera in inches times the magnification of the film frame reader used. |



FP, FP and FQ are lower and upper bounds respectively  
FQ for the final FQ value of FF. Both FP and FQ are  
in inches.

XSR A factor intended to account for distortion when  
present. 0.0 is used in all our runs. It is  
dimensionless.

N The number of image points and associated object  
points to be read in. Usually 5 to 8 are used.

X(20), The x, y, z coordinates of up to N = 20 object  
Y(20), points (in feet).  
Z(20)

P(20), The film frame coordinates of up to N = 20 image  
Q(20) points. Input in Q(20) "counts," 1000 counts/  
inch.

The input format is as follows:

READ (5,2) XX, YY, ZZ, FF, FP, FQ, XSR, N

2 FORMAT (7F10.0,I5)

Then, for I = 1, N

READ (5,4) P (I), Q(I), X(I), Y(I), Z(I)

4 FØRMAT (5F10.0)

Where each image point P(I), Q(I) is on the same  
card as its associated object point X(I), Y(I),  
Z(I).

Multiple cases may be read into the program. Figure 33  
shows a sample data deck for a case run.

There is at present a great deal of working output taken  
from the program but most of it was used for debug purposes and  
is of little consequence now and can be eliminated. Rather  
than waste many pages describing this debug output, that part  
of the output giving the camera location and orientation and  
the various checks on the goodness of the solution will be  
discussed.



The first three lines of the tab section contain the check values for the first image point. The first pair of values after the image point number are the p and q coordinates of the first film frame image point in feet. The second pair of values are the p and q coordinates of the pierce point due to object point 1, that is, the p and q coordinates of the point of the film that would be pierced by a ray from the camera focal point to the first (refer to Figure 31) object point. The last value is the distance in feet between the image point and the pierce point. It must, of course, be remembered as explained previously, that the magnification of the film frame reader enlarges the actual film frame size by about a factor of 20. However, these distances may be usefully compared both with one another in a single run, and also between runs to see if reasonable results are being obtained. To determine how far apart the image point and its associated pierce point are on the real film frame, the distance given could be divided by about 20.4, the approximate magnification of the reader used.

The last line of output for the first image and object points gives the object point number, then the x, y, and z coordinates in feet of the object point. The fifth, sixth, and seventh values are the x, y, and z components, respectively, of the miss vector  $\overline{dis}$  described in Figure 31 and the text pertaining thereto. Its components are given in feet. The last value is the magnitude of  $\overline{dis}$  in feet. This is the most important value for judging how good the solution is. The numbers written into the right of these values are the magnitude of  $\overline{dis}$  in inches, and as can be seen, are quite reasonable. This assures that not only did the program provide a good solution, but also that the object points were correctly surveyed and their film frame images were correctly read. In short, when the magnitudes of  $\overline{dis}$  are small for each object point, it provides a comprehensive check on the entire data reduction scheme.



In the run illustrated, there were seven points available on which to base the solution. Immediately after the listing of the above data for the last of these points, the camera solution data is output. In the line beginning X, Y, Z, F ... the first three numerical values are the x, y, and z coordinates of the location of the camera focal point (in feet). The fourth value is the fictitious program focal length, i.e., it is the product of the true camera focal length and the film reader magnification and is given in feet. The fifth and sixth values are the azimuth and elevation angles of the camera optical axis, both given in radians. The last value in this line of output is the angle that has been referred to us as rho. It is of no consequence after the camera solution has been generated.

The line beginning DAMG,... gives the azimuth and elevation angles of the film frame  $\bar{I}$  axis and the tilt angle of the camera from horizontal about the optical axis in that order. All angles are in radians.

It yet remains to explain a minor point regarding coordinate systems. The experimental coordinate system is a left hand system. See Figure 35.

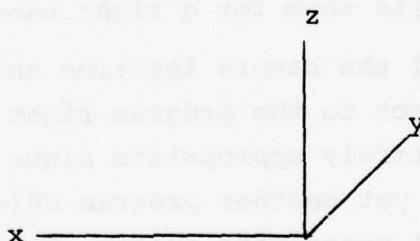


Figure 35.



The input coordinates of all object points ( $x_i, y_i, z_i$ ) and the estimated initial camera position ( $xx, yy, zz$ ) are input with respect to this coordinate system. The program changes the sign of the  $y$  coordinate of each of these points so that they are properly represented for the right hand coordinate system used in the program. See Figure 36.

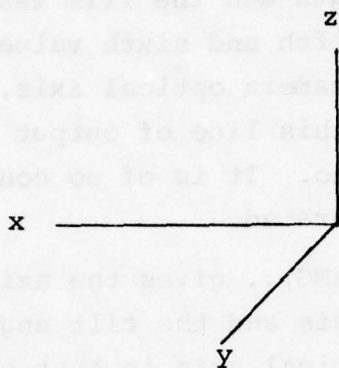


Figure 36.

This change was made so that it would not be necessary to define the components of every vector cross product used for a left hand coordinate system when it is second nature to most to automatically write them for a right handed system.

Moreover all the camera location and orientation data is output with respect to the program right hand coordinate system. This is entirely appropriate since the camera solution is used as input to yet another program which also contains a right hand principal coordinate system. Similarly, the coordinates of the object points are also output with respect to the program right hand system rather than with respect to the original experimental left hand system.

The film frame reader has a coordinate system as indicated in Figure 37 with the horizontal axis positive to the right.

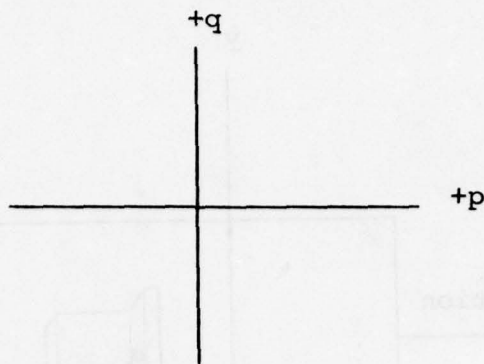


Figure 37.

In order that the unit vectors  $\bar{f}_n$ ,  $\bar{i}$ ,  $\bar{j}$  (refer to Figure 12) in that order form a right hand system, the sign of the horizontal coordinate of each image point is changed. Moreover the film frame coordinates are output with the signs of their horizontal coordinates still reversed.

There is nothing very involved about these sign changes, but one should be aware of what has been done if he attempts to use the program. These sign changes are clearer from the tab of program POOCH than from all the explanation above, and could be easily changed to suit if one were going to use the program for an experiment in which the experimental coordinate system itself were right handed.

### 3.2 TWO-RAY SOLUTIONS OF COORDINATES OF POINTS

The Camera Location Program has direct application in Program Sled which performs the reduction of data taken during seat harness tests. A dummy and an animal, or two dummies, are strapped into seats mounted aboard an acceleration sled. Also rigidly mounted aboard the sled are two high-speed cameras which photograph the reactions of the test subjects as the sled accelerates down its track in the  $+x$  direction. See Figure 38.

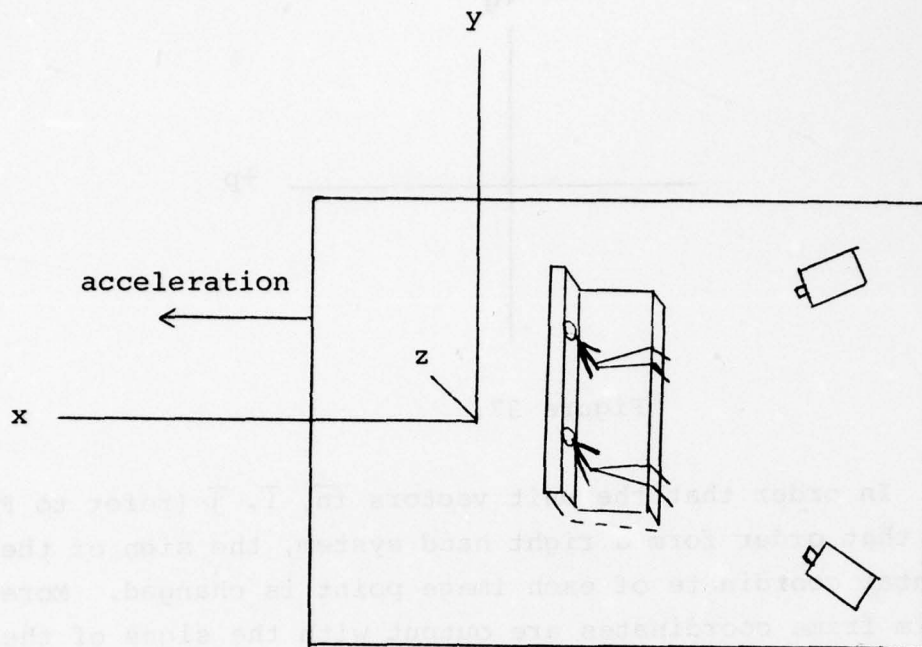


Figure 38.

The experimental coordinate system is a left-hand  $x y z$  system affixed to the moving sled. All subject motion recorded is understood to be relative to the sled. In cases run so far, two targets (plastic disks marked so as to be easily discerned on the film frame reader) are attached to each test subject. For a dummy, the forehead and chin have been targeted. When the subject was an animal, head accelerometer pack and tip of the snout were chosen as target points. The whole purpose of program Sled is to provide displacement versus time graphs of each of the targeted points on each of the test subjects.

The camera location program is used first to accurately locate and orient each of the two cameras. The coordinates of a number of points rigidly affixed to the sled are accurately measured. Their film frame image coordinates are determined for each camera. The camera location and orientation data obtained from the camera location program is then input to the Sled program.

The principal coordinate system in the Sled program is a right hand x y z system, not the experimental left-hand system indicated in Figure 38. This change is accomplished simply by changing the sign of the y coordinate of every point after it has been input to Sled. Also, so that the camera system axes will constitute a right-hand coordinate system, the horizontal film frame coordinate is reversed in sign. Unit vectors  $\bar{e}$ ,  $\bar{n}$ , and  $\bar{h}$  are directed along the x, y, z axes respectively. See Figure 39. The x, y, and z axes are mutually perpendicular.

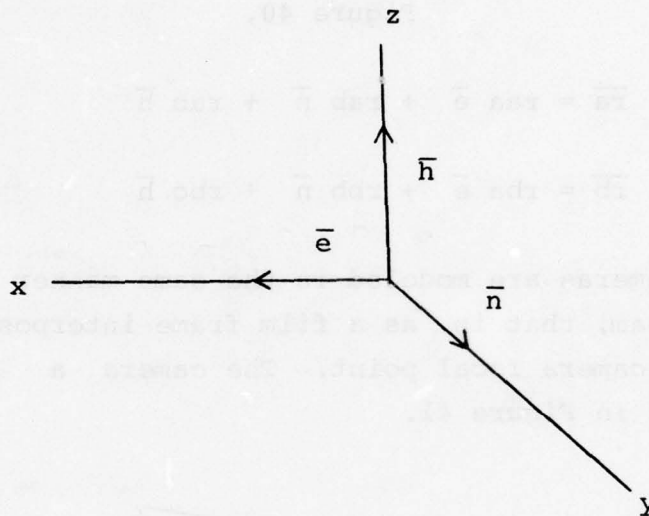


Figure 39.

The two cameras are designated camera a and camera b and their focal points are located by vectors  $\bar{ra}$  and  $\bar{rb}$  respectively. See Figure 40.



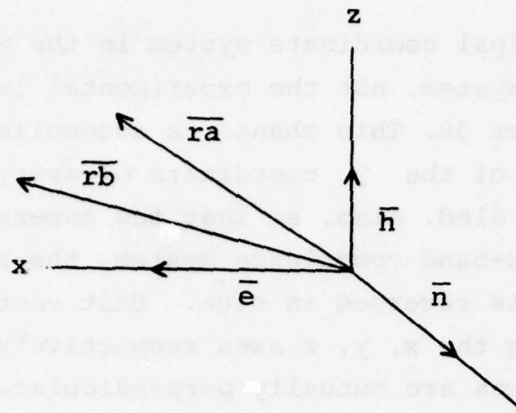


Figure 40.

$$\overline{ra} = r_{aa} \overline{e} + r_{ab} \overline{n} + r_{ac} \overline{h}$$

$$\overline{rb} = r_{ba} \overline{e} + r_{bb} \overline{n} + r_{bc} \overline{h}$$

The cameras are modeled in the same manner as in the camera location program, that is, as a film frame interposed between the scene and the camera focal point. The camera a coordinate system is illustrated in Figure 41.

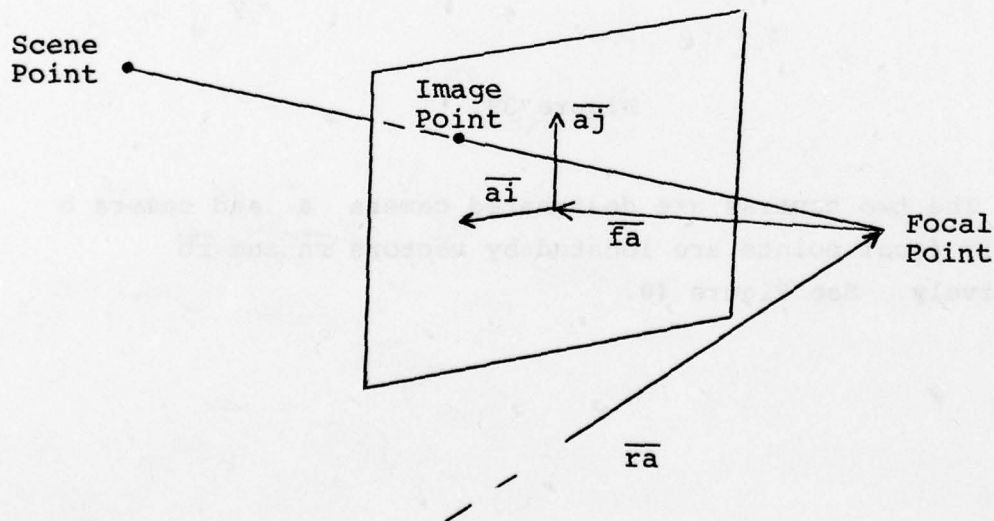


Figure 41.

$\bar{f}_a$  lies along the camera optical axis and is perpendicular to the horizontal and vertical film frame unit vectors  $\bar{a}_i$  and  $\bar{a}_j$ . The magnitude of  $\bar{f}_a$  is  $f_a$ , the camera a focal length. (As in the camera location program,  $\bar{f}_a$  is actually the product of the true camera focal length and the film reader magnification. The analogous vectors for camera b are  $\bar{b}_i$ ,  $\bar{b}_j$ ,  $\bar{f}_b$ .

The data that must be supplied to completely define camera a consists of the three components of its position vector,  $r_{aa}$ ,  $r_{ab}$ ,  $r_{ac}$ , the azimuth, elevation, and magnitude of  $\bar{f}_a$  which are  $\theta_{aa}$ ,  $\phi_{aa}$ ,  $f_a$ , the azimuth and elevation of  $\bar{a}_i$  which are  $\theta_{ia}$ ,  $\phi_{ia}$ . For camera b the analogous quantities are in the same order:  $r_{ba}$ ,  $r_{bb}$ ,  $r_{bc}$ ,  $f_b$ ,  $\theta_{ib}$ ,  $\phi_{ib}$ ,  $\theta_{ib}$ ,  $\phi_{ib}$ .

We will now discuss the principal parts of the analysis in the various subroutines. The first topic will be the derivation of the  $\alpha$  camera ray solution. See Figure 42.

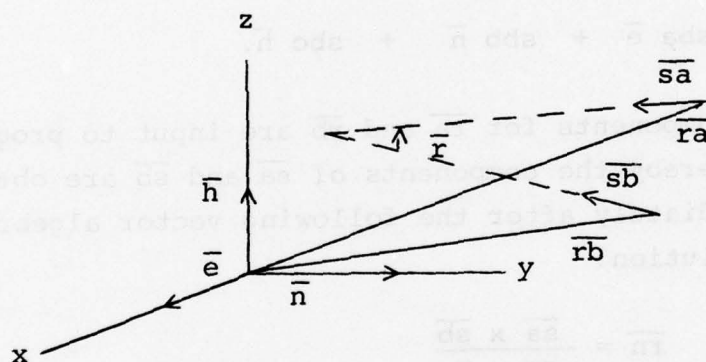


Figure 42.

$\bar{r}_a$  and  $\bar{r}_b$  are the position vectors locating cameras a and b respectively.  $\bar{s}_a$  and  $\bar{s}_b$  are unit vectors along the ray direction from the camera focal point toward the film frame image of one of the moving points on a dummy, a point whose position is to be determined with respect to the x, y, z coordinate

system. Due to film frame reading errors, camera location and orientation errors, and also to the interpolation used to find  $\overline{sa}$  and  $\overline{sb}$  at the same instant in time, the rays will not in general intersect, but will miss each other by a small distance denoted by the vector  $\overline{r}$ .  $\overline{r}$  is necessarily perpendicular to both rays.

The position of the moving point on the dummy is assumed to lie at the midpoint of  $\overline{r}$ .  $\overline{ra}$ ,  $\overline{rb}$ ,  $\overline{sa}$ , and  $\overline{sb}$  are known completely. Although the vector algebra solution below does not explicitly use the names of the components of these vectors, we will list them for completeness sake:

$$\overline{ra} = r_{aa} \overline{e} + r_{ab} \overline{n} + r_{ac} \overline{h}$$

$$\overline{rb} = r_{ba} \overline{e} + r_{bb} \overline{n} + r_{bc} \overline{h}$$

$$\overline{sa} = s_{aa} \overline{e} + s_{ab} \overline{n} + s_{ac} \overline{h}$$

$$\overline{sb} = s_{ba} \overline{e} + s_{bb} \overline{n} + s_{bc} \overline{h}.$$

The components for  $\overline{ra}$  and  $\overline{rb}$  are input to program SLED. The method whereby the components of  $\overline{sa}$  and  $\overline{sb}$  are obtained is taken up immediately after the following vector algebra two ray solution. Solution:

$$\overline{rn} = \frac{\overline{sa} \times \overline{sb}}{|\overline{sa} \times \overline{sb}|}$$

is a unit vector collinear with  $\overline{r}$ , that is,  $\overline{r}$  is perpendicular to both  $\overline{sa}$  and  $\overline{sb}$ .

Let  $\overline{r} = d \overline{rn}$  where  $d$  is the as-yet-unknown-scalar multiple of  $\overline{rn}$  which yields  $\overline{r}$ . ( $d$  will be negative if the  $\overline{sb}$  ray passes over the  $\overline{sa}$  ray in a particular case.)

(1)  $\overline{ra} + \text{coa } \overline{sa} = \overline{rb} + \text{cob } \overline{sb} + \overline{r}$  where coa and cob are scale factors to be solved for.

Substituting for  $\overline{r}$  gives

$$(2) \quad \overline{ra} + \text{coa } \overline{sa} = \overline{rb} + \text{cob } \overline{sb} + d \overline{rn}.$$

Dotting through by  $\overline{rn}$  gives

$$\overline{ra} \cdot \overline{rn} + \text{coa } \overline{sa} \cdot \overline{rn} = \overline{rb} \cdot \overline{rn} + \text{cob } \overline{sb} \cdot \overline{rn} + d \overline{rn} \cdot \overline{rn}$$

$$\overline{ra} \cdot \overline{rn} - \overline{rb} \cdot \overline{rn} = d.$$

$$(3) \quad \text{or } d = (\overline{ra} - \overline{rb}) \cdot \overline{rn}$$

Rewriting (2) in an altered form gives:

$$(4) \quad \text{coa } \overline{sa} - \text{cob } \overline{sb} = \overline{rb} - \overline{ra} + d \overline{rn}.$$

Dotting through (4) by  $\overline{sa}$  gives:

$$\text{coa} - \text{cob } \overline{sb} \cdot \overline{sa} = (\overline{rb} - \overline{ra}) \cdot \overline{sa}$$

or 
$$(5) \quad \text{coa} = (\overline{rb} - \overline{ra}) \cdot \overline{sa} + \text{cob } \overline{sa} \cdot \overline{sb}$$

Dotting through (4) by  $\overline{sb}$  gives:

$$(6) \quad \text{coa } \overline{sa} \cdot \overline{sb} - \text{cob} = (\overline{rb} - \overline{ra}) \cdot \overline{sb}.$$

Substituting (5) for coa in (6) gives

$$[(\overline{rb} - \overline{ra}) \cdot \overline{sa} + \text{cob } \overline{sa} \cdot \overline{sb}] \cdot \overline{sb} - \text{cob} = (\overline{rb} - \overline{ra}) \cdot \overline{sb}.$$

Solving for cob gives:



$$(7) \quad \text{cob} = \frac{(\overline{rb} - \overline{ra}) \cdot \overline{sa} \overline{sa} \cdot \overline{sb} - (\overline{rb} - \overline{ra}) \cdot \overline{sb}}{1 - (\overline{sa} \cdot \overline{sb})^2}$$

Substituting the value of cob into (5) gives coa.

A vector  $\overline{sol}$  locating the solution point (midpoint of  $\overline{r}$ ) can be computed by either of two equivalent vector sums.

$$\overline{sol} = \overline{rb} + \text{cob} \overline{sb} + 0.5 \overline{r} \quad (\text{see Figure 9})$$

$$\text{or} \quad \overline{sol} = \overline{ra} + \text{coa} \overline{sa} = 0.5 \overline{r}.$$

The ray miss distance dis is gotten from  $\text{dis} = /d/$ . d in the equation below

$$\overline{r} = d \overline{rn}$$

will be negative if  $\overline{rn}$  should have a direction or sense opposite to  $\overline{r}$ . Its sign depends on the order in which the cameras were read in and which ray is uppermost.

The above solution is performed in subroutine SOLVE. In order that the unit vectors  $\overline{sa}$  and  $\overline{sb}$  have their components computed with respect to the main coordinate system, the components of each camera coordinate system vector must be known with respect to the main coordinate system. Let (pa, qa) be the film frame coordinates of camera a, fa, its focal length, tha and pha the azimuth and elevation of its optical axis, thia and phia the azimuth and elevation of the camera a  $\overline{sa}$  film frame unit vector. See Figure 43.

Now  $\overline{ra} = \text{raa} \overline{e} + \text{rab} \overline{n} + \text{rac} \overline{h}$  is known, its components being read in.

$$\begin{aligned} \overline{fa} &= f_a \cos \text{tha} \cos \text{pha} \overline{e} + f_a \sin \text{tha} \cos \text{pha} \overline{n} \\ &+ \overline{fa} \sin \text{pha} \overline{h} = f_{aa} \overline{e} + f_{ab} \overline{n} + f_{ac} \overline{h} \end{aligned}$$

$$\begin{aligned} a_i &= \cos \text{thia} \cos \text{phia} \overline{e} + \sin \text{thia} \cos \text{phia} \overline{n} \\ &+ \sin \text{phia} \overline{h} = a_{ia} \overline{e} + a_{ib} \overline{n} + a_{ic} \overline{h} \end{aligned}$$

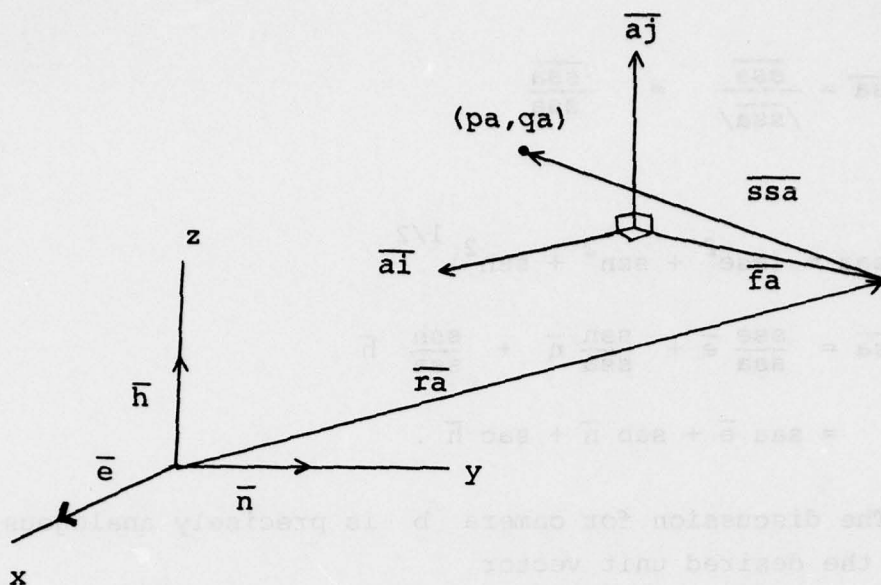


Figure 43.

$$\begin{aligned}
 \overline{a_j} &= \frac{\overline{f_a} \times \overline{a_i}}{f_a} \\
 &= \frac{f_{ab} a_{ic} - f_{ac} a_{ib}}{f_a} \overline{e} + \frac{f_{ac} a_{ia} - f_{aa} a_{ic} \overline{n}}{f_a} \\
 &\quad + \frac{f_{oa} a_{ib} - f_{ab} a_{ia}}{f_a} \overline{h} \\
 &= a_{jae} + a_{jb} \overline{n} + a_{jc} \overline{h} \\
 \overline{ssa} &= \overline{f_a} + p_a \overline{a_i} + q_a \overline{a_j} \\
 &= (f_{aa} + p_a a_{ia} + q_a a_{ja}) \overline{e} + (f_{ab} + p_a a_{ib} + q_a a_{jb}) \overline{n} \\
 &\quad + (f_{ac} + p_a a_{ic} + q_a a_{jc}) \overline{h} \\
 &= s_{se} \overline{e} + s_{sn} \overline{n} + s_{sh} \overline{h}.
 \end{aligned}$$

$\overline{ssa}$  is a vector from the camera a focal point to the film frame image point  $(p_a, q_a)$ . It has the same direction as the desired unit vector  $\overline{sa}$  but its magnitude is in general not 1. So,

$$\overline{sa} = \frac{\overline{ssa}}{|\overline{ssa}|} = \frac{\overline{ssa}}{ssa}$$

where

$$saa = (sse^2 + ssn^2 + ssh^2)^{1/2}$$

$$\begin{aligned}\overline{sa} &= \frac{sse}{ssa} \overline{e} + \frac{ssn}{ssa} \overline{n} + \frac{ssh}{ssa} \overline{h} \\ &= saa \overline{e} + sab \overline{n} + sac \overline{h} .\end{aligned}$$

The discussion for camera b is precisely analogous, yielding the desired unit vector

$$sb = sba \overline{e} + sbb \overline{n} + sbc \overline{h}.$$

In determining the solution point the unit vectors  $\overline{sa}$  and  $\overline{sb}$  in the ray directions must be known at the same instant. Since solutions are desired at equally spaced time points, a method of interpolating between two camera rays is needed.

Although there are timing flash marks on each roll of film which allow the time at which each frame was exposed to be determined very closely, the shutters of the two cameras are not synchronized. Moreover, the picture-taking rates of the two cameras are not quite equal.

Assume that we have two successive frames from either one of the cameras taken at times  $tas$  and  $tbs$  where  $tas < tbs$ . Let the film frame coordinates of the moving point's image be  $(ppa, qqa)$  at time  $tas$  and  $(ppb, qqb)$  at time  $tbs$ .

Figure 44 shows vectors  $\overline{a}$  and  $\overline{b}$  to the image points of the moving object point at times  $tas$  and  $tbs$  respectively. Now to get what would have been the ray direction to the moving point's image at time  $ts$  ( $tas < ts < tbs$ ), we assume that the ray turns with constant angular velocity through the angle  $th$  in time interval  $tbs - tas$ . That is, the angle  $th$ s turned through in time  $ts - tas$  is  $th_s = \frac{ts - tas}{tbs - tas} th$ . See Figure 45.

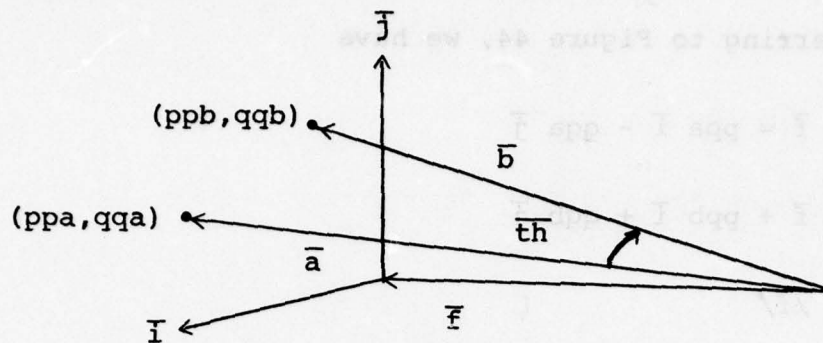


Figure 44.

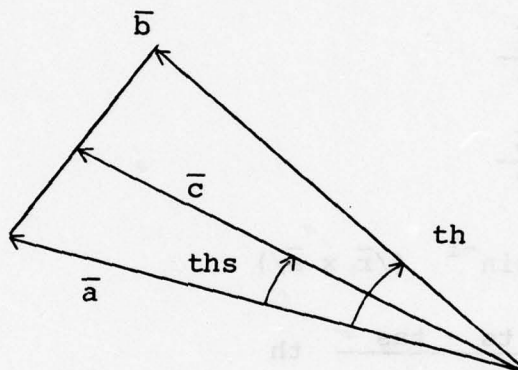


Figure 45.

Figure 45 shows vectors  $\bar{a}$ ,  $\bar{b}$ , and the angles  $th$  and  $ths$ . Vector  $\bar{c}$  is that vector which picks out on the film frame the image point position that would have occurred had a picture been taken at time  $ts$ . (The assumptions that the moving point remains in the plane of its rays  $\bar{a}$  and  $\bar{b}$  from time  $tas$  to time  $tbs$ , and that it moves in such a way that its angular velocity with respect to the camera focal point is constant are in general not exactly true, but if the film frame rate is high enough to faithfully record the experiment, they should be good assumptions. The simple error statistics on the program output seem to indicate the above is a good interpolation.)



Referring to Figure 44, we have

$$\bar{a} = \bar{f} = ppa \bar{i} - qqa \bar{j}$$

$$b = \bar{f} + ppb \bar{i} + qqb \bar{j}$$

$$f = |\bar{f}|$$

$$a = |\bar{a}| = (f^2 + ppa^2 + qqa^2)^{1/2}$$

$$b = |\bar{b}| = (f^2 + ppb^2 + qqb^2)^{1/2}$$

$$\bar{r} = \frac{\bar{a}}{a}$$

$$\bar{s} = \frac{\bar{b}}{b}$$

$$th = \sin^{-1} (|\bar{r} \times \bar{s}|)$$

$$ths = \frac{ts - tas}{tbs - tas} \quad th$$

$$tht = th - ths.$$

Let  $\bar{rs}$  be a unit vector in the direction of  $c$ . See Figure 46.

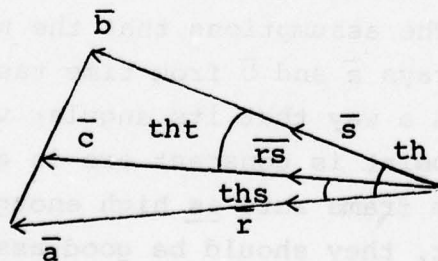


Figure 46.

So,

$$\overline{rs} = A \overline{r} + B \overline{s} \text{ where } A \text{ and } B \text{ must be found.}$$

Dotting through by  $\overline{r}$  gives:

$$\overline{r} \cdot \overline{rs} = A \overline{r} \cdot \overline{r} + B \overline{r} \cdot \overline{s}$$

or  $\cos ths = A + B \cos th.$

Dotting through by  $\overline{s}$  gives:

$$\overline{rs} \cdot \overline{s} = A \overline{r} \cdot \overline{s} + B \overline{s} \cdot \overline{s}$$

or  $\cos tht = A \cos th + B$

$$A = \frac{\begin{vmatrix} \cos ths & \cos th \\ \cos tht & 1 \\ 1 & \cos th \\ \cos th & 1 \end{vmatrix}}{\begin{vmatrix} 1 & \cos th \\ \cos th & 1 \end{vmatrix}}$$

$$= \frac{\cos (ths) - \cos th \cos tht}{1 - \cos^2 th}$$

$$= \frac{\cos (th - tht) - \cos th \cos tht}{\sin^2 th}$$

$$= \frac{\sin th \sin tht}{\sin^2 th}$$

$$A = \frac{\sin tht}{\sin th}$$

$$B = \frac{\begin{vmatrix} 1 & \cos ths \\ \cos th & \cos tht \end{vmatrix}}{\sin^2 th}$$

$$= \frac{\cos tht - \cos ths \cdot \cos th}{\sin^2 th}$$

$$B = \frac{\sin ths}{\sin th}.$$

So,

$$\overline{rs} = A \overline{r} + B \overline{s}$$

$$\overline{rs} = \frac{\sin tht}{\sin th} \overline{r} + \frac{\sin ths}{\sin th} \overline{s}$$

where  $\overline{rs}$  is a unit vector in the direction of the image of the moving point at time  $ts$ .

We need only scale  $\overline{rs}$  so that its tip just touches the film frame. See Figure 47.

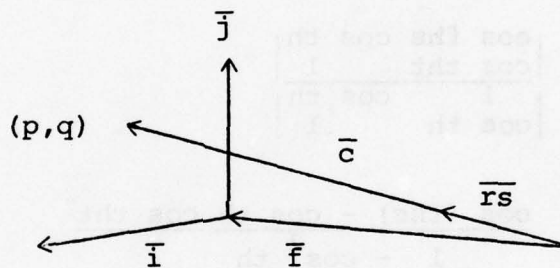


Figure 47.

The length of  $f$  is  $\overline{f}$ , i.e.,  $f = \overline{f}/$

$\overline{c} = xk \overline{rs}$  where  $xk$  must be found.

$xk \overline{rs} \cdot \frac{\overline{f}}{\overline{f}} = f$  (the component of  $\overline{c}$  in the direction of the camera optical axis must equal the focal length,  $f$ , of the camera.

So,

$$xk = \frac{f^2}{\overline{rs} \cdot \overline{f}}$$

and

$$\bar{c} = xk \bar{rs}.$$

The coordinates of the image point at time  $t_s$  are:

$$(p,q) \text{ where } p = \bar{c} \cdot \bar{i} \\ \text{and } q = \bar{c} \cdot \bar{j}.$$

This essentially concludes the discussion of the math modeling used in the program. The rest of the program is principally concerned with bookkeeping.

It is worth mentioning that the ray interpolation probably could have been done more economically. However, an additional complication with the runs is that some slight camera movement is experienced during periods of peak sled acceleration. It is very slight on the great majority of runs. There are, however, one or two runs in which camera vibration was rather severe. In order to deal with this problem, additional analysis (not reported in detail) has been done to allow frame-by-frame reorienting of the cameras. To insert this correction into the program would require a different ray interpolation routine.

The assumption of an absolutely rigid camera mounting appears to be justified in view of the data obtained so far. But reorienting of the cameras frame-by-frame might give some improvement. Also, taking the solutions from the program as it presently stands and actually going back and computing the angular accelerations of the moving points at each camera would provide an interesting check on the ray interpolation assumptions presently in the program. It might even allow a reinterpolation and a better final solution.

In short, there are a number of areas that remain to be investigated in this problem, perhaps with profit, perhaps not.



### 3.2.1 Program SLED

Program SLED uses four subroutines. Its block diagram appears in Figure 48.

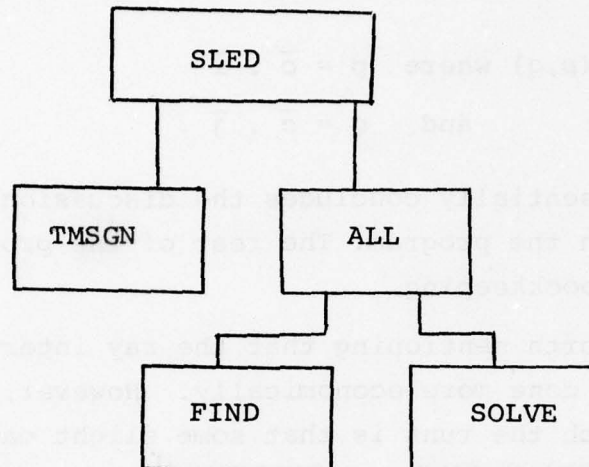


Figure 48. Block Diagram of Program SLED.

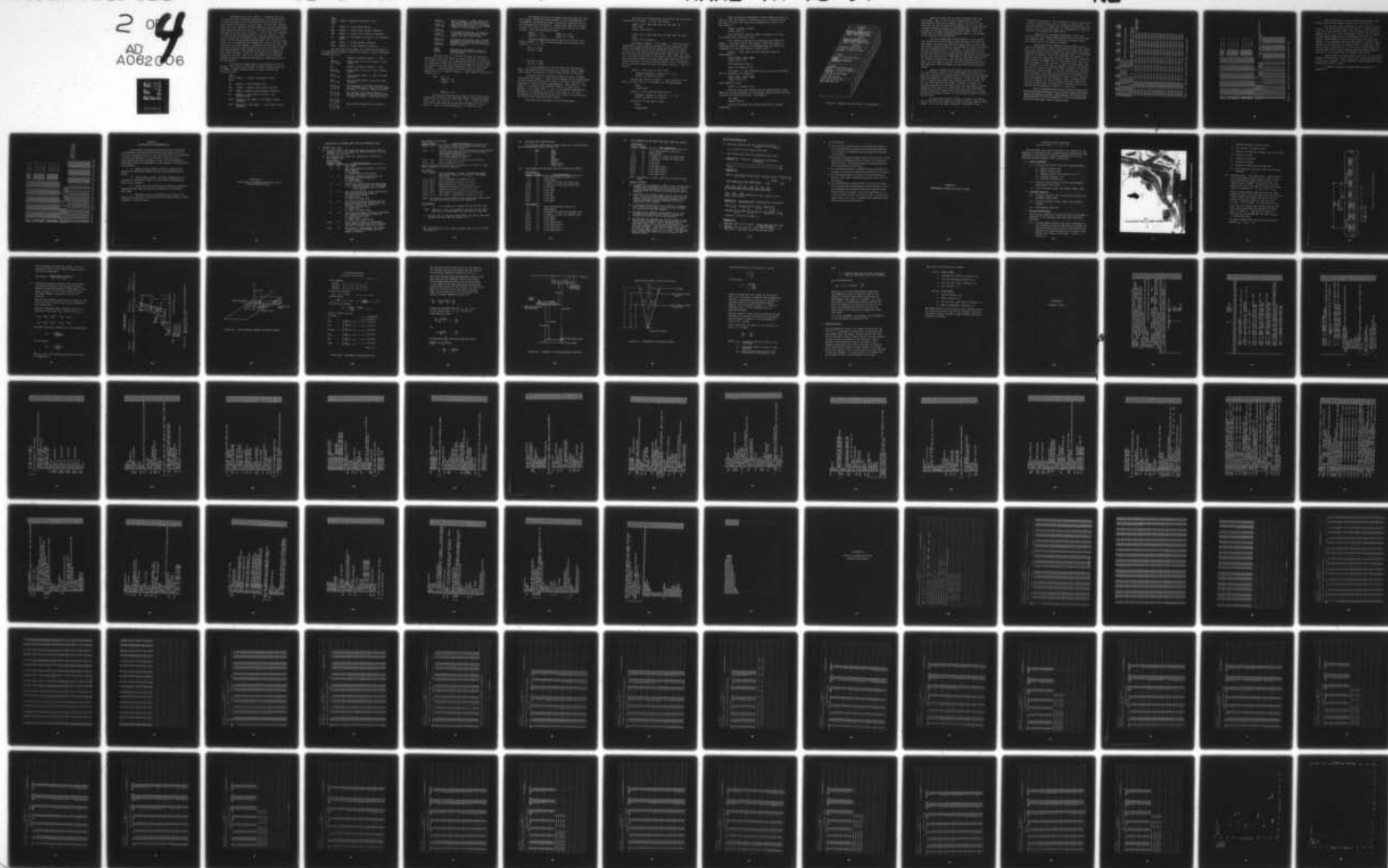
A brief overview of the program operation will be given before the more detailed discussion. The main program SLED reads in the input data, scales it where necessary, and writes it out. In broad outline this input data consists of location and orientation data for each of the two cameras and the position coordinates of certain reference points rigidly affixed to the sled. Also, the film frame coordinates of the moving points are input for each of the cameras for each film frame. The film frame coordinates of some of the fixed reference points are also input, but at present no use is being made of this information in program SLED. The time increment desired between solution points is input and a run identification number. The exact reference times for at least two frames are read in for each camera. Subroutine TMSGN (Time Assign) then, by linear interpolation, assigns to each of the other film frames its correct time.

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Subroutine ALL is then called. It computes the time,  $t_s$ , at which each of the four moving points is to be determined. It then finds that pair of film frames from each camera whose times bracket the present  $t_s$  value. Then, for the first targeted point ALL calls FIND once for each camera to get the interpolated rays toward that point at time  $t_s$ . ALL then calls SOLVE to find the position of the point at time  $t_s$ . This is done in succession for each of the four moving points on the test subjects. Then,  $t_s$  is increased by the desired time increment between solution points and the whole process repeated again. This continues until a time,  $t_s$ , is requested which exceeds the time of the last frame input for one of the cameras. Throughout this process the sum of the two ray solution miss distances are stored for each of the four moving points. Also stored is the sum of the squares of these miss distances. After the four moving points have been located for the last value of  $t_s$ , the sample mean and sample standard deviation of the miss distances is computed for each of the four points.

The principal symbols used in the program will now be defined. This first list consists of those variables appearing in COMMON. COMMON consists solely of camera location and orientation data.

RAA	}	Camera a position coordinates (feet).
RAB		
RAC		
FA		Camera a focal length (feet).
THA		Camera a optical axis azimuth (radians).
PHA		Camera a optical axis elevation (radians).
GA		Camera a tilt angle in radians. Not presently used.
THIA		Azimuth of the camera a film frame $\bar{I}$ factor (radians).
PHIA		Elevation of the camera a film frame $\bar{I}$ vector (radians).

RBA	}	Camera b position coordinates (feet).
RBB		
RBC		
FB		Camera b focal length (feet).
THB		Camera b optical axis azimuth (radians).
PHB		Camera b optical axis elevation (radians).
GB		Camera b tilt angle in radians. Not presently used.
THIB		Camera b $\bar{I}$ axis azimuth (radians).
PHIB		Camera b $\bar{I}$ axis elevation (radians).

The next part of the symbol list consists principally of the dimensioned variables used by the program. A short discussion follows this list.

NA	Number of frames of camera a data.
NFRA(I), I = 1, NA	Frame number of the ith frame of camera a data.
NB	Number of frames of camera b data.
NFRB(I), I = 1, NB	Frame number of the ith frame of camera b data.
TA(I), I = 1, NA	Time at which camera a shot ith frame (seconds).
TB(I), I = 1, NB	Time at which camera b shot ith frame (seconds).
XA(I,J), I = 1, NA; J = 1, 8	The horizontal film frame coordinate of the jth image point on the ith film frame of camera a (counts: 1000/counts/inch).
YA (I,J), I = 1, NA; J = 1, 8	The vertical film frame coordinate of the jth image point on the ith film frame of camera a (counts: 1000/counts/inch).
XB (I,J), I = 1, NB; J = 1, 8	The analogous quantities for camera b.
YB (I,J), I = 1, NB; J = 1, 8	



NREFA(I), I = 1, 10	Up to 10 camera a frame numbers and their associated times may be read in and used by TMSGN to assign the correct times to all the camera a film frames (TREFA (I) values in seconds).
TREFA (I), I = 1, 10	
NREFB(I), I = 1, 10	The analogous quantities for camera b.
TREFB(I), I = 1, 10	In practice only two reference frame numbers and times need be used.
SMEAN (J), J = 5, 8	The sample mean and the sample standard deviation of the two-ray-solution miss distances for each of the four targeted points (inches).
SSDEV(J), J = 5, 8	
XX(10) YY(10) ZZ(10)	The position coordinates of up to 10 reference points rigidly attached to the sled (feet).

The above list can be further clarified by discussing those quantities in the above list that pertain only to camera a. The cameras are brought up to speed shortly before the sled begins to accelerate in order that the picture-taking rate of each camera be constant during the actual experiment. Thus, the first frame of camera a containing data of interest might be frame 80. Assume there are 33 frames of camera a data numbered consecutively from 80 to 112.

```

Then  NA = 33
      NFRA(1) = 80
      NFRA(2) = 81
      .
      .
      .
      NFRA(33) = 112

```

Now there are eight points on each of these frames whose coordinates are read on the film frame reader. The program stores these as XA (I,J), YA(I,J) I = 1, 33; J = 1, 8. Thus, the fifth point read on the ninth frame would have coordinates XA (9,5), YA (9,5). This is on frame number 88, i.e., NFRA (9) = 88.

The cameras do run at a constant rate once they have come up to speed. There are timing flashes of light superimposed on the negative from which the time an individual frame was shot can be determined quite accurately. Suppose that frame 80 is found to have been taken at time 0.142 seconds and frame 112 at 0.208 seconds. Then the program would store

```
NREFA(1) = 80          NREFA (2) = 112
TREFA(1) = 0.142       TREFA (2) = 0.208.
```

Subroutine TMSGN then assigns the correct time to each frame of camera a data by linear interpolation and stores them in TA(I), I = 1, 33, i.e.,

```
TA (1) = 0.142
TA (2) = 0.144
.
.
.
TA (32) = 0.206
TA (33) = 0.208.
```

It is not necessary to use the first and last frame of data. Had frames 88 and 99 been used as reference frames, TMSGN would linearly extrapolate to those frames outside the interval.

Precisely the same discussion applies to those variables associated with camera b. Since the two cameras are not synchronized, the only connection between their data is the time flash which is inscribed on both film strips simultaneously. Thus, camera a and camera b in general have different numbers of frames and in general, no two frames from a and b are snapped simultaneously. Moreover, it is generally true that a test time  $t_s$  at which the position of the moving points are to be output is not coincident with that of any frame from either camera.

The input for the program will now be discussed.

The first four cards contain the location and orientation information for camera a and b as follows:

Cards 1 and 2: RAA, RAB, RAC, FA, THA, PHA, GA  
THIA, PHIA

Format (4F10.0/5F10.0)

Cards 3 and 4: RBA, RBB, RBC, FB, THB, PHB, GB, THIB,  
PHIB

Format (4F 10.0/5F10.0).

The input of camera a and camera b film frame data is terminated by signal cards at the ends of their respective data decks. The numbers NA and NB are determined during the read-in of this data. The data for each film frame requires two cards. The first card for each frame contains the frame number and then the film frame coordinates for the images of the four fixed points. The second card contains the same frame number and then the film frame coordinates for the four moving points. NA is incremented by one as the two cards for each new frame of camera a data are read in.

Camera a data input for each frame

NFRA(NA), ((XA(NA,I), YA(NA,I)), I = 1, 8)

Format (I5, 8F7.0/5X, 8F7.0).

Termination cards for camera a input consists of two cards, the first with 9's in columns 1-5, the second blank.

99999

A BLANK CARD

Camera b data input for each frame is

NFRB(NB), ((XB(NB,I), YB(NB,I)), I = 1, 8)

Format (I5, 8F7.0 / 5X, 8F7.0).

Termination is the same as camera a.

99999

A BLANK CARD.



Next the position coordinates of some reference points are read in. NHP, the number of reference points, is defined as they are read in. Again, the read-in is terminated by a signal card. The format is

XX(NHP), YY(NHP), ZZ(NHP)  
Format (3F10.0).

The termination card has 100000.0 punched in the first ten columns and is otherwise blank.

The reference times and the reference frame numbers for camera a are then input to the program. NTMA, the number of reference times for camera a, is determined when the read-in is terminated by a card with 99999 in columns 12-16.

Camera a data input for each reference time and frame number is

TREFA (NTMA), NREFA (NTMA)  
Format (F10.0, I6)

The termination card is  
99999 (in columns 12-16).

The camera b time reference input is precisely analogous and is terminated in the same way.

TREFB (NTMB), NREFB (NTMB)  
Format (F10.0, I6)

with termination card

99999 ( in columns 12-16).

The last input card contains the run identification number DESIG and the time increment DT (in seconds) desired between position solutions for the moving points. The format is

DT, DESIG  
Format (2F10.0).

Figure 49 indicates the various sections of a typical input deck.



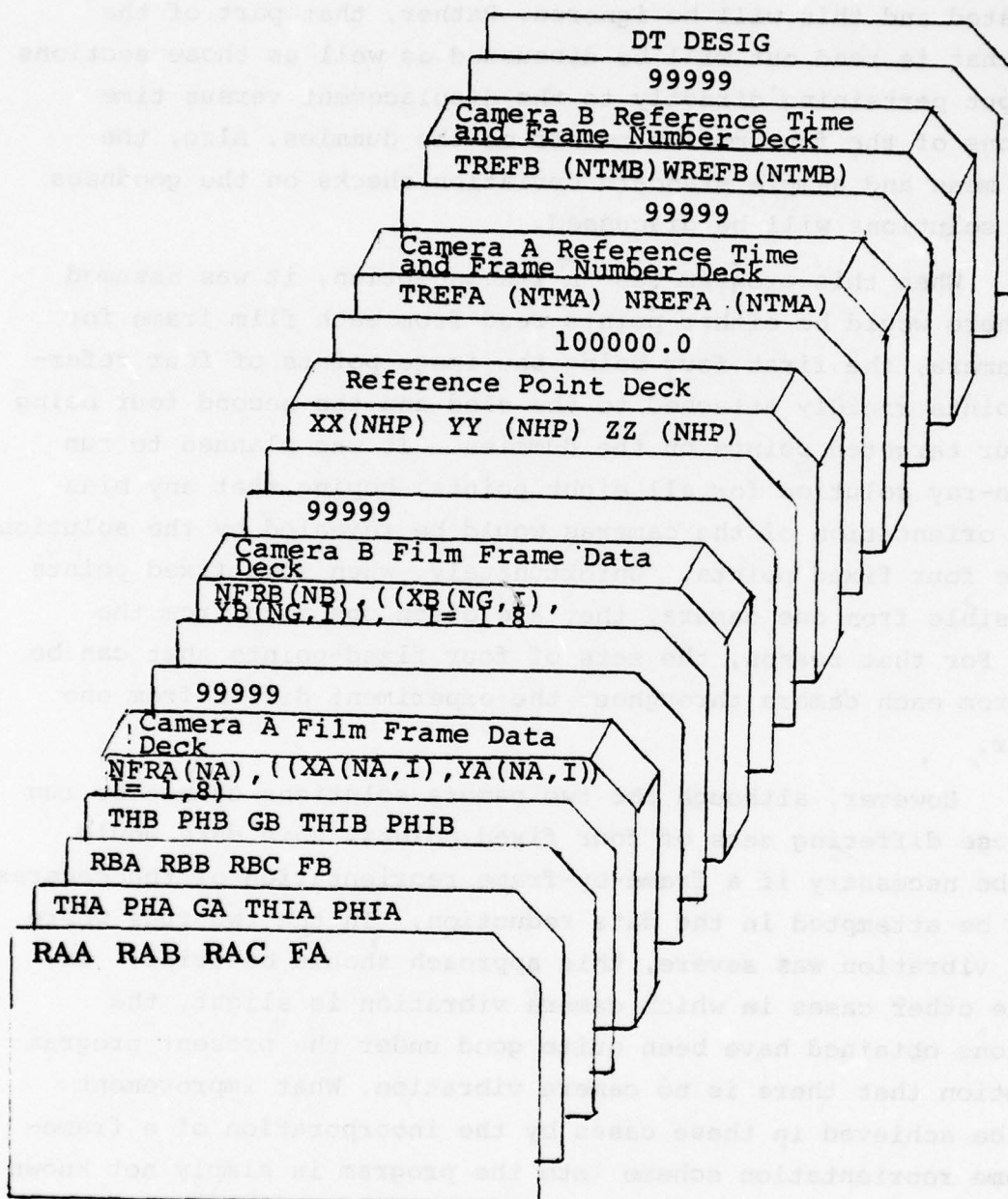


Figure 49. Typical Data Deck Input to Program SLED.

There is a great deal of output presently taken from the program. Much of this is debug output which can now be eliminated and this will be ignored. Rather, that part of the input that is read out will be discussed as well as those sections of output pertaining directly to the displacement versus time solutions of the four moving points on the dummies. Also, the sample mean and sample standard deviation checks on the goodness of the solutions will be discussed.

When this program was in its inception, it was assumed that there would be either points read from each film frame for each camera, the first four being the image points of four reference points rigidly attached to the sled and the second four being the four targeted points on the dummies. It was planned to run the two-ray solution for all eight points, hoping that any bias in the orientation of the cameras would be revealed by the solutions for the four fixed points. Unfortunately, when some fixed points are visible from one camera, they are often obscured from the other. For that reason, the sets of four fixed-points that can be read from each camera throughout the experiment differ from one another.

However, although the two camera solutions cannot be run for these differing sets of four fixed points, this data would still be necessary if a frame-by-frame reorientation of the cameras should be attempted in the data reduction. In the two runs where camera vibration was severe, this approach should be tried. In all the other cases in which camera vibration is slight, the solutions obtained have been quite good under the present program assumption that there is no camera vibration. What improvement could be achieved in these cases by the incorporation of a frame-by-frame reorientation scheme into the program is simply not known at this time.

As the program presently stands, it makes no use whatsoever of the first four image points read in for each frame of each camera. Nor is any use made of position coordinates of the

reference points read in. This information is being retained with a view as to modifications yet to be made to program SLED. For the above reasons, the sample mean and sample standard deviation read-out for the first four points are recorded as 0.0 since no solutions are attempted for these points.

Figure 50 is a tab page showing some of the output. The first two lines are the camera location and orientation data for cameras a and b. Position coordinates and focal lengths are in feet and all the angles in radians.

The bracketed data immediately below consists of the position coordinates of each of the reference points input. These are in feet and are given with respect to the program right-hand coordinate system as are the camera positions above. The reference times are in seconds. Part of the frame data for camera a is output. There are three lines for each frame of data. Taking the first frame as an example, the "1" identifies this as the first frame of camera a data, the "80" is the film frame number, and the .141864E + 00 is the time in seconds at which it was snapped. The next line gives the film frame image coordinates of the four fixed points read for camera a and the following line contains the coordinates of the four targeted points on the dummies. All these film frame image coordinates are output in feet. After all the film frame data for both cameras a and b has been output, the time increment, dt, desired between solution positions for each of the four points is printed out in seconds. Refer to the complete listing beginning on page F-15 to see this.

Figure 51 displays that page of the tab on which the sample mean and the sample standard deviation for each of the four targeted points (point numbers 5 through 8) are provided. These quantities are the mean and the standard deviation of all the miss distances, d, in the two-ray solutions for each of the moving points. They are output in inches.









The last section of output gives the positions of the moving points on the subjects versus time. See Figure 52.

The position versus time data is first output for points 5 and 6, the forehead and chin of the subject in the passenger seat. The first quantity is the time in seconds. The next three numbers are the x, y, and z coordinates of point five in inches. The next three numbers are the coordinates of point six in inches. The coordinates of the moving points are output with respect to the original left-hand experimental coordinate system affixed to the sled. The run number is just an identifier. Then points 5 and 6 are specified. All this data is also punched out on cards for input to other programs. The last three numbers of each line of this output are not punched on the cards.

These numbers are debug output. The first is the distance between the point pair 5 and 6 to the left. The second and third are the miss distance,  $d$ , that occurred in the computation of the positions of points 5 and 6.

A complete listing of program SLED is presented in Appendix F.

FINO	.202264E+00	-.150750E+06	.465000E-01	-.152333E+00	.500000E+01	.204000E+03			
SOLVE	-.151595E+00	-.300921E-01	-.152000E+00	.434355E-01	.700617E+00	.118425E+01	.224636E+01	126	
FINO	.203398E+00	-.113417E+00	.600000E-01	-.117790E+00	.612500E-01	.204000E+00			
FINO	.202268E+00	-.149167E+00	.199167E-01	-.149750E+00	.195633E-01	.204000E+00			
SOLVE	-.113421E+00	.600036E-01	-.149657E+00	.196367E-01	.945439E+00	-.143721E+01	.255607E+01	127	
CORR	-.588562E+00	-.121360E+00	.97255E+00	.143717E-01	.157796E-01				
FINO	.644625E+00	-.299439E+00	.220532E+01	.300164E-01	.326768E-01	.206000E+00			
FINO	.203944E+00	.593333E-01	.250000E-01	.610000E-01	.259167E-01	.206000E+00			
FINO	.204330E+00	.104167E+00	.551667E-01	.101667E+00	.552500E-01	.206000E+00			
SOLVE	.603476E-01	.256479E-01	.102141E+00	.552442E-01	.126178E+01	-.134204E+01	.223462E+01	128	
FINO	.203398E+00	.765833E-01	.975000E-02	.746167E-01	.808333E-02	.206000E+00			
FINO	.204330E+00	.126917E+00	.500000E-01	.130667E+00	.430000E-01	.206000E+00			
SOLVE	.733276E-01	-.813573E-02	.123954E+00	.491901E-01	.824994E+00	.206000E+00			
FINO	.203944E+00	-.150583E+00	.900433E-01	-.151667E+00	.931667E-01	.206000E+00	.237075E+01	129	
FINO	.204330E+00	-.152333E+00	.500000E-01	-.156250E+00	.528333E-01	.206000E+00			
SOLVE	-.151633E+00	.930697E-01	-.155505E+00	.522943E-01	.695149E+00	.112611E+01	.224345E+01	130	
FINO	.203944E+00	-.113417E+00	.600000E-01	-.117750E+00	.612500E-01	.206000E+00			
FINO	.204330E+00	-.149750E+00	.195833E-01	-.151667E+00	.153167E-01	.206000E+00			
SOLVE	-.117617E+00	.612107E-01	-.152322E+00	.166140E-01	.982693E+00	-.151684E+01	.257922E+01	131	
CORR	-.588573E+00	-.321275E+00	.977112E+00	.156571E-01	.165019E-01				
FINO	.644776E+00	-.299439E+00	.220601E+01	.295619E-01	.323806E-01	.208000E+00			
FINO	.206065E+00	.610000E-01	.259167E-01	.611667E-01	.235000E-01	.208000E+00			
FINO	.206392E+00	.101667E+00	.552500E-01	.101417E+00	.550000E-01	.208000E+00	.223321E+01	132	
SOLVE	.632422E-01	.292644E-01	.101472E+00	.550550E-01	.126043E-01	.208000E+00			
FINO	.206065E+00	.794167E-01	.808333E-02	.813333E-01	.341667E-02	.208000E+00			
FINO	.206392E+00	.130667E+00	.490000E-01	.131000E+00	.480033E-01	.208000E+00			
SOLVE	.812074E-01	-.372341E-02	.130427E+00	.482850E-01	.541703E+00	.208000E+00	.238001E+01	133	
FINO	.206065E+00	-.151667E+00	.911667E-01	-.149447E+00	.981667E-01	.208000E+00			
FINO	.206392E+00	-.156250E+00	.528333E-01	-.156750E+00	.526667E-01	.208000E+00			
SOLVE	-.143965E+00	.977340E-01	-.156640E+00	.527033E-01	.637825E+00	.113332E+01	.226163E+01	134	
FINO	.206065E+00	-.117750E+00	.612500E-01	-.115667E+00	.633333E-01	.208000E+00			
FINO	.206392E+00	-.153667E+00	.159157E-01	-.154250E+00	.153167E-01	.208000E+00			
SOLVE	-.115044E+00	.631965E-01	-.154122E+00	.153167E-01	.976730E+00	-.151895E+01	.259988E+01	135	
CORR	-.588562E+00	-.321298E+00	.976985E+00	.152101E-01	.170844E-01				
NO OF PTS	PT NO MEAN	DEV	34	10.	0.				
NO OF PTS	PT NO MEAN	DEV	34	20.	0.				
NO OF PTS	PT NO MEAN	DEV	34	30.	0.				
NO OF PTS	PT NO MEAN	DEV	34	40.	0.				
NO OF PTS	PT NO MEAN	DEV	34	50.	0.				
NO OF PTS	PT NO MEAN	DEV	34	60.	0.				
NO OF PTS	PT NO MEAN	DEV	34	70.	0.				
NO OF PTS	PT NO MEAN	DEV	34	80.	0.				
NO OF PTS	PT NO MEAN	DEV	34	90.	0.				
NO OF PTS	PT NO MEAN	DEV	34	100.	0.				
NO OF PTS	PT NO MEAN	DEV	34	110.	0.				
NO OF PTS	PT NO MEAN	DEV	34	120.	0.				
NO OF PTS	PT NO MEAN	DEV	34	130.	0.				
NO OF PTS	PT NO MEAN	DEV	34	140.	0.				
NO OF PTS	PT NO MEAN	DEV	34	150.	0.				
NO OF PTS	PT NO MEAN	DEV	34	160.	0.				
NO OF PTS	PT NO MEAN	DEV	34	170.	0.				
NO OF PTS	PT NO MEAN	DEV	34	180.	0.				
NO OF PTS	PT NO MEAN	DEV	34	190.	0.				
NO OF PTS	PT NO MEAN	DEV	34	200.	0.				
NO OF PTS	PT NO MEAN	DEV	34	210.	0.				
NO OF PTS	PT NO MEAN	DEV	34	220.	0.				
NO OF PTS	PT NO MEAN	DEV	34	230.	0.				
NO OF PTS	PT NO MEAN	DEV	34	240.	0.				
NO OF PTS	PT NO MEAN	DEV	34	250.	0.				
NO OF PTS	PT NO MEAN	DEV	34	260.	0.				
NO OF PTS	PT NO MEAN	DEV	34	270.	0.				
NO OF PTS	PT NO MEAN	DEV	34	280.	0.				
NO OF PTS	PT NO MEAN	DEV	34	290.	0.				
NO OF PTS	PT NO MEAN	DEV	34	300.	0.				
NO OF PTS	PT NO MEAN	DEV	34	310.	0.				
NO OF PTS	PT NO MEAN	DEV	34	320.	0.				
NO OF PTS	PT NO MEAN	DEV	34	330.	0.				
NO OF PTS	PT NO MEAN	DEV	34	340.	0.				
NO OF PTS	PT NO MEAN	DEV	34	350.	0.				
NO OF PTS	PT NO MEAN	DEV	34	360.	0.				
NO OF PTS	PT NO MEAN	DEV	34	370.	0.				
NO OF PTS	PT NO MEAN	DEV	34	380.	0.				
NO OF PTS	PT NO MEAN	DEV	34	390.	0.				
NO OF PTS	PT NO MEAN	DEV	34	400.	0.				
NO OF PTS	PT NO MEAN	DEV	34	410.	0.				
NO OF PTS	PT NO MEAN	DEV	34	420.	0.				
NO OF PTS	PT NO MEAN	DEV	34	430.	0.				
NO OF PTS	PT NO MEAN	DEV	34	440.	0.				
NO OF PTS	PT NO MEAN	DEV	34	450.	0.				
NO OF PTS	PT NO MEAN	DEV	34	460.	0.				
NO OF PTS	PT NO MEAN	DEV	34	470.	0.				
NO OF PTS	PT NO MEAN	DEV	34	480.	0.				
NO OF PTS	PT NO MEAN	DEV	34	490.	0.				
NO OF PTS	PT NO MEAN	DEV	34	500.	0.				
NO OF PTS	PT NO MEAN	DEV	34	510.	0.				
NO OF PTS	PT NO MEAN	DEV	34	520.	0.				
NO OF PTS	PT NO MEAN	DEV	34	530.	0.				
NO OF PTS	PT NO MEAN	DEV	34	540.	0.				
NO OF PTS	PT NO MEAN	DEV	34	550.	0.				
NO OF PTS	PT NO MEAN	DEV	34	560.	0.				
NO OF PTS	PT NO MEAN	DEV	34	570.	0.				
NO OF PTS	PT NO MEAN	DEV	34	580.	0.				
NO OF PTS	PT NO MEAN	DEV	34	590.	0.				
NO OF PTS	PT NO MEAN	DEV	34	600.	0.				
NO OF PTS	PT NO MEAN	DEV	34	610.	0.				
NO OF PTS	PT NO MEAN	DEV	34	620.	0.				
NO OF PTS	PT NO MEAN	DEV	34	630.	0.				
NO OF PTS	PT NO MEAN	DEV	34	640.	0.				
NO OF PTS	PT NO MEAN	DEV	34	650.	0.				
NO OF PTS	PT NO MEAN	DEV	34	660.	0.				
NO OF PTS	PT NO MEAN	DEV	34	670.	0.				
NO OF PTS	PT NO MEAN	DEV	34	680.	0.				
NO OF PTS	PT NO MEAN	DEV	34	690.	0.				
NO OF PTS	PT NO MEAN	DEV	34	700.	0.				
NO OF PTS	PT NO MEAN	DEV	34	710.	0.				
NO OF PTS	PT NO MEAN	DEV	34	720.	0.				
NO OF PTS	PT NO MEAN	DEV	34	730.	0.				
NO OF PTS	PT NO MEAN	DEV	34	740.	0.				
NO OF PTS	PT NO MEAN	DEV	34	750.	0.				
NO OF PTS	PT NO MEAN	DEV	34	760.	0.				
NO OF PTS	PT NO MEAN	DEV	34	770.	0.				
NO OF PTS	PT NO MEAN	DEV	34	780.	0.				
NO OF PTS	PT NO MEAN	DEV	34	790.	0.				
NO OF PTS	PT NO MEAN	DEV	34	800.	0.				
NO OF PTS	PT NO MEAN	DEV	34	810.	0.				
NO OF PTS	PT NO MEAN	DEV	34	820.	0.				
NO OF PTS	PT NO MEAN	DEV	34	830.	0.				
NO OF PTS	PT NO MEAN	DEV	34	840.	0.				
NO OF PTS	PT NO MEAN	DEV	34	850.	0.				
NO OF PTS	PT NO MEAN	DEV	34	860.	0.				
NO OF PTS	PT NO MEAN	DEV	34	870.	0.				
NO OF PTS	PT NO MEAN	DEV	34	880.	0.				
NO OF PTS	PT NO MEAN	DEV	34	890.	0.				
NO OF PTS	PT NO MEAN	DEV	34	900.	0.				
NO OF PTS	PT NO MEAN	DEV	34	910.	0.				
NO OF PTS	PT NO MEAN	DEV	34	920.	0.				
NO OF PTS	PT NO MEAN	DEV	34	930.	0.				
NO OF PTS	PT NO MEAN	DEV	34	940.	0.				
NO OF PTS	PT NO MEAN	DEV	34	950.	0.				
NO OF PTS	PT NO MEAN	DEV	34	960.	0.				
NO OF PTS	PT NO MEAN	DEV	34	970.	0.				
NO OF PTS	PT NO MEAN	DEV	34	980.	0.				
NO OF PTS	PT NO MEAN	DEV	34	990.	0.				
NO OF PTS	PT NO MEAN	DEV	34	1000.	0.				
NO OF PTS	PT NO MEAN	DEV	34	1010.	0.				
NO OF PTS	PT NO MEAN	DEV	34	1020.	0.				
NO OF PTS	PT NO MEAN	DEV	34	1030.	0.				
NO OF PTS	PT NO MEAN	DEV	34	1040.	0.				
NO OF PTS	PT NO MEAN	DEV	34	1050.	0.				
NO OF PTS	PT NO MEAN	DEV	34	1060.	0.				
NO OF PTS	PT NO MEAN	DEV	34	1070.	0.				
NO OF PTS	PT NO MEAN	DEV	34	1080.	0.				
NO OF PTS	PT NO MEAN	DEV	34	1090.	0.				
NO OF PTS	PT NO MEAN	DEV	34	1100.	0.				
NO OF PTS	PT NO MEAN	DEV	34	1110.	0.				
NO OF PTS	PT NO MEAN	DEV	34	1120.	0.				
NO OF PTS	PT NO MEAN	DEV	34	1130.	0.				
NO OF PTS	PT NO MEAN	DEV	34	1140.	0.				
NO OF PTS	PT NO MEAN	DEV	34	1150.	0.				
NO OF PTS	PT NO MEAN	DEV	34	1160.	0.				
NO OF PTS	PT NO MEAN	DEV	34	1170.	0.				
NO OF PTS	PT NO MEAN	DEV	34	1180.	0.				
NO OF PTS	PT NO MEAN	DEV	34	1190.	0.				
NO OF PTS	PT NO MEAN	DEV	34	1200.	0.				
NO OF PTS	PT NO MEAN	DEV	34	1210.	0.				
NO OF PTS	PT NO MEAN	DEV	34	1220.	0.				
NO OF PTS	PT NO MEAN	DEV	34	1230.	0.				
NO OF PTS	PT NO MEAN	DEV	34	1240.	0.				
NO OF PTS	PT NO MEAN	DEV	34	1250.	0.				
NO OF PTS	PT NO MEAN								



SECTION 4  
CONCLUSIONS AND RECOMMENDATIONS

The processes developed and applied during the period of performance have satisfied the basic requirements for which they were developed. There is still much that could be accomplished to refine the programs for the purposes of improving cost effectiveness and user confidence in the solutions generated. Continuing review is recommended for the purpose of accomplishing the following.

- A. Modify program HIFPD to include a computerized analysis of differences between the raw and smoothed solution points.
- B. Modify program HIFPD to provide computerized calculations of conversion factors for the various anthropometric points being tracked.
- C. Investigate the desirability of employing smoothing techniques other than the moving arc quadratic fit currently being used.
- D. Determine accuracy requirements and criteria for analyzing the accuracy of solutions prior to applications of these processes to future studies.



# DESCRIPTION OF PROGRAM INPUT DATA AND PARAMETER CODES

## 1. PROGRAM SETUP CARDS

- A) The first card in the setup deck must contain the data in columns 1 to 10; for example, 11 FEB 74 or FEB 11, 74 (only one date card per job).
- B) The following four cards are required for each test in the computer job:

### Card Number 1

Column	Format	Data Description
1-5	5F	Test number
6	11	TRX--flag controlling polarity of X-axis data; blank or 0--no change; 1--change sign of X-axis data
7	11	TRZ--flag controlling input data and data blank or 0--blank or 1--blank
8	11	TRYS--flag controlling input data; blank or 0--blank and process all 3 variables; 1--blank and process only variables 1, 2, and 3
9	11	ISL--flag controlling linear velocity and acceleration data; blank or 0--print and plot data; 1--print only; 2--omit all input data
11	11	IPA--flag controlling angular velocity and acceleration data; blank or 0--print and plot data; 1--print only; 2--omit all angular data
12	11	TPC--flag controlling variable displacement with respect to lead data; blank or 0--print and plot data; 1--print only; 2--omit these computations
14-16	3F	First frame included in displacement with respect to the lead plot (if blank, the first available frame is plotted)
17-19	3F	Last frame in displacement with respect to the lead plot (if blank, the last frame is plotted)

## DESCRIPTION OF PROGRAM INPUT DATA AND PARAMETER CODES

### I. PROGRAM SETUP CARDS

- A) The first card in the setup deck must contain the date in columns 1 to 10; for example, 12 FEB 74 or FEB 11,74 (only one date card per job).
- B) The following four cards are required for each test in the computer job:

#### Card Number 1

Column	Format	Data Description
1-5	A5	Test number
6	11	IRX--flag controlling polarity of X-axis data- blank or 0---no change 1---change sign of X-axis data
7	11	IPR--flag controlling input data and difference printout -blank or 0---print data 1---omit printout
8	11	ITYPE--flag controlling input data-blank or 0 ---read and process all 8 variables 1 ---read and process only variables 1,2,7, and 8
9	11	IPL--flag controlling linear velocity and acceleration data -blank or 0---print and plot data 1---print only 2---omit all linear data
11	11	IPA--flag controlling angular velocity and acceleration data (shoulder-hip and head pt.1, head pt.2)--blank or 0---print and plot data 1---print only 2---omit all angular data
13	11	IPC--flag controlling variable displacement with respect to sled data -blank or 0---print and plot data 1---print only 2---omit these computations
14-16	13	First frame included in displacement with respect to the sled plot (if blank, the first available frame is plotted).
17-19	13	Last frame in displacement with respect to the sled plot (if blank, the last frame is plotted).

Card Number 2 (Continued)

Column	Format	Data Description
20-21	12	The number of sets (M) of linear velocity and acceleration to be computed.
23-24	211	Variable code of variable and reference respectively (see variable codes in Item II) for first set of linear data; for example, 21---sled relative to range or 32---hip relative to sled
26-27	211	Same as above for the 2nd set of linear data
29-30	211	Same as above for 3rd set

Repeat the above for each of the M (maximum of 12) sets of linear motion (Format: IX, 211 for each set).

Card Number 3

1-10	F10.0	Time calibration---number of frames per second. May be left blank if film speed is 500 frames per second.
11-20	F10.0	SLED calibration in counts per foot
21-30	F10.0	HIP calibration in counts per foot*
31-40	F10.0	KNEE calibration in counts per foot*
41-50	F10.0	SHOULDER calibration in counts per foot*
51-60	F10.0	ELBOW calibration in counts per foot*
61-70	F10.0	HEAD POINT 1 calibration in counts per foot
71-80	F10.0	HEAD POINT 2 calibration in counts per foot

NOTE: The decimal must be punched in the above data fields unless the data are integer and are right justified.

Card Number 4

1        11        9 in column 1 to indicate the end of test input

NOTE: Cards 1, 2, and 3 are placed in front of the test deck and card 4 is placed after the last frame in the test.

C) The last card in the input deck (before the end of job card) contains the word "END" in columns 1 to 3.

---

\* The calibration field for these variables must be zero or blank for ITYPE = 1.

## II. VARIABLE CODE IDENTIFICATION

The following code versus variable name list is used throughout the program and card 2 in Item 1-B:

<u>Code</u>	<u>Name</u>
1	Range
2	Sled
3	Hip
4	Knee
5	Shoulder
6	Elbow
7	Head Point 1
8	Head Point 2

## III. CARD FORMATS FOR THE TEST INPUT DATA CARDS FOR ITYPE=0

### Card Number 1

<u>Column</u>	<u>Format</u>	<u>Data Description</u>
1	11	Card identification (must be 1).
2-5	14	Frame number
6-12	17	X reading in counts for Range data
13-19	17	Z reading in counts for Range data
20-26	17	X for Sled
27-33	17	Z for Sled
34-40	17	X for Hip
41-47	17	Z for Hip
48-54	17	X for Knee
55-61	17	Z for Knee

### Card Number 2

1	11	Card identification (must be 2)
2-5	14	Frame Number
6-12	17	X reading in counts for Shoulder data
13-19	17	Z reading in counts for Shoulder data
20-26	17	X for Elbow
27-33	17	Z for Elbow
34-40	17	X for Head Point 1
41-47	17	Z for Head Point 1
48-54	17	X for Head Point 2
55-61	17	Z for Head Point 2



#### IV. CARD FORMATS FOR THE TEST INPUT DATA CARDS FOR ITYPE=1

##### Card Number 1

Column	Format	Data Description
1	11	Card identification (must be 1).
2-5	14	Frame number
6-12	17	X reading in counts for Range data
13-19	17	Z reading in counts for Range data
20-26	17	X for Sled
27-33	17	Z for Sled
34-40	17	X for Head Point 1
41-47	17	Z for Head Point 1
48-54	17	X for Head Point 2
55-61	17	Z for Head Point 2

NOTE: For ITYPE = 1, only 1 data card is read for each frame.

#### V. GENERAL COMMENTS

- A) If there are any errors in frame or card identification numbers, error statements will be printed at the top of the first output page for the test and all computations after the listing of the input data will be deleted.
- B) A maximum of 150 frames (MAXN) will be read for each test. If the test input deck contains more than 150 frames, only the first 150 will be processed. This could be changed by changing MAXN and the array dimensions in the program.
- C) If the calibration factor for a variable is missing, flag ICAL(J) is set equal to zero and that variable will be deleted from the analysis.
- D) An eleven point quadratic least-square fit is used throughout the program. This could be changed by changing the value of "NP" in the program.
- E) The CALCOMP plot abscissa and ordinate scales for the velocity and acceleration data are determined by the plot subroutine (CPLT). The X (abscissa) and Z (ordinate) scales for the variable relative to the sled data are constants. The X-scale ranges from -1.4 to 2.6 feet for IRX = 0 and -3.6 to 0.4 feet for IRX = 1 and Z scale ranges from 0.0 to 4.0 feet. Any displacements outside this range will be set equal to the limiting value.

## HYGE Program Setup Cards

- 1) DATA card, used once per job: 

--	--	--	--	--	--	--	--	--	--

  
Col.1 Col.10

e.g. 12 FEB 74 (first card in input deck).

- 2) The following four cards are required for each test:

**CARD No. 1** TITLE Card --80 columns of alphanumeric information.

--

  
Col.1 80

**CARD No. 2**

TEST No. 

--	--	--	--	--

 IRX 

--

 IPR 

--

 ITYPE 

--

 IPL 

--

 IPA 

--

 IPC 

--

  
1 5 6 7 8 9 11 13

M Sets +

FIRST FRAME 

--	--	--

 LAST FRAME 

--	--	--

 M 

--

--	--

2 3 4 5 6 7 8 9  

--	--

--	--

--	--

--	--

--	--

--	--

--	--

--	--

  
26 27 29 30 32 33 35 36 37 39 41 42 44 45 47 48

10 11 12  

--	--

--	--

--	--

 (Maximum of 12 sets; usually 3 or 4.)  
50 51 53 54 56 57

**CARD NO. 3** Calibration Data (frames/second or counts/foot).

TIME: 

--	--

 SLED 

--	--

 HIP \* 

--	--

 KNEE\* 

--	--

  
1 10 11 20 21 30 31 40

SHOULDER\* 

--	--

 ELBOW\* 

--	--

 HEAD PT.1 

--	--

 HEAD 

--	--

  
41 50 51 60 61 70 PT.2 71 80

\* Must be 0 or blank for "ITYPE = 1".

**CARD NO. 4**

Card No. 4 has a "9" in column 1 (insert after the last frame in the data deck).

- 3) END Card, used once per job: Punch "END" in columns 1 to 3. (last card in input deck; before "END OF JOB" Card).

V. General Comments:

- A) If there are any errors in frame or card identification numbers, error statements will be printed at the top of the first output page for the test and all computations after the listing of the input data will be deleted.
- B) A maximum of 150 frames (MAXN) will be read for each test. If the test input deck contains more than 150 frames, only the first 150 will be processed. This could be changed by changing MAXN and the array dimensions in the program.
- C) If the calibration factor for a variable is missing, flag ICAL(J) is set equal to zero and that variable will be deleted from the analysis.
- D) An eleven point quadratic least square fit is used throughout the program. This could be changed by changing the value of "NP" in the program.
- E) The CALCOMP plot abscissa and ordinate scales for the velocity and acceleration data are determined by the plot subroutine (CPLT). The X (abscissa) and Z (ordinate) scales for the variable relative to the sled data are constants. The X scale ranges from -1.4 to 2.6 feet for IRX = 0 and -3.6 to 0.4 feet for IRX = 1 and the Z scale ranges from 0.0 to 4.0 feet. Any displacements outside this range will be set equal to the limiting value.

- A) If there are any errors in format or card identification numbers, error statements will be printed at the top of the first output page for the test and all computations after the listing of the input data will be deleted.
- B) A maximum of 150 frames (MAXN) will be read for each test. If the test input deck contains more than 150 frames, only the first 150 will be processed. This could be changed by changing MAXN and the array dimensions in the program.
- C) If the calibration factor for a variable is missing, the ICALF is set equal to zero and that variable will be deleted from the analysis.
- D) An eleven point quadratic least squares fit is used throughout the program. This could be changed by changing the value of "NPTS" in the program.
- E) The CALCOMP plot routines and coordinate scales for the velocity and acceleration data are controlled by the plot routines (CPLOT).

## APPENDIX B

### PREPARATION OF DATA FOR INPUT TO HIFPD

The data are prepared for input to the HIFPD program by the plot routines (CPLOT) to the data file constant. The X scale ranges from -1.4 to 1.4 for the INX = 0 and -1.4 to 0.4 for INX = 1 and the Y scale ranges from 0.0 to 4.0 for INX = 0 and 0.0 to 1.0 for INX = 1. Any data points outside this range will be set equal to the limiting value.



STANDARD PRACTICE PROCEDURE  
93291-02-1 (Rev. "I", 4 Oct. '76)

This procedure describes the process to be employed in the reduction of photometric data acquired during experimental tests conducted on the Horizontal Impulse Accelerator during the Restraint Systems Dynamics (RSD) investigation.

1. Source Documents

- 1.1 16 mm motion picture film from cameras mounted:
  - a. Onboard Lateral view
  - b. Onboard Oblique view
  - c. Offboard Lateral view (Backup for "A")
  - d. Offboard Downtrack view
  - e. Offboard Overhead view
- 1.2 Restraint System Dynamic Pretest Anthropometric Measurements data sheet.
- 1.3 Sled Coordinate System and Camera Scheme, (RSD).

2. Equipment Required

- 2.1 Producers Service Corp. film digitizer coupled to Teletype w/tape punch.
- 2.2 Teletype Terminal w/tape reader and telephone coupler.
- 2.3 IBM Key punch, Type 029.

3. Editing Requirements

The following sequence of operations shall be followed to determine if all necessary data have been adequately recorded.

- 3.1 Preview Onboard lateral view film to determine if the following points are observable throughout the test period from first motion of the subject with respect to the seat through return to rest of the subject with respect to the seat. (Refer to Figure B-1).

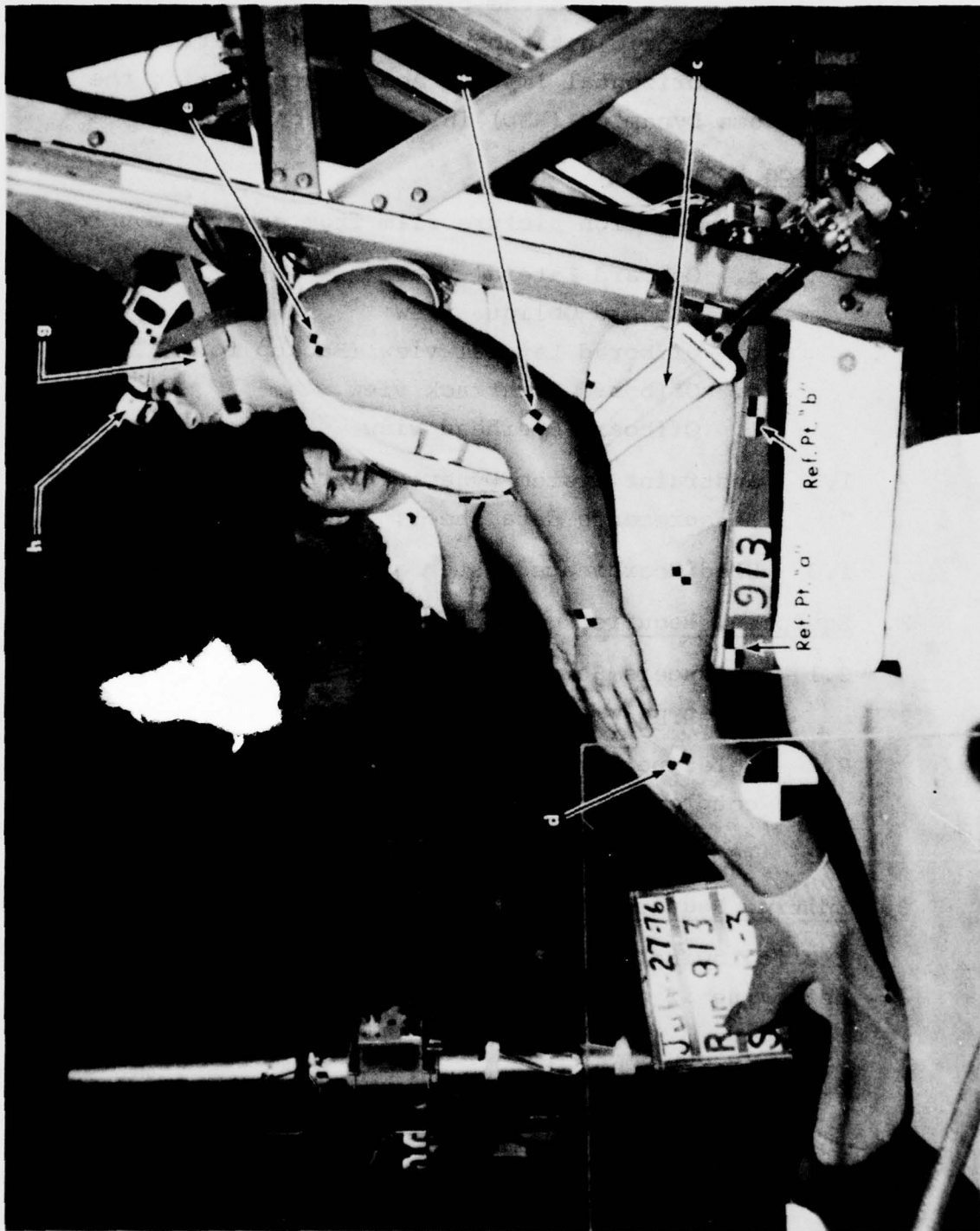


Figure B-1. Anthropometric Points to be Tracked.

- a. Forward fiducial, LH side of seat
- b. Aft fiducial, LH side of seat
- c. Fiducial over hip (or fiducial over iliac crest)
- d. Fiducial on knee
- e. Fiducial on shoulder
- f. Fiducial on elbow
- g. Fiducial on jaw hinge (or head mount)
- h. Accelerometer at origin of 9TAP accelerometer assembly.

3.2 Determine time - film frame table. Assume time to be 0.000 seconds at upper edge of frame in which the synchronizing flash is first observed, set frame counter to 00000. Interpolate time lapse between this point and next 0.1-second time pulse. (Refer to Figure B-2). Set this value to  $t_{e1}$ .

Using the same method, determine the time lapse between the last .01 second time pulse prior to the frame at which the subject returns to rest with respect to the seat (Frame "n" and the start (or top) of this frame. Let this value be  $t_{e2}$ .

Count the 0.01 second time intervals between the first pulse after frame 000 and the last pulse prior to frame "n". Multiply the number of intervals by 0.01 seconds and let this value be  $t_c$  (calibrated time).

The total elapsed time can now be calculated by summing  $t_{e1} + t_{e2} + t_c$ .

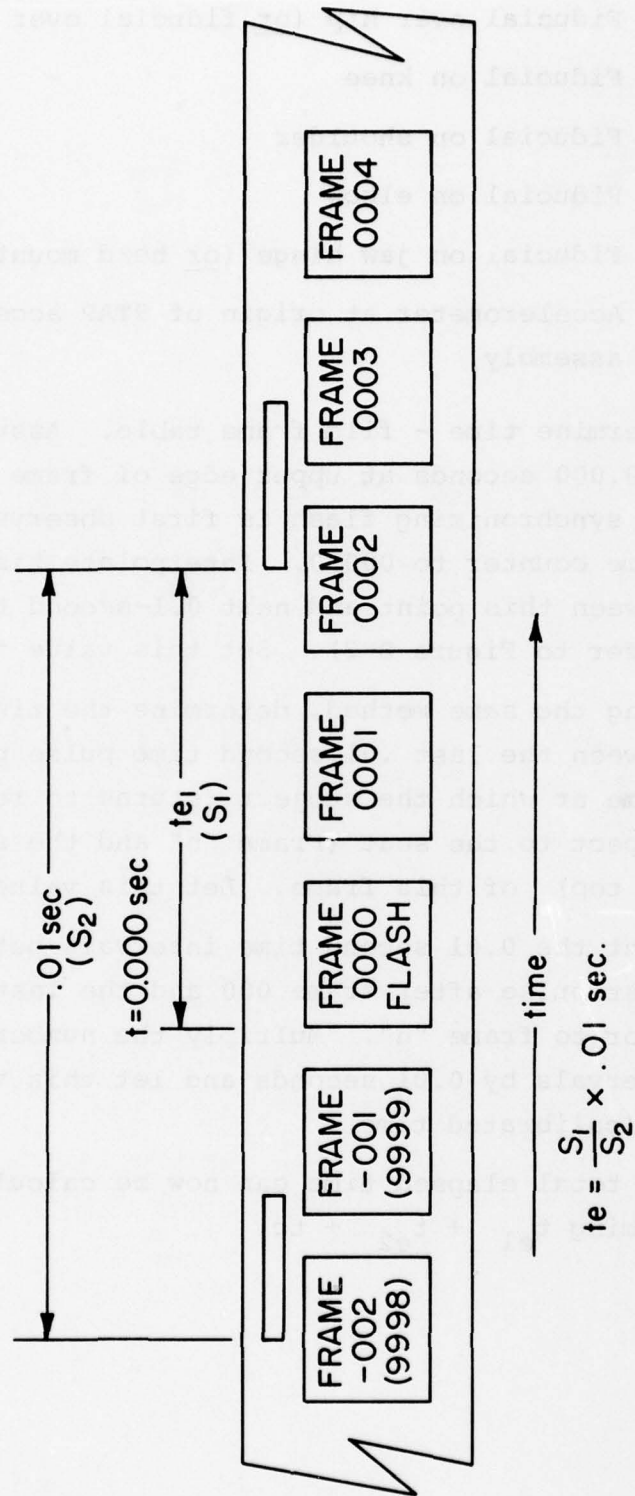


Figure B-2. Time Lapse Determination.



The film speed (or frames per second), which is required as input to the computer program "HIFPD" can now be calculated:

$$\text{Film Speed} = \frac{\text{Frame Count at Frame "n"}}{t_{e1} + t_e + t_{e2}}$$

- 3.3 Determine Conversion Constants using the "widths" information recorded on the "Restraint Systems Dynamics Pretest Anthropometric Measurements" data sheet, (Figure B-3) the "Sled Coordinate System and Camera Scheme" (Figure B-4) and the PSC digitizer.

Read the coordinate of the fiducials mounted on the side of the seat. Record these on the Calibration Form (Figure B-5).

Calculate resultant scalar dimension between the fiducials on the panel ( $s_{pi}$ ) and the seat ( $s_{si}$ ):

$$s_{pi} = (x_{p1} - x_{p2})^2 + (y_{p1} - y_{p2})^2$$

$$s_{si} = (x_{s1} - x_{s2})^2 + (y_{s1} - y_{s2})^2.$$

Calculate conversion constants for these dimensions:

$$f_p = \frac{s_{pi}}{\frac{11.96875}{12}}$$

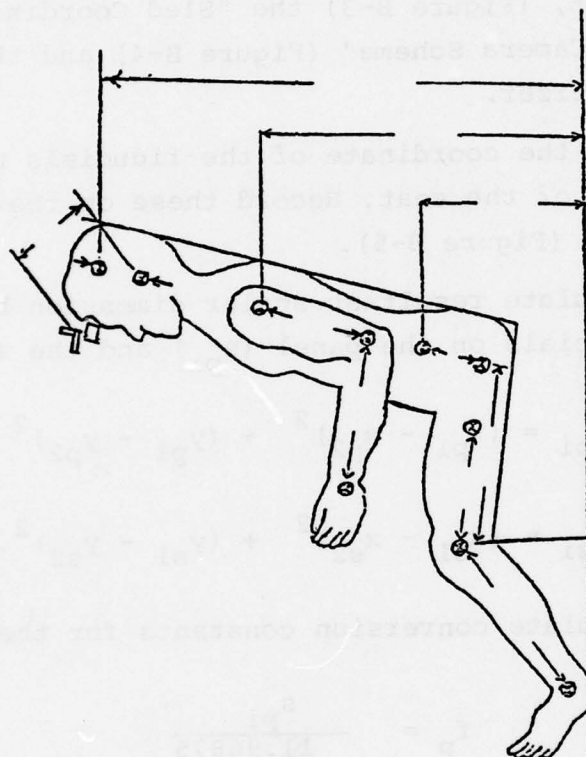
In like manner:

$$f_s = \frac{s_{si}}{\frac{12.0}{12}}$$

Where  $f_p$  and  $f_s$  are conversion constants in terms of counts/foot.

# RESTRAINT SYSTEM DYNAMICS Pretest Dimensions

Run _____	Subject _____	Seat _____	Velocity _____
Date _____	Restraint _____	Seat Back _____	Acceleration _____



WIDTHS:

Jaws	_____
Shoulders	_____
Elbows	_____
Hips	_____
Knees	_____
Ankles	_____

Mid shoulder height \_\_\_\_\_

Figure B-3. Restraint System Dynamics Pretest Anthropometric Measurements Data Form.

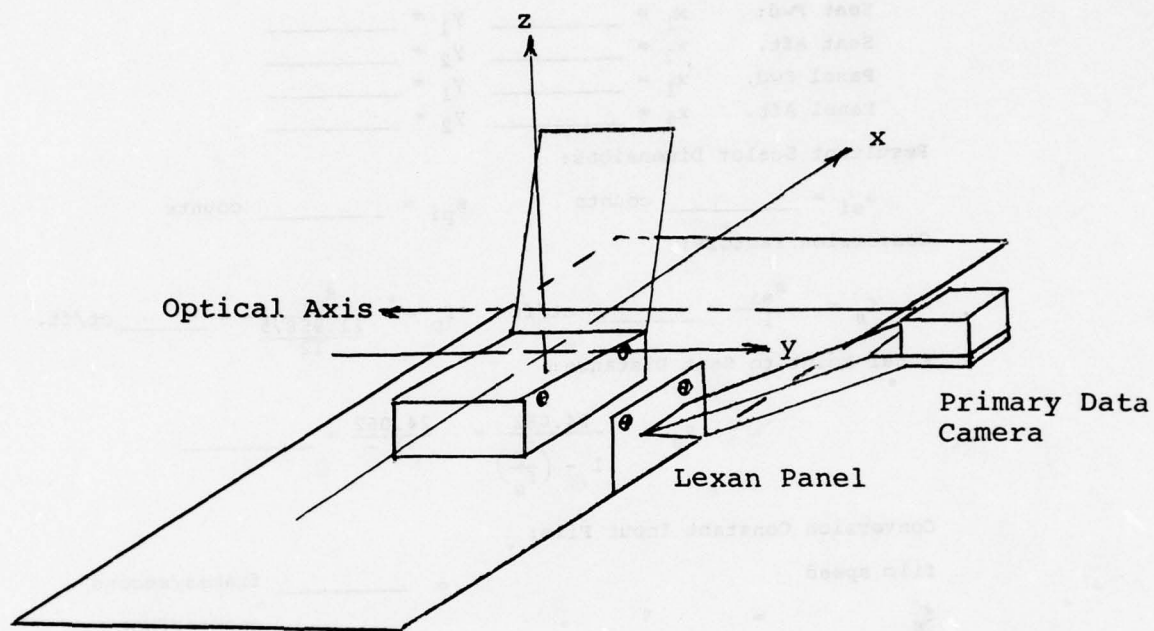


Figure B-4. Sled Coordinate System and Camera Scheme.

RESTRAINT SYSTEM DYNAMICS  
Photometric Calibration Form

TEST \_\_\_\_\_

Fiducial Readings:

Seat Fwd:	$x_1 =$ _____	$y_1 =$ _____
Seat Aft.	$x_2 =$ _____	$y_2 =$ _____
Panel Fwd.	$x_1 =$ _____	$y_1 =$ _____
Panel Aft.	$x_2 =$ _____	$y_2 =$ _____

Resultant Scalar Dimensions:

$s_{si} =$  \_\_\_\_\_ counts       $s_{pi} =$  \_\_\_\_\_ counts

Conversion Factors:

$$f_s = \frac{s_{si}}{1} = \text{_____ ct/ft} \quad f_p = \frac{s_{pi}}{\frac{11.96875}{12}} = \text{_____ ct/ft.}$$

Focal Point to Seat Distance:

$$s_s = \frac{24.062}{1 - \left(\frac{f_p}{f_s}\right)} = \frac{24.062}{1 - \text{_____}} = \text{_____}$$

Conversion Constant Input File:

film speed	=	_____ frames/second
$f_s$	=	_____ counts/foot
$f_{hip}$	=	$\frac{s_s}{s_s + 8 - \text{_____}} \times f_s =$ _____ counts/foot
$f_{knee}$	=	$\frac{s_s}{s_s + 8 - \text{_____}} \times f_s =$ _____ counts/foot
$f_{shoulder}$	=	$\frac{s_s}{s_s + 8 - \text{_____}} \times f_s =$ _____ counts/foot
$f_{elbow}$	=	$\frac{s_s}{s_s + 8 - \text{_____}} \times f_s =$ _____ counts/foot
$f_{jaw}$	=	$\frac{s_s}{s_s + 8 - \text{_____}} \times f_s =$ _____ counts/foot
$f_{accel.}$	=	$\frac{s_s}{s_s + 8 - \text{_____}} \times f_s =$ _____ counts/foot

TEST \_\_\_\_\_

Figure B-5. Photometric Calibration Form.



The distance from the focal point of the camera to the vertical plane of the edge of the seat can now be calculated (Reference Figures B-6 and B-7).

Since the distance from the transparent panel to the seat edge has been measured to be 24.062-inches and the approximate distance from the focal plane of the camera to the seat edge plane was measured to be 60.625-inches then the distance from the focal point of the lens to the lexan panel, the seat edge, and thus the seat  $G_L$  can be calculated by similar triangles (Reference Figure B-7).

$$\frac{s_p}{s_s} = \frac{s_{si} \times f_p}{s_{si} \times f_s} = \frac{f_p}{f_s}$$

Knowing the measured distance  $s_s - s_p$  to be 24.062 inches, thus  $s_p = s_s - 24.062$ , by substituting we have:

$$\frac{s_s - 24.062}{s_s} = \frac{f_p}{f_s}$$

and

$$\frac{1 - 24.062}{s_s} = \frac{f_p}{f_s}$$

By subtracting  $\frac{f_p}{f_s}$  from both terms and adding  $\frac{24.062}{s_s}$  to both terms:

$$1 - \frac{f_p}{f_s} = \frac{24.062}{s_s}$$

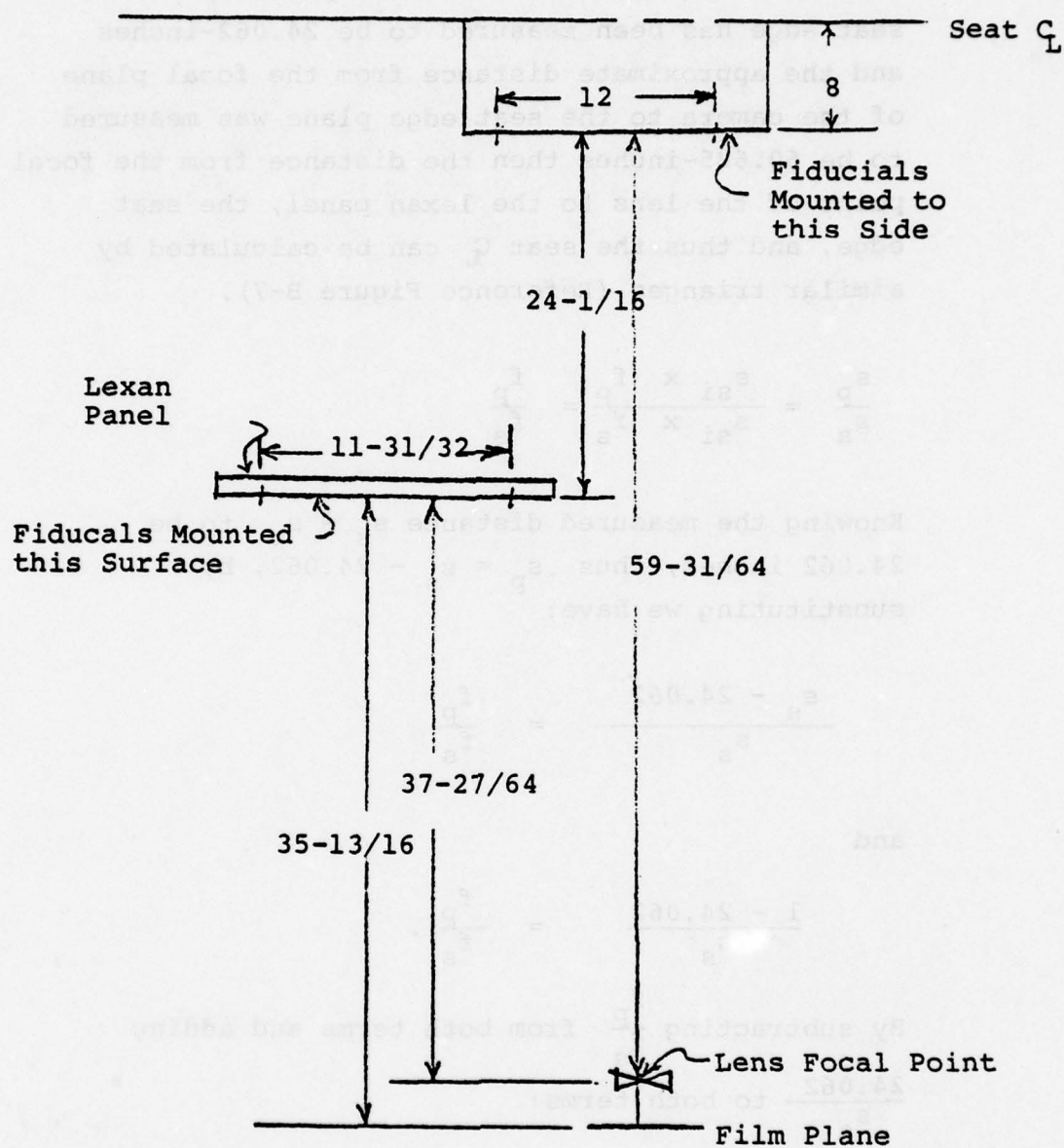


Figure B-6. Schematic of Camera-Reference Fiducials.

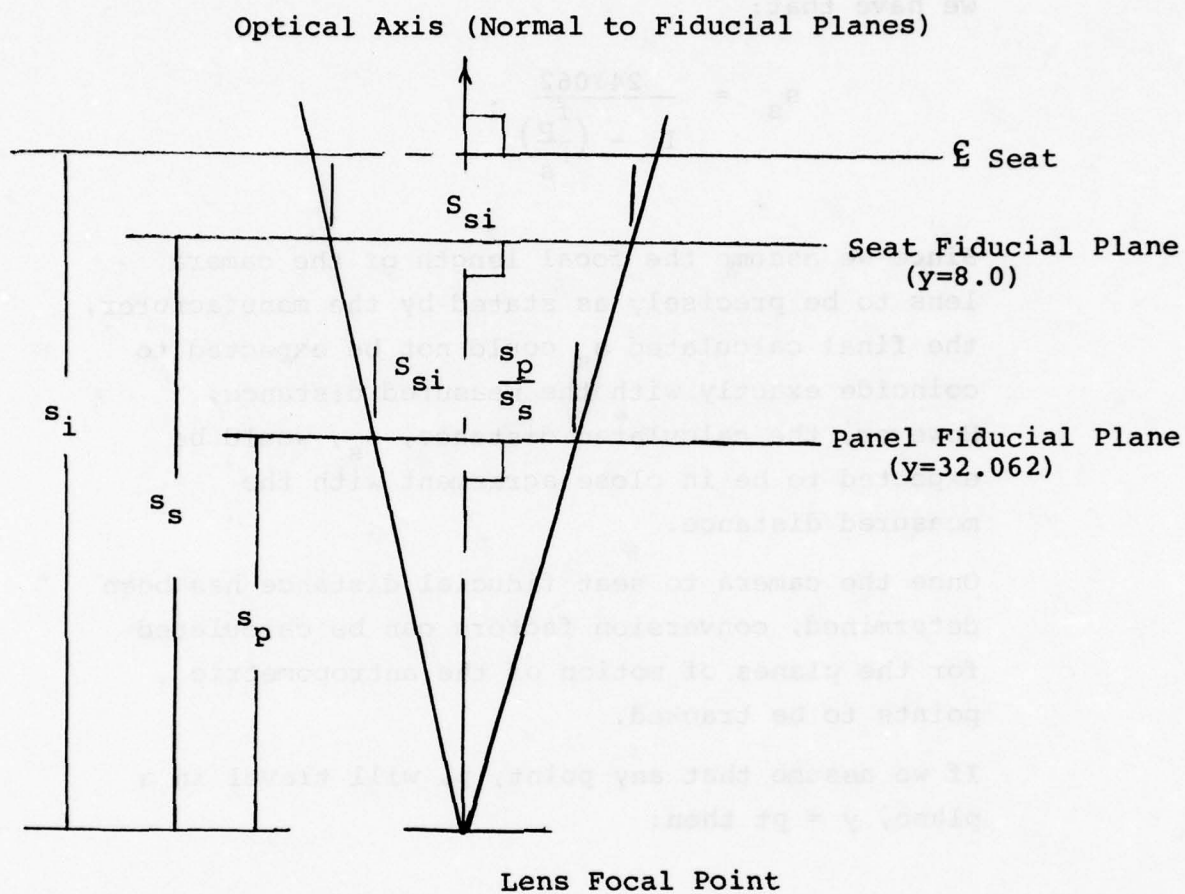


Figure B-7. Photometric Calibration Scheme.

and by multiplying both terms by  $s_s$  and by

$$\frac{1}{1 - \frac{f_p}{f_s}}$$

we have that:

$$s_s = \frac{24.062}{1 - \left(\frac{f_p}{f_s}\right)}.$$

Since we assume the focal length of the camera lens to be precisely as stated by the manufacturer, the final calculated  $s_s$  could not be expected to coincide exactly with the measured distance. However, the calculated distance,  $s_s$ , would be expected to be in close agreement with the measured distance.

Once the camera to seat fiducial distance has been determined, conversion factors can be calculated for the planes of motion of the antropometric points to be tracked.

If we assume that any point,  $p$ , will travel in a plane,  $y = pt$  then:

$$\frac{f_{pt}}{f_s} = \frac{s_{pt}}{s_s}$$

where:  $f_{pt}$  = conversion factor in plane  $y = pt$   
(ft/count)

$f_s$  = conversion factor in plane of seat  
fiducials

$s_{pt}$  = distance along optical axis from  
focal point to the plane  $y = pt$ ,



and:

$s_s$  = distance along optical axis from focal point to the plane of the seat fiducials

$s_{pt}$  is determined by:

$$s_{pt} = s_s + 8 \text{ inches} - \frac{w_p}{2}$$

where  $w_p$  is the width measurement between the anthropometric points on opposite sides of the subject as noted on the pretest anthropometric measurements form, and  $s_s = 8 \text{ inches} = s_Q$  and the subject is assumed to be seated such that his plane of symmetry coincides with the seat  $Q_L$  and that the anthropometric points on the left and right sides of the subject are symmetrical about that plane.

All of the preceding calculations are provided for on the photometric calibration form.

#### 4. Film Digitizing

The anthropometric points are tracked by digitizing the "x" and "y" coordinated of each point as projected from each frame during the impact response period. The film must be mounted in such a manner that the subject appears to face the left as viewed on the projection screen. Because of the smoothing routines utilized in the computer processing of the data, care must be taken to start digitizing the data at least fifteen (15) frames before the subject starts to move relative to the seat and it must be continued at least fifteen (15) frames after the subject returns to rest relative to the seat.

Data points are digitized as follows:

Line 1: Frame Number

- a. Forward seat reference fiducial; x,y
- b. Aft seat reference fiducial; x,y
- c. Hip (or iliac crest) fiducial; x,y
- d. Knee fiducial; x,y

Line 2: Frame Number

- e. Should fiducial; x,y
- f. Elbow fiducial; x,y
- g. Jaw (or accel. pack mount) fiducial; x,y
- h. 9TAP accelerometer reference; x,y

The above data are to be listed on the teletype printer and punched into paper tape on the teletype. Care must be taken to punch a series of rubouts before and after digitizing the data.











C	IF (NP1 .LT. 3) NP1=11	001050
C	IF (NP2 .LT. 3) NP2=11	001060
C		001070
C	TITLE(2) CONTAINS THE TEST NUMBER.	001080
C		001090
	READ(5,1030) TITLE(2), IRX, IPR, ITYPE, IPL, IPA, IPC, JD, JR, M,	001100
	1 (ID(I), IR(I), I=1, M)	001110
	READ(5,1020) DT, (CAL(J), J=2, 8)	001120
	IF (JD .LT. 1) JD=1	001130
	IF (JR .LT. 1) JR=999	001140
	WRITE(6,2500) TITLE, NP	001150
	IF (IRX) 480, 480, 490	001160
	480 IRX=0	001170
	GO TO 495	001180
	490 IRX=1	001190
	495 IF (IPR) 500, 500, 505	001200
	500 IPR=0	001210
	GO TO 510	001220
	505 IPR=1	001230
	510 IF (IPL-1) 515, 525, 520	001240
	515 IPL=0	001250
	GO TO 525	001260
	520 IPL=2	001270
	525 IF (IPA-1) 530, 540, 535	001280
	530 IPA=0	001290
	GO TO 540	001300
	535 IPA=2	001310
	540 IF (IPC-1) 545, 560, 550	001320
	545 IPC=0	001330
	GO TO 560	001340
	550 IPC=2	001350
	560 I=1	001360
	TFLAG=0	001370

```

NC1=1
NC2=999
IFRD=-100
IF (OT) 565,565,570
565 OT=500.0
570 IF (ITYPE) 575,575,580
575 ITYPE=0
J1=3
GO TO 10
580 ITYPE=1
J1=7
585 READ(5,1000) ICD,IFR(I),(X(I,J),Z(I,J),J=1,2),(X(I,J),Z(I,J),J=7,8)
1)
DO 590 J=3,6
X(I,J)=0.0
590 Z(I,J)=0.0
IF (ICD-1) 595,595,100
595 IF (IFR(I)-IFRD) 600,600,610
600 WRITE(6,2410) IFR(I)
IFLAG=1
610 IFRD=IFR(I)
GO TO 40
C
C FROM HERE TO LABEL 115: READ A MAXIMUM OF 'MAXN' FRAMES OF INPUT DATA
C
10 READ(5,1000) ICD,IFR(I),(X(I,J),Z(I,J),J=1,4)
C FOLLOWING CARD CHANGED TO INPUT PAPER TAPE DATA:
IF (ICD-1) 15,15,100
C
IF (ICD-1) 100,15,100
15 IF (IFR(I)-IFRD) 20,20,25
20 WRITE(6,2410) IFR(I)
IFLAG=1
25 READ(5,1000) ICD,IFRD,(X(I,J),Z(I,J),J=5,8)

```

```

001380
001390
001400
001410
001420
001430
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001450
001460
001470
001480
001490
001500
001510
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001570
001580
001590
001600
001610
001620
001630
001640
001650
001660
001670
001680
001690
001700

```



```

C FOLLOWING CARD CHANGED TO INPUT PAPER TAPE DATA:
C
  30 IF (ICD-2) 30,30,70
  35 IF (ICD-2) 70,30,70
  30 IF (IFR(I)-IFRD) 35,40,35
  35 WRITE(6,2400) IFR(I),IFRD
  IFLAG=1
  40 T(I)=FLOAT(IFR(I))/DT
  IF (IFR(I) .EQ. JD) NC1=I
  IF (IFR(I) .EQ. JR) NC2=I
  IF (I-MAXN) 50,50,60
  50 I=I+1
  IF (ITYPE) 10,10,585
  60 WRITE(6,2840) MAXN,IFR(I)
  IF (ITYPE) 10,10,585
  70 WRITE(6,2000) ICD,IFRD
  IFLAG=1
  GO TO 10
  100 IF (ICD-9) 110,115,110
  110 WRITE(6,2000) ICD,IFR(I)
  IFLAG=1
  IF (ITYPE) 10,10,585
  115 N=I-1
  DTI=(T(N)-T(1))/FLOAT(N-1)
  IF (IRX) 118,118,116
  116 DO 117 I=1,N
  DO 117 J=1,8
  117 X(I,J)=-X(I,J)
C
C PRINT TEST PARAMETER SUMMARY PAGE.
C
  118 WRITE(6,2100) (I,I=1,M)
  WRITE(6,2110) TITLE(2),N,DT,IRX,ITYPE,IPR,IPL,IPA,IPC,M,
  1 (ID(I),IR(I),I=1,M)
001710
001720
001730
001740
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001760
001770
001780
001790
001800
001810
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001830
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001950
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001970
001980
001990
002000
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002020
002030

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002040  
002050  
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002100  
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002120  
002130  
002140  
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002200  
002210  
002220  
002230  
002240  
002250  
002260  
002270  
002280  
002290  
002300  
002310  
002320  
002330  
002340  
002350  
002360

```

WRITE(6,2120) (HEADL(I),I=2,8)
WRITE(6,2130) (CAL(I),I=2,8)
WRITE(6,2140) OTT
WRITE(6,2150) N
WRITE(6,2155) YNPL(2-IRX)
WRITE(6,2160) YNPR(IPR+1)
WRITE(6,2190) YNPR(IPL+1),YNPL(IPL+1)
WRITE(6,2180) YNPR(IPA+1),YNPL(IPA+1)
WRITE(6,2170) YNPR(IPC+1),YNPL(IPC+1)
DO 130 J=2,8
IF (ABS(CAL(J))) 120,125,120
120 CAL(J)=1.0/CAL(J)
ICAL(J)=1
GO TO 130
125 ICAL(J)=0
WRITE(6,2820) HEADL(J)
130 CONTINUE
WRITE(6,2570)
IF (M) 137,137,132
132 DO 135 K=1,M
JD=ID(K)
JR=IR(K)
IF (ICAL(JD) .LT. 1 .OR. ICAL(JR) .LT. 1) GO TO 135
WRITE(6,2210) K,HEADL(JD),HEADL(JR)
135 CONTINUE
137 IF (IPR) 140,140,165
C
C PRINT RAW INPUT DATA IN COUNTS.
C
140 WRITE(6,2500) TITLE,NP
WRITE(6,2550)
WRITE(6,2560) HEADC
DO 145 I=1,N

```

```

145 WRITE(6,2580) IFR(I),(X(I,J),Z(I,J),J=1,8)
    WRITE(6,2500) TITLE,NP
    WRITE(6,2552)
    WRITE(6,2560) HEADC
C
C COMPUTE AND PRINT FRAME TO FRAME DIFFERENCES IN COUNTS
C
    IF (ITYPE) 148,148,146
146 DO 147 J=3,6
    XD(J)=0.0
147 XD(J)=0.0
148 DO 160 I=2,N
    XD(1)=X(I,1)-X(I-1,1)
    ZD(1)=Z(I,1)-Z(I-1,1)
    XD(2)=X(I,2)-X(I-1,2)-XD(1)
    ZD(2)=Z(I,2)-Z(I-1,2)-ZD(1)
    DO 150 J=J1,8
    XD(J)=X(I,J)-X(I-1,J)-XD(1)
    ZD(J)=Z(I,J)-Z(I-1,J)-ZD(1)
150 WRITE(6,2580) IFR(I),(XD(J),ZD(J),J=1,8)
160 CONTINUE
C CONVERT DATA FROM COUNTS TO FEET.
165 IF (IFLAG) 170,170,167
167 WRITE(6,2500) TITLE,NP
    WRITE(6,2830)
    GO TO 5
170 DO 185 I=1,N
C
C H1 AND H2 ADJUST DATA FOR SHIFT IN RANGE REFERENCE READING.
C
    H1=X(I,1)-X(1,1)
    H2=Z(I,1)-Z(1,1)
    X(I,2)=(X(I,2)-H1)*CAL(2)

```

```

002700      Z(I,2)=(Z(I,2)-H2)*CAL(2)
002710      DO 180 J=J1,8
002720      X(I,J)=(X(I,J)-H1)*CAL(J)
002730      180 Z(I,J)=(Z(I,J)-H2)*CAL(J)
002740      185 CONTINUE
002750      C      DO 800 NP=NP1,NP2,2
002760          N1=(NP-1)/2+1
002770          N2=N-N1+1
002780          N3=3*N1-2
002790          N4=N-N3+1
002800          NN=N2-N1+1
002810          IF (IPC+IPA-4) 700,800,800
002820
002830      C***** COMPUTE PARAMETER VERSUS SLED DISPLACEMENTS.
002840      C
002850      700 DO 725 J=3,8
002860          JJ=J-2
002870          IF (ICAL(J)) 715,715,705
002880      705 DO 710 I=1,N
002890          XD(I)=X(I,J)-X(I,2)
002900      710 ZD(I)=Z(I,J)-Z(I,2)
002910          I=1
002920          CALL SM(I,XD,XX(I,JJ),N,NP)
002930          CALL SM(I,ZD,ZZ(I,JJ),N,NP)
002940          GO TO 725
002950      715 DO 720 I=N1,N2
002960          XX(I,JJ)=0.0
002970      720 ZZ(I,JJ)=0.0
002980      725 CONTINUE
002990          IF (IPC-1) 728,728,743
003000      728 LINE=60
003010          DO 740 I=N1,N2
003020          IF (LINE-50) 735,730,730

```



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003100
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003120
003130
003140
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003190
003200
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003230
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003250
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003280
003290
003300
003310
003320
003330
003340
003350

730 WRITE(6,2500) TITLE,NP
    WRITE(6,2555)
    WRITE(6,2565) (HEADC(J),J=3,8)
    LINE=J
C PRINT PARAMETER VERSUS SLED DATA.
735 WRITE(6,2585) IFR(I),T(I),(XX(I,JJ),ZZ(I,JJ),JJ=1,6)
    LINE=LINE+1
740 CONTINUE
    IF (IPC) 742,742,743
742 IF (NC1.LT. N1) NC1=N1
    IF (NC2.GT. N2) NC2=N2
    NN=NC2-NC1+1
    IP=1
C PLOT PARAMETER VERSUS SLED DATA.
    CALL CPLT(T,DI,DC,IP)
    WRITE(6,2595) IFR(NC1),IFR(NC2)
743 IF (IPA-2) 745,800,800
C*****
C COMPUTE ANGULAR VELOCITY AND ACCELERATION; HERE TO LABER 775.
C*****
745 XD(N1-1)=PI
    ZD(N1-1)=PI
    IF (ICAL(3)+ICAL(5)-2) 756,750,750
750 DO 755 I=N1,N2
    H1=ZZ(I,3)-ZZ(I,1)
    H2=XX(I,3)-XX(I,1)
    C SHOULDER - HIP ANGLE
    XD(I)=ATAN2(H1,H2)
    IF (XD(I).LT. 0.0) XD(I)=XD(I)+PI2
    IF (ABS(XD(I)-XD(I-1)).GT. PI34) XD(I)=XD(I)+PI2
755 CONTINUE
    CALL DERIV1(T,XD,WS,N,NP,1)
    CALL DERIV1(T,WS,WS2,N,NP,2)

```

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003360
003370
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003540
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003560
003570
003580
003590
003600
003610
003620
003630
003640
003650
003660
003670
003680

GO TO 758
756 DO 757 I=N1,N2
    XD(I)=0.0
    WS(I)=0.0
757 WS2(I)=0.0
758 IF (ICAL(7)+ICAL(8)-2) 762,759,759
759 DO 760 I=N1,N2
    H1=ZZ(I,5)-ZZ(I,6)
    H2=XX(I,5)-XX(I,6)
    C HEAD PACK - SNOUT ANGLE
    ZD(I)=ATAN2(H1,H2)
    IF (ZD(I) .LT. 0.0) ZD(I)=ZD(I)+PI2
    IF (ABS(ZD(I)-ZD(I-1)) .GT. PI34) ZD(I)=ZD(I)+PI2
760 CONTINUE
    CALL DERIV1(T,ZD,WH,N,NP,1)
    CALL DERIV1(T,WH,WH2,N,NP,2)
    GO TO 768
762 DO 764 I=N1,N2
    ZD(I)=0.0
    WH(I)=0.0
764 WH2(I)=0.0
768 LINE=60
    DO 775 I=N3,N4
    IF (LINE-50) 772,770,770
770 WRITE(6,2500) TITLE,NP
    WRITE(6,2551)
    WRITE(6,2520)
    LINE = 0
    C PRINT ANGULAR VELOCITY AND ACCELERATION.
772 WRITE(6,2590) IFR(I),T(I),XD(I),WS(I),WS2(I),ZD(I),WH(I),WH2(I)
    LINE=LINE+1
775 CONTINUE
    IF (IPA) 780,780,800

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```

780 IP=2
NN=N4-N3+1
JD=5
JR=3
IF (ICAL(3)+ICAL(5)-2) 790,785,785
C PLOT ANGULAR VELOCITY AND ACCELERATION DATA.
785 CALL CPLT(T(N3),WS(N3),WS2(N3),IP)
790 JD=7
JR=8
IF (ICAL(7)+ICAL(8)-2) 800,795,795
795 CALL CPLT(T(N3),WH(N3),WH2(N3),IP)
800 CONTINUE
IF (M.LT. 1 .OR. IPL .EQ. 2) GO TO 5
DO 200 J=2,8
IF (ICAL(J)) 200,200,190
190 DO 195 I=2,N
X(I,J)=X(I,J)-X(1,J)
195 Z(I,J)=Z(I,J)-Z(1,J)
X(1,J)=0.0
Z(1,J)=0.0
200 CONTINUE
IP=3
C 202 DO 410 NP=NP1,NP2,2
C N1=(NP-1)/2+1
C N2=N-N1+1
C N3=3*N1-2
C N4=N-N3+1
C NN=N4-N3+1
C *****
C COMPUTE LINEAR VELOCITY AND ACCEL DATA FOR PARAMETER ID(K) WITH
C RESPECT TO IR(K); HERE TO LABEL 400.
C *****

```

```

C
00 400 K=1,M
JD=ID(K)
IF (JD .LE. 1) GO TO 390
JR=IR(K)
IF (JR .LT. 1) GO TO 395
IF (ICAL(JD) .LT. 1 .OR. ICAL(JR) .LT. 1) GO TO 400
XMP=C1
ZMP=C1
RM= C1
XMN=-C1
ZMN=-C1
DO 212 I=1,N
IF (JR-1) 205,205,210
205 OI(I)=X(I,JD)
DC(I)=Z(I,JD)
GO TO 212
210 OI(I)=X(I,JD)-X(I,JR)
DC(I)=Z(I,JD)-Z(I,JR)
212 CONTINUE
CALL SM(T,DI,XD,N,NP)
CALL SM(T,DC,ZD,N,NP)
C
C COMPUTE MAXIMUM X, Z AND RESULTANT DISPLACEMENT.
C
DO 260 I=N1,N2
RES(I)=SQRT(XD(I)*XD(I)+ZD(I)*ZD(I))
IF (XD(I)-XMP) 220,220,215
215 XMP=XD(I)
TXMP=T(I)
GO TO 230
220 IF (XD(I)-XMN) 225,230,230
225 XMN=XD(I)

```

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004020
004030
004040
004050
004060
004070
004080
004090
004100
004110
004120
004130
004140
004150
004160
004170
004180
004190
004200
004210
004220
004230
004240
004250
004260
004270
004280
004290
004300
004310
004320
004330
004340

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```

TXMN=T(I)
230 IF (ZD(I)-ZMP) 240,240,235
235 ZMP=ZD(I)
TZMP=T(I)
GO TO 250
240 IF (ZD(I)-ZMN) 245,245,250
245 ZMN=ZD(I)
TZMN=T(I)
250 IF (RES(I)-RM) 260,260,255
255 RM=RES(I)
TRM= T(I)
260 CONTINUE
C COMPUTE LINEAR VELOCITY.
CALL DERIV1(T,RES,VEL,N,NP,1)
C COMPUTE LINEAR ACCELERATION DATA.
CALL DERIV1(T,VEL,ACC,N,NP,2)
LINE=60
DO 280 I=N3,N4
IF (LINE-50) 275,270,270
270 WRITE(6,2500) TITLE,NP
WRITE(6,2200) HEADR(JD),HEADL(JR)
WRITE(6,2510)
LINE= J
C PRINT LINEAR DISPL, VEL AND ACCEL DATA.
275 ACCG(I)=ACC(I)/32.2
WRITE(6,2600) IFR(I),T(I),XD(I),ZD(I),RES(I),VEL(I),ACCG(I)
LINE=LINE+1
280 CONTINUE
IF (LINE-40) 330,330,320
320 WRITE(6,2500) TITLE,NP
330 WRITE(6,2200) HEADR(JD),HEADL(JR)
WRITE(6,2700) XMP,TXMP
WRITE(6,2710) XMN,TXMN

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```

WRITE(6,2720)ZMP,TZMP
WRITE(6,2730) ZMN,TZMN
WRITE(6,2740) RM,TRM
004680
004690
004700
004710
004720
004730
004740
004750
004760
004770
004780
004790
004800
004810
004820
004830
004840
004850
004860
004870
004880
004890
004900
004910
004920
004930
004940
004950
004960
004970
004980
004990
005000

C
C PLOT LINEAR VELOCITY AND ACCELERATION DATA.
C
350 IF (IPL) 360,360,400
360 CALL CPLT(T(N3),VEL(N3),ACCG(N3),IP)
GO TO 400
390 WRITE(6,2500) TITLE,NP
WRITE(6,2800) K
GO TO 400
395 WRITE(6,2500) TITLE,NP
WRITE(6,2810) K
400 CONTINUE
C 410 CONTINUE
GO TO 5
999 WRITE(6,2900)
CALL PLOTE
STOP

C FOLLOWING CARD CHANGED TO INPUT PAPER TAPE DATA:
1000 FORMAT(I1,I4,8F7.0)
C1000 FORMAT(I1,I5,8F6.0)
1010 FORMAT(8A10)
1020 FORMAT(8F10.0)
1030 FORMAT(A5,4I1,2I2,2I3,I2,12(I2,I1))
2000 FORMAT(/ 4X,*ERROR IN CARD IDENTIFICATION NUMBER; CARD ID=*,I2,
1 *; FRAME NUMBER =*,I4)
2100 FORMAT(/ 4X,*TEST N OT IRX ITYPE IPR IPL IPA
1IPC M SETS:*,12I4)
2110 FORMAT( 3X,A5,I6,F10.3,I4,5I6,I5,7X,12(I3,I1))
2120 FORMAT(/ 36X,7(A10,2X))
2130 FORMAT( 4X,*CALIB DATA IN COUNTS PER FOOT:*,F9.3,6F12.3)

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2140 FORMAT(/ 4X, *AVERAGE TIME INCREMENT BETWEEN POINTS:*, F10.5)      005010
2150 FORMAT(/ 4X, *NUMBER OF FRAMES READ: *, I4, * FRAMES*)              005020
2155 FORMAT(/ 4X, *REVERSE POLARITY OF X-AXIS DATA (MULT. BY -1.0): *, A3) 005030
2160 FORMAT(/ 4X, *PRINT LISTING OF INPUT DATA IN COUNTS: *, A3)        005040
2170 FORMAT(/ 4X, *PARAMETERS RELATIVE TO SLED DISPLACEMENTS: PRINT? *, 005050
      1A3, 4X, *PLOT? *, A3) 005060
2180 FORMAT(/ 4X, *ANGULAR VELOCITY AND ACCELERATION DATA: PRINT? *, 005070
      1A3, 4X, *PLOT? *, A3) 005080
2190 FORMAT(/ 4X, *LINEAR VELOCITY AND ACCELERATION DATA: PRINT? *, 005090
      1A3, 4X, *PLOT? *, A3) 005100
2200 FORMAT(/ 31X, A9, * MOTION RELATIVE TO THE *, A9) 005110
2210 FORMAT(/ 10X, I2, *) *, A9, * MOTION RELATIVE TO THE *, A9) 005120
2400 FORMAT(/ 4X, *ERROR IN FRAME NUMBERS; FRAME NUMBER ON CARD 1 = *, I4, 005130
      1 * FRAME NUMBER ON CARD 2 = *, I4) 005140
2410 FORMAT(/ 4X, *FRAME NUMBER IS NOT INCREASING; CHECK FRAME COUNT FOR 005150
      1 CARD 1, FRAME= *, I5) 005160
2500 FORMAT(1H1, 3X, *DATE: *, A10, 20X, *TEST NUMBER: *, A5/ 005170
      1/ 4X, 8A10, 5X, I2, * POINT QUADRATIC FIT*) 005180
2510 FORMAT(/ 32X, *DISPLACEMENT*, 15X, *VELOCITY *, 2(5X, *ACCELERATION*)/ 005190
      A 4X, *FRAME*, 005200
      1 4X, *TIME*, 8X, *X*, 10X, *Z *, 2(5X, *RESULTANT*), 2(8X, *RESULTANT*)/ 005210
      B 4X, * NO. *, 005220
      2 4X, *(SEC)*, 2(5X, *(FEET)*), 6X, *(FEET)*, 7X, *(FT/SEC)*, 7X, *(FT/SEC 005230
      3SQ)*, 10X, *(G)*) 005240
2520 FORMAT(/ 29X, *SHOULDER - HIP*, 23X, *HEAD PACK - SNOOT*/ 005250
      1 * FRAME TIME*, 2( 7X, *THETA*, 8X, *W*, 10X, *W-ACC*, 4X)/ 005260
      2 * NO. (SEC)*, 2(4X, *(RAD/SEC) (RAD/SEC SQ) *) 005270
2550 FORMAT(/ 4X, *THE FOLLOWING IS A LISTING OF THE INPUT DATA IN COUNT 005280
      1S:*) 005290
2551 FORMAT(/ 4X, *THE FOLLOWING IS A LISTING OF THE ANGULAR MOTION OF T 005300
      1HE HEAD AND SHOULDER:*) 005310
2552 FORMAT(/ 4X, *THE FOLLOWING IS A LISTING OF D(I)-DR(I)-D(I-1)+DR(I- 005320
      11) IN COUNTS:*) 005330

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2555 FORMAT(//4X,*THE FOLLOWING IS A LISTING OF PARAMETER - SLED DISPLA005340
      ICEMENT IN FEET:*) 005350
2560 FORMAT(// * FRAME *, 8(6X,A10)/ 2X,*NO.*, 8(8X,*X*,6X,*Z*)) 005360
2565 FORMAT(// * FRAME TIME *,6( 7X,A10)/ 005370
      1 * NO. (SEC)*, 6( 7X,*X*,6X,*Z *)) 005380
2570 FORMAT(//4X,*LINEAR DISPLACEMENT, VELOCITY AND ACCELERATION DATA M005390
      WILL BE COMPUTED FOR THE FOLLOWING:*) 005400
2580 FORMAT(1X,I4,2X,8(F9.0,F7.0)) 005410
2585 FORMAT(1X,I4,F11.5,6(F10.3,F7.3)) 005420
2590 FORMAT(1X,I4,F11.5,2(F10.3,F11.3,F13.3,6X)) 005430
2595 FORMAT(//4X,*THE ABOVE DATA WAS PLOTTED (X VERSUS Z) FOR FRAME NUM005440
      1BER*,I4,* TO FRAME NUMBER*,I4) 005450
2600 FORMAT(4X,I4, F11.5,F10.3,F11.3,F12.3,F15.3,F16.3,F17.3) 005460
2700 FORMAT(/ 4X,*MAXIMUM POSITIVE X DISPLACEMENT=*,F8.3, * AT TIME *005470
      1, F8.5) 005480
2710 FORMAT(/ 4X,*MAXIMUM NEGATIVE X DISPLACEMENT=*,F8.3, * AT TIME *005490
      1, F8.5) 005500
2720 FORMAT(/ 4X,*MAXIMUM POSITIVE Z DISPLACEMENT=*,F8.3, * AT TIME *005510
      1, F8.5) 005520
2730 FORMAT(/ 4X,*MAXIMUM NEGATIVE Z DISPLACEMENT=*,F8.3, * AT TIME *005530
      1, F8.5) 005540
2740 FORMAT(/ 4X,*MAXIMUM RESULTANT DISPLACEMENT=*,F8.3, * AT TIME *005550
      1, F8.5) 005560
2800 FORMAT(//4X, *OMIT COMPUTATIONS FOR SET*,I3/ 4X,*THE PROGRAM IS005570
      1 NOT DESIGNED TO COMPUTE RANGE DISPLACEMENT, VELOCITY AND ACCELE005580
      2TION.*/ 4X,*DATA PARAMETER CODE IS LESS THAN OR EQUAL TO 1*) 005590
2810 FORMAT(//4X, *OMIT COMPUTATIONS FOR SET*,I3/ 005600
      1 4X,*REFERENCE PARAMETER CODE IS LESS THAN 1*) 005610
2820 FORMAT(/ 4X,*CALIBRATION FACTOR IS 0.0 THUS COMPUTATIONS WILL BE 005620
      1MITTED FOR THE FOLLOWING PARAMETER: *,A10) 005630
2830 FORMAT(//1X,134(1H*))//4X, *OMIT THE REMAINDER OF THE COMPUTATIONS005640
      1 FOR THIS TEST BECAUSE OF INPUT CARD PROBLEMS.*/ 005650
      2 4X,*SEE ERROR STATEMENTS AT THE BEGINNING OF THE OUTPUT FOR THIS 005660

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3TEST1*// 1X,134(1H*))                                005670
2840 FORMAT(/4X,*NUMBER OF FRAMES IS >*,I4,*;  OMIT DATA FOR FRAME NUMB 005680
1ER*,I4)                                                005690
2900 FORMAT(*1  END OF JOB*)                            005700
END                                                    005710
SUBROUTINE CPLT(T,Y,Z,IP)                               005720
DIMENSION X(302),T(1),Y(1),Z(1)                      005730
COMMON  JD,JR,  N,NP,I1,I2,XX(302,6),ZZ(302,6),ICAL(8) 005740
COMMON /CPLTC/ HEADL(8),DATE,TEST,TITLE(8),IRX       005750
C IP=1 --- COMPOSITE PLOT OF PARAMETER VERSUS SLED DATA 005760
C IP=2 --- PLOT OF ANGULAR VEL AND ACCEL                005770
C IP=3 --- PLOT OF VEL AND ACCEL                       005780
C Sxmax IS THE MAXIMUM LENGTH OF THE TIME SCALE IN INCHES. 005790
Sxmax=32.0                                             005800
SY=10.0                                              005810
DX=0.02                                              005820
N1=N+1                                              005830
N2=N+2                                              005840
IF (IP-2) 300,5,5                                     005850
5 DO 10 J=1,N                                         005860
10 X(J)=T(J)                                          005870
X(N1)=FLOAT(IFIX(X(1)*100.01))*0.01                005880
X(N2)=DX                                              005890
SX=  FLOAT(IFIX((X(N)-X(N1))/DX)+1)                 005900
IF (SX .GT. Sxmax) SX= Sxmax                         005910
CALL AXIS(0.0,0.0,0.0,12,TIME IN SEC.,-12,SX,0.0,X(N1),DX) 005920
IF (IP .EQ. 2) GO TO 400                             005930
AMX=-1.0E10                                          005940
AMN= 1.0E10                                          005950
DO 15 J=1,N                                          005960
AMX=AMAX1(AMX,Y(J))                                  005970
AMN=AMAX1(AMX,Z(J))                                  005980
AMN=AMIN1(AMN,Y(J))                                  005990

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      AMN=AMIN1(AMN,Z(J))
15  CONTINUE
      IF (AMN) 30,20,20
20  AMN=0.0
      GO TO 40
30  AMN=FLOAT(IFIX(AMN/10.0)-1)*10.0
40  AMX=FLOAT(IFIX(AMX/10.0)+1)*10.0
      OYY=(AMX-AMN)/SY
      IF (OYY-10.0) 50,50,60
50  OY=10.0
      YMIN=AMN
      GO TO 100
60  IF (OYY-20.0) 70,70,80
70  OY=20.0
      GO TO 90
80  OY=30.0
90  YMIN=FLOAT(IFIX(AMN/OY))*OY
      IF (YMIN.GT. AMN) YMIN=YMIN-OY
100 YMAX=SY*OY+YMIN
      IF (AMX.GT. YMAX) YMIN=YMIN+OY
      Y(N1)=YMIN
      Z(N1)=OY
      Y(N2)=OY
      Z(N2)=OY
      CALL AXIS(0.0,0.0,26HVEL IN FT/SEC --- ACC IN G,26,SY,90.,YMIN,OY)
      IF (YMIN) 105,110,110
105 Y0=ABS(YMIN/OY)
      CALL PLOT(0.0,Y0,3)
      CALL PLOT(SX,Y0,2)
110 DO 120 I=1,N
      IF (Y(I).GT. YMAX) Y(I)=YMAX
      IF (Z(I).GT. YMAX) Z(I)=YMAX
      IF (Y(I).LT. YMIN) Y(I)=YMIN

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006010
006020
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006100
006110
006120
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006160
006170
006180
006190
006200
006210
006220
006230
006240
006250
006260
006270
006280
006290
006300
006310
006320

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      IF (Z(I) .LT. YMIN) Z(I)=YMIN
120  CONTINUE
130  CALL LINE(X,Y,N,1,10,1)
      CALL LINE(X,Z,N,1,10,3)
      H1=HEADL(JD)
      CALL SYMBOL(0.25,9.5,0.105,H1,0.0,9)
      CALL SYMBOL(0.25,9.3,0.105,6HREL TO,0.0,6)
      H1=HEADL(JR)
      CALL SYMBOL(0.25,9.1,0.105,H1,0.0,9)
      J=1
      CALL SYMBOL(0.5, 8.8,0.105,J,0.0,-1)
      CALL SYMBOL(0.65,8.75,0.105,3HVEL,0.0,3)
      J=3
      CALL SYMBOL(0.5, 8.55,0.105,J,0.0,-1)
      CALL SYMBOL(0.65,8.50,0.105,3HACC,0.0,3)
140  CALL SYMBOL(0.25,9.8,0.105,4HTEST,0.0,4)
      CALL SYMBOL(0.75,9.8,0.105,TEST,0.0,5)
      CALL NUMBER(1.75,9.8,0.105,FLOAT(NP),0.0,-1)
      CALL SYMBOL(2.05,9.8,0.105,9HPOINT FIT,0.0,9)
      GO TO 999

C
C  PLOT THE COMPOSITE PLOT OF PARAMETERS VERSUS SLED.
C  NOTE:  ORDINATE AND ABSCISSA SCALING IS FIXED.
C
300  ZMIN=0.0
      XMIN=-1.4-2.2*FLOAT(IRX)
      XMIN=-1.0
      DZ=0.4
      DX=0.4
      SX=10.0
      CALL AXIS(0.0,0.0,14HX DISP IN FEET,-14,SX,0.0,XMIN,DX)
      CALL AXIS(0.0,0.0,14HZ DISP IN FEET, 14,SY,90.0,ZMIN,DZ)
      CALL SYMBOL(0.25,9.5,0.105,16HDATA REL TO SLED,0.0,16)

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006330
006340
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006370
006380
006390
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006470
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006500
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006585
006590
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006630
006640

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006650  
006660  
006670  
006680  
006690  
006700  
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006970

```

X(N1)=XMIN
X(N2)=DX
Z(N1)=ZMIN
Z(N2)=DZ
XMAX=SX*DX+XMIN
ZMAX=SY*DZ+ZMIN
Y0=10.0
DO 310 J=1,6
  IF (ICAL(J+2)) 310,310,305
  H1=HEADL(J+2)
  Y0=Y0-0.25
  CALL SYMBOL(-1.75,Y0+0.05,0.105,J,0.0,-1)
  CALL SYMBOL(-1.60,Y0,0.105,H1,0.0,9)
310 CONTINUE
DO 325 J=1,6
  IF (ICAL(J+2)) 325,325,315
  II=0
DO 320 I=I1,I2
  II=II+1
  X(II)=XX(I,J)
  Z(II)=ZZ(I,J)
  IF (X(II) .GT. XMAX) X(II)=XMAX
  IF (X(II) .LT. XMIN) X(II)=XMIN
  IF (Z(II) .GT. ZMAX) Z(II)=ZMAX
  IF (Z(II) .LT. ZMIN) Z(II)=ZMIN
320 CONTINUE
  CALL LINE(X,Z,N,1,-1,J)
325 CONTINUE
  GO TO 140
C
C C SETUP AND PLOT ANGULAR VEL AND ACCEL.
C
C 400 CALL SCALE(Y,SY,N,1)

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006980 CALL SCALE(Z,SY,N,1)
006990 YMIN=Y(N1)
007000 ZMIN=Z(N1)
007010 DY= Y(N2)
007020 DZ= Z(N2)
007030 WRITE(6,2000) YMIN,DY,ZMIN,DZ
007040 CALL AXIS(0.0,0.0,22HANGULAR VEL -- RAD/SEC, 22,SY,90.,YMIN,DY)
007050 CALL AXIS(SX,0.0,26HANGULAR ACC -- RAD/SEC/SEC,-26,SY,90.,ZMIN,DZ)
007060 GO TO 130
007070 999 CALL PLOT(SX+3.0,0.0,-3)
007080 RETURN
007090 2000 FORMAT(/'4X,*THE ABOVE VEL AND ACCEL DATA ARE PLOTTED; YMIN=*,
007100 1F10.2,* DY=*,F8.2 ,5X,* ZMIN=*,F10.2,* DZ=*,F8.2)
007110 END
007120 SUBROUTINE SM(X,Y,YC,N,NP)
007130 NP MUST BE AN ODD INTEGER .GE. 3.
007140 C COMPUTE THE COEFFICIENTS FOR A QUADRATIC LEAST SQUARES FIT OF 'NP'
007150 C POINTS AND COMPUTE THE FIT OF THE DATA (NO DERIVATIVES) 'YC(I)'.
007160 C DIMENSION C(3),X(1),Y(1),YC(1)
007170 M=(NP-1)/2
007180 NN=N-M
007190 N1=NN+1
007200 DO 10 I=1,M
007210 10 YC(I)=J.0
007220 DO 20 I=N1,N
007230 20 YC(I)=J.0
007240 MM=M+1
007250 DO 100 I=MM,NN
007260 N1=I-M
007270 N2=I+M
007280 CALL QLSQ(X,Y,N1,N2,C)
007290 YC(I)=C(1)*X(I)*X(I)+C(2)*X(I)+C(3)
007300 YP(I)=2.0*C(1)*X(I)+C(2)
C

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C      YPP(I)=2.0*C(1)
100 CONTINUE
      RETURN
      END
      SUBROUTINE DERIV1(X,Y,YP,N,NP,IO)
C      NP MUST BE AN ODD INTEGER .GE. 3.
C      ID=1 FOR FIRST DERIVATIVE.
C      ID=2 FOR SECOND DERIVATIVE.
C      COMPUTE THE COEFFICIENTS FOR A QUADRATIC LEAST SQUARES FIT OF 'NP'
C      POINTS AND COMPUTE THE FIRST DERIVATIVE 'YP(I)'.
      DIMENSION C(3),X(1),Y(1),YP(1)
      M=(NP-1)/2
      K=M+M*IO
      NN=N-K
      N1=NN+1
      DO 10 I=1,K
10      YP(I)=0.0
      DO 20 I=N1,N
20      YP(I)=0.0
      MM=K+1
      DO 100 I=MM,NN
      N1=I-M
      N2=I+M
      CALL QLSQ(X,Y,N1,N2,C)
      YP(I)=2.0*C(1)*X(I)+C(2)
      YC(I)=C(1)*X(I)+C(2)*X(I)+C(3)
      YPP(I)=2.0*C(1)
100 CONTINUE
      RETURN
      END
      SUBROUTINE QLSQ(X,Y,N1,N2,C)
      DIMENSION X(1),Y(1),C(1)

```

```

C THIS SUBROUTINE COMPUTES THE QUADRATIC LEAST SQUARE COEFFICIENTS
C 'C(3)' FOR NP DATA POINTS (NP MUST BE AN ODD INTEGER .GE. 3).
C THE DATA NEED NOT BE EQUALLY SPACED.
C C(1)*(X**2)+C(2)*X+C(3)=Y
C C(1)*X+C(2)=Y
C SUBSTITUTE XP=X-FF, WHERE FF IS X((N1+N2)/2)
C THEN C(3)=C(3)+C(1)*FF+FF-C(2)*FF
C C(2)=C(2)-2.0*C(1)*FF
C C(1)=C(1)
C
F(A1,A2,A3,B1,B2,B3,C1,C2,C3)=A1*(B2*C3-B3*C2)+A2*(B3*C1-B1*C3)+A3
1*(B1*C2-B2*C1)
FN=FLOAT(N2-N1+1)
NN=(N1+N2)/2
FF=X(NN)
Z1=0
Z2=0
Z3=0
Z4=0
Z5=0
Z6=0
Z7=0
10 DO 20 I=N1,N2
X2=X(I)-FF
X1=X2*X2
Z1=Z1+X2
Z2=Z2+X1
Z3=Z3+X1*X2
Z4=Z4+X1*X1
Z5=Z5+Y(I)
Z6=Z6+X2*Y(I)
Z7=Z7+X1*Y(I)
20 CONTINUE

```

```

007640
007650
007660
007670
007680
007690
007700
007710
007720
007730
007740
007750
007760
007770
007780
007790
007800
007810
007820
007830
007840
007850
007860
007870
007880
007890
007900
007910
007920
007930
007940
007950
007960

```

```

DEN=F(Z4,Z3,Z2,Z3,Z2,Z1,Z2,Z1,Z2,Z1,FN)
C(1)=F(Z7,Z6,Z5,Z3,Z2,Z1,Z2,Z1,FN)/DEN
C(2)=F(Z4,Z3,Z2,Z7,Z6,Z5,Z2,Z1,FN)/DEN
C(3)=F(Z4,Z3,Z2,Z3,Z2,Z1,Z7,Z6,Z5)/DEN
C(3)=C(3)+C(1)*FF+FF-C(2)*FF
C(2)=C(2)-2.0*C(1)*FF
RETURN
END

```

```

007970
007980
007990
008000
008010
008020
008030
008040

```



APPENDIX D  
TYPICAL LISTINGS AND PLOTS  
GENERATED BY HIFPD

44 POINT QUADRATIC FIT

~~11 POINT QUADRATIC FIT~~

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ELBOW  
1715-113

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10

DATE: 9 JUN 77 TEST NUMBER: 1039

RSD STUDY, SUBJECT C 2, RUN#133, Z5417, NYLON

11 POINT QUADRATIC FIT

THE FOLLOWING IS A LISTING OF THE INPUT DATA IN COUNTS:

FRAME NO.	RANGE			SLED	HIP			KNEE	SHOULDER			ELBOW			HAND PT. 1			HAND PT. 2						
	X	Y	Z		X	Y	Z		X	Y	Z	X	Y	Z	X	Y	Z	X	Y	Z				
0	-154	-2134	-1817	-2357	-1893	-1849	650	-1716	-2689	967	-2519	-919	-2483	1713	-1976	-2483	1713	-1976	-2483	1713	-1976	-2483	1713	-1976
1	-155	-2193	-1819	-2356	-1899	-1849	652	-1712	-2694	963	-2520	-914	-2494	1742	-1966	-2494	1742	-1966	-2494	1742	-1966	-2494	1742	-1966
2	-152	-2192	-1821	-2353	-1892	-1845	648	-1712	-2693	966	-2521	-914	-2497	1712	-1976	-2497	1712	-1976	-2497	1712	-1976	-2497	1712	-1976
3	-162	-2193	-1820	-2374	-1899	-1855	649	-1716	-2694	956	-2518	-923	-2492	1717	-1979	-2492	1717	-1979	-2492	1717	-1979	-2492	1717	-1979
4	-163	-2222	-1814	-2372	-1892	-1853	652	-1716	-2696	956	-2522	-929	-2497	1725	-1978	-2497	1725	-1978	-2497	1725	-1978	-2497	1725	-1978
5	-161	-2203	-1820	-2372	-1900	-1858	657	-1718	-2694	955	-2520	-922	-2495	1723	-1974	-2495	1723	-1974	-2495	1723	-1974	-2495	1723	-1974
6	-155	-2200	-1819	-2371	-1892	-1852	658	-1708	-2691	950	-2511	-922	-2486	1711	-1973	-2486	1711	-1973	-2486	1711	-1973	-2486	1711	-1973
7	-162	-2198	-1820	-2371	-1893	-1850	662	-1715	-2695	960	-2518	-919	-2498	1733	-1980	-2498	1733	-1980	-2498	1733	-1980	-2498	1733	-1980
8	-163	-2193	-1823	-2355	-1896	-1847	663	-1706	-2693	971	-2519	-908	-2504	1717	-1984	-2504	1717	-1984	-2504	1717	-1984	-2504	1717	-1984
9	-156	-2193	-1817	-2357	-1893	-1852	666	-1710	-2688	967	-2513	-913	-2487	1730	-2022	-2487	1730	-2022	-2487	1730	-2022	-2487	1730	-2022
10	-162	-2188	-1823	-2352	-1900	-1845	657	-1702	-2698	974	-2522	-900	-2510	1718	-2006	-2510	1718	-2006	-2510	1718	-2006	-2510	1718	-2006
11	-162	-2196	-1823	-2371	-1898	-1852	659	-1713	-2691	972	-2521	-914	-2495	1742	-2024	-2495	1742	-2024	-2495	1742	-2024	-2495	1742	-2024
12	-159	-2193	-1819	-2353	-1892	-1845	648	-1712	-2693	966	-2521	-914	-2497	1712	-1976	-2497	1712	-1976	-2497	1712	-1976	-2497	1712	-1976
13	-160	-2195	-1820	-2369	-1896	-1854	650	-1713	-2697	953	-2520	-911	-2497	1740	-2027	-2497	1740	-2027	-2497	1740	-2027	-2497	1740	-2027
14	-152	-2206	-1814	-2371	-1891	-1854	662	-1711	-2690	958	-2514	-912	-2486	1736	-2018	-2486	1736	-2018	-2486	1736	-2018	-2486	1736	-2018
15	-158	-2200	-1820	-2372	-1895	-1855	655	-1709	-2689	962	-2515	-917	-2500	1733	-2025	-2500	1733	-2025	-2500	1733	-2025	-2500	1733	-2025
16	-159	-2196	-1819	-2356	-1897	-1850	656	-1708	-2695	965	-2515	-914	-2493	1719	-2020	-2493	1719	-2020	-2493	1719	-2020	-2493	1719	-2020
17	-158	-2194	-1819	-2374	-1898	-1847	655	-1712	-2693	969	-2515	-911	-2500	1741	-2021	-2500	1741	-2021	-2500	1741	-2021	-2500	1741	-2021
18	-159	-2193	-1822	-2350	-1900	-1848	660	-1710	-2694	964	-2519	-907	-2494	1736	-2020	-2494	1736	-2020	-2494	1736	-2020	-2494	1736	-2020
19	-161	-2192	-1819	-2352	-1896	-1848	650	-1708	-2693	966	-2516	-908	-2496	1741	-2022	-2496	1741	-2022	-2496	1741	-2022	-2496	1741	-2022
20	-161	-2193	-1819	-2354	-1892	-1842	660	-1715	-2689	967	-2518	-912	-2496	1739	-2019	-2496	1739	-2019	-2496	1739	-2019	-2496	1739	-2019
21	-157	-2194	-1813	-2357	-1892	-1847	670	-1715	-2683	968	-2510	-908	-2476	1735	-2019	-2476	1735	-2019	-2476	1735	-2019	-2476	1735	-2019
22	-163	-2198	-1823	-2358	-1899	-1851	660	-1711	-2697	963	-2519	-915	-2481	1739	-2027	-2481	1739	-2027	-2481	1739	-2027	-2481	1739	-2027
23	-164	-2202	-1827	-2374	-1897	-1851	660	-1713	-2694	958	-2523	-911	-2491	1732	-2029	-2491	1732	-2029	-2491	1732	-2029	-2491	1732	-2029
24	-163	-2200	-1823	-2373	-1898	-1855	659	-1722	-2697	958	-2523	-914	-2493	1737	-2031	-2493	1737	-2031	-2493	1737	-2031	-2493	1737	-2031
25	-171	-2199	-1831	-2374	-1902	-1854	650	-1712	-2704	962	-2526	-917	-2504	1733	-2042	-2504	1733	-2042	-2504	1733	-2042	-2504	1733	-2042
26	-164	-2204	-1825	-2380	-1899	-1861	662	-1721	-2696	957	-2516	-921	-2485	1734	-2035	-2485	1734	-2035	-2485	1734	-2035	-2485	1734	-2035
27	-156	-2198	-1814	-2377	-1891	-1854	666	-1718	-2692	953	-2513	-922	-2479	1719	-2027	-2479	1719	-2027	-2479	1719	-2027	-2479	1719	-2027
28	-159	-2198	-1819	-2374	-1892	-1847	674	-1718	-2689	951	-2507	-921	-2478	1718	-2024	-2478	1718	-2024	-2478	1718	-2024	-2478	1718	-2024
29	-157	-2204	-1818	-2381	-1887	-1859	670	-1719	-2692	953	-2512	-911	-2496	1724	-2024	-2496	1724	-2024	-2496	1724	-2024	-2496	1724	-2024
30	-150	-2197	-1814	-2376	-1876	-1855	674	-1712	-2682	953	-2500	-914	-2489	1731	-2021	-2489	1731	-2021	-2489	1731	-2021	-2489	1731	-2021
31	-152	-2201	-1813	-2380	-1882	-1861	679	-1711	-2681	948	-2499	-928	-2480	1721	-2023	-2480	1721	-2023	-2480	1721	-2023	-2480	1721	-2023
32	-150	-2207	-1812	-2386	-1871	-1861	682	-1719	-2678	942	-2493	-931	-2482	1715	-2013	-2482	1715	-2013	-2482	1715	-2013	-2482	1715	-2013
33	-167	-2210	-1806	-2389	-1855	-1862	696	-1723	-2668	942	-2482	-934	-2475	1718	-2016	-2475	1718	-2016	-2475	1718	-2016	-2475	1718	-2016
34	-143	-2218	-1805	-2382	-1853	-1863	701	-1728	-2661	938	-2472	-939	-2473	1714	-2007	-2473	1714	-2007	-2473	1714	-2007	-2473	1714	-2007
35	-139	-2212	-1797	-2398	-1840	-1875	720	-1723	-2645	934	-2457	-944	-2469	1735	-1997	-2469	1735	-1997	-2469	1735	-1997	-2469	1735	-1997
36	-140	-2217	-1802	-2401	-1833	-1881	718	-1735	-2640	922	-2449	-954	-2444	1638	-1985	-2444	1638	-1985	-2444	1638	-1985	-2444	1638	-1985
37	-141	-2221	-1800	-2405	-1830	-1898	740	-1730	-2629	919	-2436	-953	-2436	1703	-1982	-2436	1703	-1982	-2436	1703	-1982	-2436	1703	-1982
38	-142	-2221	-1801	-2407	-1832	-1898	743	-1735	-2620	926	-2427	-960	-2432	1696	-1977	-2432	1696	-1977	-2432	1696	-1977	-2432	1696	-1977
39	-146	-2224	-1803	-2401	-1820	-1899	756	-1737	-2603	925	-2412	-951	-2422	1690	-1967	-2422	1690	-1967	-2422	1690	-1967	-2422	1690	-1967
40	-134	-2217	-1794	-2398	-1800	-1878	773	-1736	-2578	927	-2381	-948	-2380	1711	-1942	-2380	1711	-1942	-2380	1711	-1942	-2380	1711	-1942
41	-139	-2217	-1793	-2397	-1791	-1883	776	-1728	-2561	927	-2364	-947	-2374	1711	-1931	-2374	1711	-1931	-2374	1711	-1931	-2374	1711	-1931
42	-126	-2211	-1785	-2391	-1776	-1868	800	-1720	-2531	941	-2332	-945	-2333	1736	-1910	-2333	1736	-1910	-2333	1736	-1910	-2333	1736	-1910
43	-122	-2209	-1785	-2392	-1749	-1873	821	-1711	-2507	941	-2307	-944	-2324	1707	-1865	-2324	1707	-1865	-2324	1707	-1865	-2324	1707	-1865
44	-123	-2216	-1787	-2398	-1744	-1875	832	-1721	-2489	937	-2286	-951	-2315	1633	-1850	-2315	1633	-1850	-2315	1633	-1850	-2315	1633	-1850
45	-128	-2215	-1789	-2399	-1733	-1882	855	-1729	-2466	930	-2261	-952	-2278	1734	-1827	-2278	1734	-1827	-2278	1734	-1827	-2278	1734	-1827
46	-136	-2214	-1735	-2388	-1714	-1874	858	-1728	-2446	932	-2239	-951	-2272	1635	-1804	-2272	1635	-1804	-2272	1635	-1804	-2272	1635	-1804
47	-139	-2212	-1798	-2392	-1706	-1876	881	-1721	-2423	930	-2213	-948	-2252	1636	-1794	-2252	1636	-1794	-2252	1636	-1794	-2252	1636	-1794
48	-140	-2210	-1802	-2390	-1693	-1871	895	-1726	-2399	93														



53	-155	-2201	-1810	-2383	-1633	-1858	978	-1720	-2275	-2014	-930	-2093	1699	-1613	2360
54	-153	-2200	-1812	-2378	-1639	-1856	987	-1720	-2255	-1978	-923	-2057	1731	-1562	2362
55	-162	-2206	-1820	-2379	-1613	-1864	999	-1727	-2235	-1940	-926	-2040	1679	-1530	2362
56	-167	-2199	-1824	-2374	-1604	-1852	1008	-1719	-2233	-1899	-911	-2008	1698	-1492	2361
57	-172	-2197	-1830	-2368	-1598	-1850	1003	-1723	-2214	-1866	-901	-1988	1634	-1673	2359
58	-169	-2194	-1839	-2368	-1588	-1844	1015	-1727	-2199	-1828	-894	-1962	1708	-1449	2369
59	-178	-2209	-1837	-2378	-1590	-1855	1020	-1738	-2171	-1787	-900	-1942	1688	-1396	2337
60	-174	-2214	-1835	-2374	-1576	-1857	1022	-1738	-2158	-1740	-891	-1915	1661	-1460	2315
61	-169	-2203	-1830	-2374	-1564	-1842	1030	-1737	-2155	-1690	-881	-1905	1670	-1320	2317
62	-164	-2193	-1825	-2360	-1561	-1831	1033	-1724	-2133	-1649	-859	-1891	1630	-1197	2304
63	-158	-2187	-1830	-2362	-1559	-1831	1039	-1723	-2133	-1615	-846	-1885	1675	-1277	2294
64	-158	-2201	-1819	-2374	-1563	-1853	1040	-1727	-2117	-1564	-845	-1867	1645	-1272	2294
65	-155	-2208	-1817	-2376	-1552	-1850	1027	-1735	-2146	-1516	-833	-1854	1625	-1230	2224
66	-155	-2204	-1816	-2376	-1557	-1854	1024	-1730	-2154	-1473	-824	-1852	1630	-1212	2203
67	-163	-2199	-1827	-2373	-1569	-1854	1007	-1731	-2152	-1439	-793	-1852	1611	-1186	2163
68	-167	-2189	-1829	-2362	-1580	-1844	994	-1723	-2143	-1398	-759	-1838	1624	-1159	2152
69	-176	-2197	-1838	-2365	-1594	-1849	970	-1729	-2171	-1361	-743	-1838	1630	-1135	2116
70	-181	-2198	-1848	-2360	-1609	-1846	951	-1728	-2148	-1330	-728	-1842	1574	-1112	2071
71	-184	-2200	-1847	-2370	-1618	-1849	942	-1724	-2193	-1297	-699	-1837	1576	-1096	2035
72	-183	-2197	-1847	-2362	-1624	-1848	933	-1726	-2197	-1260	-668	-1840	1561	-1073	1998
73	-182	-2188	-1849	-2362	-1637	-1849	916	-1714	-2203	-1227	-630	-1833	1560	-1086	1852
74	-178	-2189	-1837	-2364	-1635	-1850	914	-1707	-2208	-1192	-605	-1830	1537	-1026	1908
75	-178	-2192	-1837	-2367	-1642	-1850	892	-1709	-2220	-1162	-575	-1830	1521	-1009	1863
76	-176	-2200	-1837	-2372	-1666	-1864	889	-1714	-2220	-1128	-556	-1833	1513	-984	1809
77	-177	-2198	-1836	-2358	-1661	-1852	887	-1698	-2232	-1110	-512	-1831	1506	-1005	1785
78	-180	-2190	-1840	-2360	-1677	-1849	852	-1692	-2241	-1095	-479	-1819	1514	-988	1748
79	-175	-2188	-1839	-2359	-1672	-1851	833	-1693	-2246	-1071	-446	-1812	1499	-964	1712
80	-181	-2190	-1841	-2360	-1686	-1854	819	-1689	-2259	-1064	-431	-1802	1477	-956	1674
81	-173	-2194	-1837	-2371	-1693	-1856	815	-1695	-2264	-1042	-410	-1802	1455	-947	1622
82	-166	-2203	-1828	-2372	-1692	-1863	809	-1695	-2259	-1030	-392	-1779	1446	-926	1579
83	-161	-2198	-1824	-2372	-1695	-1863	803	-1690	-2273	-1022	-375	-1779	1456	-911	1541
84	-155	-2193	-1817	-2368	-1702	-1863	797	-1677	-2277	-1014	-349	-1779	1447	-909	1510
85	-157	-2202	-1819	-2376	-1714	-1872	779	-1675	-2290	-1021	-346	-1772	1453	-908	1505
86	-152	-2196	-1814	-2369	-1722	-1869	767	-1666	-2299	-1022	-331	-1761	1446	-916	1499
87	-149	-2195	-1813	-2374	-1725	-1872	756	-1652	-2305	-1025	-320	-1759	1446	-918	1482
88	-156	-2198	-1818	-2376	-1736	-1872	750	-1648	-2314	-1038	-303	-1749	1434	-917	1472
89	-156	-2193	-1821	-2379	-1742	-1873	735	-1632	-2314	-1047	-290	-1748	1452	-905	1464
90	-159	-2206	-1821	-2384	-1749	-1870	729	-1620	-2317	-1050	-280	-1740	1456	-898	1467
91	-166	-2200	-1829	-2379	-1760	-1871	708	-1619	-2320	-1067	-286	-1733	1459	-897	1467
92	-167	-2205	-1826	-2379	-1762	-1870	703	-1596	-2320	-1073	-289	-1719	1454	-888	1475
93	-164	-2200	-1823	-2371	-1764	-1871	691	-1574	-2319	-1097	-282	-1710	1454	-877	1491
94	-164	-2197	-1820	-2370	-1763	-1860	691	-1561	-2319	-1103	-284	-1702	1479	-870	1496
95	-167	-2199	-1825	-2372	-1768	-1863	674	-1551	-2323	-1123	-273	-1696	1492	-858	1493
96	-159	-2201	-1821	-2374	-1766	-1864	669	-1542	-2318	-1132	-268	-1686	1486	-852	1497
97	-162	-2199	-1826	-2373	-1769	-1856	667	-1535	-2316	-1153	-262	-1683	1509	-840	1521
98	-160	-2190	-1821	-2366	-1765	-1843	659	-1518	-2315	-1163	-251	-1673	1517	-792	1599
99	-158	-2191	-1819	-2365	-1764	-1840	652	-1506	-2309	-1180	-239	-1672	1516	-831	1542
100	-156	-2193	-1819	-2366	-1765	-1836	637	-1501	-2305	-1198	-227	-1650	1514	-812	1562
101	-160	-2195	-1827	-2367	-1771	-1834	646	-1491	-2305	-1226	-216	-1651	1525	-799	1575
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103	-162	-2197	-1826	-2371	-1770	-1828	641	-1477	-2303	-1263	-192	-1638	1539	-790	1633
104	-164	-2192	-1833	-2365	-1778	-1822	624	-1465	-2310	-1291	-180	-1642	1553	-794	1633
105	-170	-2187	-1836	-2360	-1784	-1813	631	-1456	-2312	-1291	-180	-1642	1553	-794	1633
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107	-173	-2192	-1837	-2364	-1789	-1806	628	-1446	-2315	-1320	-159	-1642	1595	-792	1663
108	-172	-2193	-1843	-2367	-1796	-1806	611	-1443	-2314	-1344	-148	-1649	1544	-794	1695
109	-175	-2192	-1841	-2367	-1794	-1806	614	-1432	-2312	-1359	-141	-1644	1591	-792	1703
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111	-180	-2200	-1845	-2373	-1802	-1796	600	-1421	-2319	-1391	-117	-1645	1534	-805	1728
112	-180	-2193	-1845	-2372	-1812	-1827	588	-1416	-2318	-1408	-103	-1652	1538	-805	1747
113	-181	-2195	-1845	-2369	-1814	-1795	594	-1410	-2325	-1420	-100	-1653	1599	-807	1775
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117	-181	-2193	-1847	-2372	-1835	-1783	582	-1386	-2353	-1461	-85	-1673	1620	-829	1834
118	-181	-2191	-1846	-2370	-1830	-1783	574	-1377	-2362	-1464	-84	-1676	1625	-843	1843



119	-180	-2198	-1846	-2377	-1842	-1788	567	-1374	-2357	1189	-1471	-285	-1680	1631	-848	1858
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121	-171	-2184	-1839	-2375	-1846	-1786	577	-1359	-2370	1182	-1479	-282	-1679	1637	-870	1866
122	-169	-2205	-1834	-2378	-1843	-1783	572	-1358	-2368	1189	-1473	-278	-1686	1618	-880	1884
123	-163	-2205	-1829	-2375	-1841	-1779	572	-1351	-2370	1193	-1472	-272	-1686	1641	-880	1897
124	-170	-2242	-1835	-2373	-1857	-1786	560	-1347	-2380	1179	-1486	-287	-1693	1632	-898	1892
125	-165	-2281	-1827	-2374	-1855	-1783	565	-1339	-2398	1184	-1488	-288	-1701	1631	-916	1910
126	-158	-2183	-1820	-2371	-1851	-1781	579	-1325	-2374	1189	-1478	-283	-1705	1630	-907	1913
127	-160	-2199	-1821	-2357	-1860	-1774	568	-1319	-2382	1191	-1480	-281	-1714	1633	-918	1920
128	-165	-2201	-1823	-2359	-1867	-1787	563	-1320	-2390	1176	-1487	-280	-1718	1643	-927	1933
129	-169	-2201	-1825	-2370	-1871	-1778	558	-1311	-2399	1176	-1491	-285	-1736	1636	-946	1933
130	-167	-2197	-1831	-2368	-1869	-1776	554	-1307	-2405	1166	-1490	-283	-1743	1634	-958	1938
131	-159	-2201	-1821	-2371	-1866	-1783	558	-1299	-2402	1164	-1490	-286	-1739	1637	-957	1943
132	-162	-2202	-1826	-2371	-1867	-1781	561	-1296	-2412	1161	-1493	-240	-1758	1656	-943	1948
133	-160	-2203	-1829	-2372	-1872	-1786	554	-1300	-2421	1161	-1500	-237	-1766	1653	-982	1947
134	-166	-2201	-1827	-2376	-1875	-1789	560	-1289	-2428	1149	-1497	-241	-1778	1655	-998	1957
135	-166	-2196	-1827	-2370	-1872	-1787	554	-1289	-2440	1143	-1499	-233	-1801	1654	-1016	1956
136	-165	-2201	-1823	-2378	-1866	-1789	559	-1289	-2440	1139	-1501	-237	-1801	1656	-1018	1961
137	-167	-2203	-1830	-2377	-1872	-1794	562	-1285	-2453	1146	-1505	-231	-1816	1637	-1039	1974
138	-168	-2202	-1834	-2384	-1868	-1792	564	-1284	-2460	1137	-1509	-227	-1824	1637	-1039	1975
139	-168	-2203	-1828	-2373	-1869	-1791	566	-1283	-2468	1136	-1506	-221	-1827	1676	-1045	1977
140	-174	-2203	-1834	-2375	-1870	-1794	558	-1275	-2479	1139	-1513	-219	-1835	1674	-1053	1983
141	-170	-2202	-1835	-2381	-1866	-1798	555	-1292	-2485	1131	-1516	-229	-1850	1677	-1080	1993
142	-171	-2198	-1835	-2375	-1869	-1796	559	-1284	-2494	1131	-1519	-219	-1852	1646	-1093	2003
143	-183	-2198	-1841	-2372	-1866	-1800	548	-1291	-2505	1126	-1534	-228	-1878	1678	-1104	2008
144	-179	-2203	-1837	-2377	-1867	-1806	561	-1294	-2510	1120	-1533	-229	-1886	1676	-1126	2014
145	-185	-2198	-1848	-2375	-1865	-1801	554	-1286	-2526	1130	-1545	-225	-1898	1695	-1138	2030
146	-179	-2201	-1840	-2373	-1866	-1802	547	-1298	-2530	1126	-1545	-224	-1903	1730	-1156	2034
147	-181	-2205	-1844	-2377	-1851	-1809	558	-1306	-2542	1107	-1545	-245	-1930	1674	-1175	2021
148	-183	-2205	-1846	-2379	-1853	-1813	551	-1309	-2552	1119	-1554	-252	-1937	1637	-1178	2041
149	-185	-2201	-1850	-2373	-1847	-1810	542	-1310	-2550	1118	-1557	-245	-1942	1695	-1195	2048
150	-188	-2244	-1848	-2343	-1850	-1816	550	-1328	-2557	1110	-1555	-252	-1937	1637	-1204	2046

DATE: 9 JUN 77

TEST NUMBER: 1629

ASD STUDY, SUBJECT C-2, DUNELF, 761117, NATION

11 POINT QUADRATIC FIT

THE FOLLOWING IS A LISTING OF 0(I)-0P(I)-0(I-1)+0R(I-1) IN COUNTS:

FRAME NO.	RANGE			SLED			HIP			KNEE			SHOULDER			ELBOW			HEAD PT. 1			HEAD PT. 2		
	X	Y	Z	X	Y	Z	X	Y	Z	X	Y	Z	X	Y	Z	X	Y	Z	X	Y	Z	X	Y	Z
1	-11	1	1	2	1	1	5	1	1	13	3	3	6	5	5	10	4	4	0	1	1	23	16	6
2	0	1	1	-2	1	3	2	3	4	-1	-1	2	1	2	2	-1	-1	-11	-3	-11	-2	-6	6	6
3	-7	3	3	-4	3	3	-5	3	3	-2	3	3	-4	3	3	0	2	2	-2	2	2	-6	6	6
4	-3	3	3	5	5	5	4	5	6	6	3	3	1	3	3	1	3	1	-2	4	4	4	2	2
5	-4	4	4	1	1	1	-5	1	1	1	1	1	-2	0	0	-2	3	3	-2	1	1	0	7	7
6	6	3	3	-4	2	2	6	3	-5	7	7	7	-3	-8	8	3	3	3	3	5	5	-5	3	3
7	7	2	2	2	2	2	6	0	11	-9	-9	3	-3	-8	8	0	0	0	-2	0	0	-5	5	5
8	-1	5	5	-2	1	1	-2	2	4	4	4	3	3	6	6	0	6	6	-1	1	1	-3	2	2
9	7	0	0	1	1	1	-4	1	4	-4	-4	-2	-4	-4	-4	-1	-1	-1	-1	-1	-1	-4	2	2
10	-6	5	5	0	0	0	-5	2	-3	-2	-2	2	-4	2	2	-3	8	8	-17	17	17	22	7	7
11	3	3	3	1	1	1	5	1	6	3	3	3	7	6	6	1	6	7	25	13	13	-18	7	7
12	3	3	3	3	3	3	-6	-1	-3	2	2	2	-9	-5	-5	-3	1	1	-7	2	2	-3	-9	-9
13	-1	2	2	0	0	0	-2	2	-2	-3	-3	3	1	-5	-5	-2	-3	-3	-7	-5	-5	-2	11	11
14	8	-1	1	-2	-1	1	-3	1	-6	3	3	3	-1	-4	-4	-2	-3	-3	4	4	4	1	-5	-5
15	-6	4	4	3	3	3	1	2	-9	6	6	6	7	8	8	5	2	2	7	1	1	6	3	3
16	-1	4	4	3	2	2	0	2	2	-1	-1	-5	-1	-1	-1	1	-1	-1	8	2	2	6	3	3
17	1	2	2	-2	2	2	-2	2	-2	-8	-8	2	1	2	2	-1	1	1	8	8	8	2	0	0
18	-1	1	1	-2	5	5	-1	-2	6	1	1	0	0	-6	-6	-3	3	3	7	7	7	2	-7	-7
19	-2	1	1	6	3	3	0	1	2	1	1	3	3	1	1	5	-2	-2	0	4	4	0	4	4
20	0	-1	1	-1	-1	1	4	2	0	-6	-6	4	4	2	2	-2	-3	-3	0	1	1	3	1	1
21	4	-1	1	2	2	2	-4	1	6	1	1	2	2	2	2	4	5	5	16	2	2	-4	0	0
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23	-1	4	4	-3	3	3	3	6	1	2	2	1	1	1	1	3	3	3	0	7	7	-2	1	1
24	1	2	2	3	-1	1	2	-6	-2	-11	-11	-4	-2	-2	-2	-1	-5	-5	-8	-7	-7	-3	-2	-2
25	-8	1	1	0	-2	2	4	0	-3	9	9	1	3	3	3	5	-4	-4	2	5	5	-3	7	7
26	7	-5	5	-1	-1	1	-4	-2	5	-4	-4	1	1	1	1	3	1	1	-4	-4	-4	0	-7	-7
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32	2	-6	6	-1	0	0	9	6	6	-2	-2	1	1	1	1	4	3	3	-11	11	11	0	-8	-8
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96	8	-2	-4	0	-6	1	-13	11	-3	19	-17	-11	2	-2	-2	6
97	-3	2	-2	-1	0	6	-1	5	5	23	-18	2	6	19	15	22
98	2	9	3	-2	2	0	-10	8	-1	11	-12	2	8	-2	7	12
99	2	-1	0	2	-1	4	-1	13	4	20	-19	-3	-1	6	5	8
100	2	-4	-2	3	-3	8	-7	9	2	18	-18	2	20	1	10	17
101	-4	0	-4	-1	-2	2	-7	10	4	16	-26	-1	3	7	17	13
102	2	3	0	0	4	1	4	7	16	16	-1	-6	1	13	8	-9
103	-4	-5	0	-2	-1	7	-7	9	-12	8	-16	-3	15	11	1	35
104	-2	5	-5	1	-6	1	6	7	-5	19	-13	-3	1	7	4	29
105	-6	5	3	0	0	4	-8	4	4	-18	-25	-2	2	1	2	0
106	0	-5	1	1	-4	4	-6	4	4	2	-13	3	7	-3	1	6
107	-3	0	1	0	2	2	8	11	-13	13	-22	-3	-4	28	4	24
108	-4	-1	-2	-2	-3	1	-13	4	5	3	-16	-4	-3	0	-2	33
109	2	1	0	-1	0	-1	1	10	0	10	-12	-4	3	6	4	7
110	-2	-5	1	2	-9	6	0	5	-5	4	-11	3	2	5	-5	18
111	-3	-2	0	0	6	12	-9	14	3	-2	-16	3	2	-3	-3	15
112	0	1	0	0	-10	-2	-2	4	1	1	-15	-1	-7	12	0	18
113	-1	4	2	-1	-1	-3	-3	2	-5	4	-13	-5	0	-4	-1	24
114	1	0	-1	-1	-4	3	-6	9	-14	10	-12	8	5	8	-12	14
115	-1	6	2	1	-8	3	-5	1	-7	-2	-13	3	-7	13	-2	11
116	0	-4	-2	0	-3	4	2	13	3	8	-6	8	3	0	1	24
117	0	-5	-1	1	-6	-1	-3	5	-10	5	-10	4	-20	5	-9	18
118	0	1	3	1	-4	-1	-3	8	-5	-5	-7	-1	-2	4	-14	18
119	1	0	-3	0	-4	-5	-13	7	-1	-2	-4	0	-6	-4	-4	5



120	5	0	1	2	1	4	5	4	1	10	8	6	10	4	5	7	3
121	2	6	1	1	1	4	6	4	1	11	2	2	5	5	11	28	14
122	4	1	1	1	1	4	1	4	9	2	18	8	2	5	11	14	16
123	6	0	1	1	1	4	4	4	6	7	4	4	4	6	6	13	13
124	7	3	1	1	1	10	9	10	5	1	1	17	7	2	1	3	8
125	5	1	1	1	1	2	3	2	0	7	12	4	7	2	14	31	12
126	7	3	0	0	0	1	3	1	7	11	7	2	2	12	9	16	0
127	6	1	1	1	1	8	1	8	3	7	0	7	4	3	1	3	4
128	1	2	3	0	0	11	8	11	6	1	8	3	0	3	12	8	15
129	1	0	2	1	0	9	0	9	1	9	9	0	0	15	12	21	0
130	2	4	8	2	1	2	0	2	1	6	0	14	1	2	11	16	1
131	9	4	1	1	1	3	6	3	5	12	6	2	2	1	15	7	11
132	4	1	1	1	1	3	3	3	7	4	4	2	1	3	15	0	6
133	4	1	1	1	1	4	1	4	3	3	3	2	1	4	12	8	0
134	0	2	2	0	0	5	1	5	6	9	7	14	3	6	12	10	8
135	0	5	0	1	0	3	3	3	6	5	12	11	2	3	21	4	5
136	1	5	3	3	3	3	5	3	4	5	1	1	1	1	1	7	18
137	2	2	5	1	1	4	4	4	5	6	11	9	2	8	11	1	15
138	1	1	1	1	1	5	5	1	3	0	6	10	3	3	7	9	1
139	0	1	2	2	2	7	1	0	2	0	8	2	2	3	3	2	0
140	0	2	3	0	0	1	2	1	5	10	8	5	5	4	5	0	8
141	1	1	2	2	2	5	3	5	4	18	7	9	2	11	16	2	9
142	1	4	1	2	0	2	8	2	5	4	8	4	2	6	11	5	6
143	12	0	6	1	1	4	5	4	1	7	1	5	3	9	14	1	5
144	4	5	0	0	0	1	5	1	9	2	9	1	1	4	12	3	11
145	6	3	5	3	3	0	2	0	13	3	10	5	5	1	6	14	11
146	6	3	2	5	2	2	3	2	13	9	10	1	1	4	17	9	1
147	2	4	2	0	0	3	7	3	4	13	10	15	8	17	19	23	3
148	2	0	0	2	0	4	0	4	5	3	8	12	7	7	5	13	20
149	2	4	2	2	2	1	8	1	7	5	4	5	4	3	11	14	3
150	3	3	5	7	3	0	0	3	11	15	4	5	5	4	8	5	1



DATE: 9 JUN 77

TEST NUMBER: 1039

ESD STUDY, SUBJECT C 2, RUN 1039, 764147, NYLON

11 POINT QUADRATIC FIT

THE FOLLOWING IS A LISTING OF PARAMETER - SLED DISPLACEMENT IN FEET:

FRAME NO.	TIME (SEC)	HIP		KNEE		SHOULDER		ELBOW		HEAD PT. 1		HEAD PT. 2	
		X	Z	X	Z	X	Z	X	Z	X	Z	X	Z
5	.01020	-.055	.315	1.509	.375	-.500	2.005	-.366	.898	-.539	2.574	-.246	3.076
6	.01224	-.055	.306	1.510	.375	-.500	2.005	-.366	.899	-.540	2.574	-.249	3.079
7	.01428	-.055	.315	1.512	.375	-.499	2.007	-.365	.901	-.540	2.576	-.253	3.083
8	.01632	-.055	.305	1.513	.375	-.499	2.008	-.365	.902	-.539	2.578	-.257	3.085
9	.01836	-.055	.315	1.513	.375	-.498	2.010	-.365	.903	-.538	2.579	-.264	3.087
10	.02040	-.055	.305	1.513	.375	-.499	2.010	-.366	.904	-.538	2.580	-.270	3.090
11	.02244	-.056	.304	1.513	.374	-.499	2.011	-.366	.904	-.538	2.581	-.275	3.091
12	.02448	-.056	.304	1.511	.375	-.499	2.010	-.366	.904	-.537	2.580	-.279	3.091
13	.02652	-.056	.304	1.510	.376	-.500	2.010	-.366	.903	-.538	2.580	-.280	3.093
14	.02856	-.055	.304	1.509	.376	-.500	2.009	-.366	.903	-.538	2.579	-.279	3.092
15	.03060	-.056	.304	1.509	.376	-.500	2.008	-.366	.902	-.538	2.579	-.280	3.091
16	.03264	-.055	.303	1.509	.375	-.500	2.006	-.365	.901	-.541	2.577	-.278	3.089
17	.03468	-.056	.304	1.509	.374	-.499	2.007	-.365	.902	-.541	2.577	-.277	3.089
18	.03672	-.056	.304	1.510	.373	-.499	2.007	-.365	.901	-.539	2.576	-.277	3.088
19	.03876	-.056	.304	1.511	.372	-.499	2.007	-.365	.901	-.537	2.576	-.277	3.088
20	.04080	-.055	.304	1.512	.372	-.499	2.007	-.366	.902	-.535	2.575	-.277	3.088
21	.04284	-.055	.305	1.513	.372	-.498	2.007	-.366	.903	-.534	2.575	-.278	3.088
22	.04488	-.054	.305	1.513	.373	-.498	2.008	-.365	.903	-.534	2.576	-.279	3.089
23	.04692	-.054	.306	1.513	.375	-.498	2.009	-.365	.904	-.534	2.576	-.281	3.090
24	.04896	-.054	.306	1.514	.375	-.498	2.009	-.365	.904	-.534	2.576	-.281	3.090
25	.05100	-.054	.307	1.514	.375	-.499	2.008	-.365	.904	-.536	2.576	-.282	3.090
26	.05304	-.053	.307	1.514	.375	-.500	2.008	-.364	.904	-.539	2.577	-.282	3.090
27	.05508	-.053	.307	1.514	.376	-.500	2.008	-.364	.904	-.540	2.577	-.283	3.091
28	.05712	-.053	.307	1.514	.377	-.500	2.007	-.363	.903	-.540	2.577	-.283	3.090
29	.05916	-.051	.307	1.516	.378	-.499	2.007	-.362	.903	-.540	2.577	-.282	3.090
30	.06120	-.049	.308	1.517	.378	-.499	2.006	-.361	.903	-.539	2.577	-.282	3.090
31	.06324	-.047	.309	1.519	.380	-.497	2.006	-.359	.903	-.540	2.577	-.281	3.090
32	.06528	-.044	.309	1.521	.381	-.495	2.007	-.356	.903	-.539	2.577	-.281	3.089
33	.06731	-.042	.309	1.525	.382	-.492	2.006	-.352	.902	-.536	2.576	-.280	3.088
34	.06935	-.038	.309	1.528	.383	-.489	2.006	-.348	.901	-.534	2.577	-.278	3.087
35	.07139	-.034	.307	1.534	.383	-.485	2.006	-.343	.900	-.530	2.575	-.275	3.085
36	.07343	-.030	.306	1.540	.383	-.479	2.006	-.337	.900	-.525	2.574	-.271	3.085
37	.07547	-.026	.303	1.546	.382	-.472	2.006	-.330	.900	-.517	2.573	-.265	3.085
38	.07751	-.022	.302	1.552	.382	-.465	2.005	-.321	.899	-.509	2.572	-.259	3.083
39	.07955	-.017	.301	1.559	.381	-.455	2.005	-.312	.899	-.498	2.572	-.251	3.082
40	.08159	-.011	.302	1.565	.382	-.446	2.006	-.301	.899	-.488	2.571	-.241	3.082
41	.08363	-.005	.303	1.572	.383	-.435	2.007	-.290	.899	-.477	2.572	-.230	3.082
42	.08567	.003	.305	1.579	.383	-.423	2.008	-.277	.898	-.464	2.572	-.215	3.082
43	.08771	.010	.307	1.588	.385	-.410	2.008	-.263	.898	-.451	2.573	-.208	3.081
44	.08975	.019	.307	1.598	.385	-.397	2.007	-.249	.898	-.438	2.571	-.184	3.081
45	.09179	.028	.306	1.610	.386	-.382	2.006	-.234	.897	-.423	2.569	-.167	3.080
46	.09383	.038	.306	1.621	.384	-.367	2.006	-.218	.897	-.407	2.568	-.150	3.079
47	.09587	.047	.305	1.633	.384	-.352	2.004	-.202	.897	-.391	2.566	-.133	3.075
48	.09791	.057	.306	1.645	.382	-.336	2.003	-.184	.896	-.374	2.564	-.115	3.072
49	.09995	.066	.305	1.657	.382	-.320	2.003	-.164	.896	-.357	2.563	-.094	3.068
50	.10199	.075	.308	1.669	.381	-.304	2.003	-.145	.897	-.339	2.563	-.074	3.065
51	.10403	.083	.308	1.681	.380	-.287	2.003	-.124	.897	-.320	2.562	-.051	3.062
52	.10607	.093	.308	1.692	.379	-.271	2.004	-.101	.898	-.299	2.560	-.024	3.059
53	.10811	.101	.308	1.703	.378	-.256	2.004	-.077	.900	-.279	2.558	.001	3.056
54	.11015	.110	.308	1.712	.375	-.241	2.004	-.053	.901	-.258	2.555	.028	3.055

DATE: 9 JUN 77

TEST NUMBER: 1039

RSD STUDY, SUBJECT G-2, RUNIC679, 751117, NYLON

11 POINT QUADRATIC FIT

THE FOLLOWING IS A LISTING OF PARAMETER - SLED DISPLACEMENT IN FEET:

FRAME NO.	TIME (SEC)	HIP			KNEE			SHOULDER			ELBOW			HEAD PT. 1			HEAD PT. 2		
		X	Y	Z	X	Y	Z	X	Y	Z	X	Y	Z	X	Y	Z	X	Y	Z
55	11249	118	126	133	137	143	149	154	160	166	172	178	184	189	195	201	206	212	218
56	11423	133	140	147	154	161	168	175	182	189	196	203	210	215	222	229	235	242	249
57	11627	143	151	159	167	175	183	191	199	207	215	223	231	237	245	253	260	268	276
58	11831	159	168	177	186	195	204	213	222	231	240	249	258	266	275	284	292	301	310
59	12035	175	185	195	205	215	225	235	245	255	265	275	285	294	304	314	323	333	343
60	12239	191	202	213	224	235	246	256	267	278	289	299	310	319	329	339	349	359	369
61	12443	207	219	231	242	254	266	277	289	300	312	323	335	344	355	366	376	387	398
62	12647	223	236	249	260	272	285	296	308	319	331	342	354	363	374	385	395	406	417
63	12851	239	253	267	278	291	304	315	327	338	350	361	373	382	393	404	414	425	436
64	13055	255	270	285	296	309	322	333	345	356	368	379	391	400	411	422	432	443	454
65	13259	271	287	303	314	327	340	351	363	374	386	397	409	418	429	440	450	461	472
66	13463	287	304	321	332	345	358	369	381	392	404	415	427	436	447	458	468	479	490
67	13667	303	321	339	350	363	376	387	399	410	422	433	445	454	465	476	486	497	508
68	13871	319	338	357	368	381	394	405	417	428	440	451	463	472	483	494	504	515	526
69	14075	335	355	375	386	400	413	424	436	447	459	470	482	491	502	513	523	534	545
70	14279	351	372	393	404	418	431	442	454	465	477	488	500	509	520	531	541	552	563
71	14483	367	389	411	422	436	449	460	472	483	495	506	518	527	538	548	559	569	580
72	14687	383	406	429	440	454	467	478	489	501	512	523	535	544	555	565	576	587	598
73	14891	399	423	447	458	472	485	496	508	519	530	542	553	563	574	585	595	606	617
74	15095	415	440	465	476	490	503	514	526	537	548	560	571	581	592	603	613	624	635
75	15299	431	457	483	494	508	521	532	544	555	566	578	589	600	610	621	631	642	653
76	15503	447	474	501	512	526	539	550	562	573	584	596	607	617	628	638	649	659	670
77	15707	463	491	519	530	544	557	568	580	591	602	614	625	635	646	656	667	677	688
78	15911	479	508	537	548	562	575	586	598	609	620	632	643	653	664	674	685	695	706
79	16115	495	525	555	566	580	593	604	616	627	638	649	660	670	681	691	702	712	723
80	16319	511	542	573	584	598	611	622	634	645	656	667	678	688	699	709	720	730	741
81	16523	527	559	591	602	616	629	640	652	663	674	685	696	706	717	727	737	747	758
82	16727	543	576	609	620	634	647	658	670	681	692	703	714	724	735	745	755	765	776
83	16931	559	593	627	638	652	665	676	688	699	710	721	732	742	753	763	773	783	794
84	17135	575	610	645	656	670	683	694	706	717	728	739	750	760	771	781	791	801	812
85	17339	591	627	663	674	688	701	712	724	735	746	757	768	778	789	799	809	819	830
86	17543	607	644	681	692	706	719	730	742	753	764	775	786	796	807	817	827	837	848
87	17747	623	661	700	711	725	738	749	761	772	783	794	805	815	826	836	846	856	867
88	17951	639	678	717	728	742	755	766	778	789	800	811	822	832	843	853	863	873	884
89	18155	655	695	735	746	760	773	784	796	807	818	829	840	850	861	871	881	891	902
90	18359	671	712	753	764	778	791	802	814	825	836	847	858	868	879	889	899	909	920
91	18563	687	729	771	782	796	809	820	832	843	854	865	876	886	897	907	917	927	938
92	18767	703	746	789	800	814	827	838	850	861	872	883	894	904	915	925	935	945	956
93	18971	719	763	807	818	832	845	856	868	879	890	901	912	922	933	943	953	963	974
94	19175	735	780	825	836	850	863	874	886	897	908	919	930	940	951	961	971	981	992
95	19379	751	797	843	854	868	881	892	904	915	926	937	948	958	969	979	989	999	1010
96	19583	767	814	861	872	886	899	910	922	933	944	955	966	976	987	997	1007	1017	1028
97	19786	783	831	879	890	904	917	928	940	951	962	973	984	994	1005	1015	1025	1035	1046
98	19990	799	848	897	908	922	935	946	958	969	980	991	1002	1012	1023	1033	1043	1053	1064
99	20194	815	865	915	926	940	953	964	976	987	998	1009	1020	1030	1041	1051	1061	1071	1082
100	20398	831	882	933	944	958	971	982	994	1005	1016	1027	1038	1048	1059	1069	1079	1089	1100
101	20602	847	899	951	962	976	989	1000	1012	1023	1034	1045	1056	1066	1077	1087	1097	1107	1118
102	20806	863	916	969	980	994	1007	1018	1030	1041	1052	1063	1074	1084	1095	1105	1115	1125	1136
103	21010	879	933	987	998	1012	1025	1036	1048	1059	1070	1081	1092	1102	1113	1123	1133	1143	1154
104	21214	895	950	1005	1016	1030	1043	1054	1066	1077	1088	1099	1110	1120	1131	1141	1151	1161	1172

DATE: 9 JUN 77

TEST NUMBER: 1039

SSO STUDY, SUBJECT C-2, RUNIC13, 761117, NYLON

11 POINT QUADRATIC FIT

THE FOLLOWING IS A LISTING OF PARAMETER - SLED DISPLACEMENT IN FEET:

FRAME NO.	TIME (SEC)	HIP		KNEE		SHOULDER		ELBOW		HEAD PT. 1		HEAD PT. 2	
		X	Z	X	Z	X	Z	X	Z	X	Z	X	Z
105	21418	.024	.323	1.503	.528	-.262	2.105	.360	1.264	.033	2.461	.572	2.547
106	21622	.022	.325	1.502	.532	-.262	2.112	.351	1.262	.034	2.466	.573	2.560
107	21826	.021	.328	1.500	.536	-.263	2.116	.340	1.261	.035	2.470	.574	2.573
108	22030	.020	.331	1.498	.541	-.261	2.120	.331	1.260	.035	2.474	.574	2.592
109	22234	.018	.333	1.495	.545	-.261	2.123	.322	1.259	.034	2.478	.574	2.594
110	22438	.017	.336	1.493	.551	-.261	2.126	.314	1.259	.035	2.482	.573	2.608
111	22642	.015	.337	1.491	.555	-.263	2.130	.305	1.259	.034	2.485	.571	2.621
112	22846	.013	.339	1.488	.559	-.265	2.133	.298	1.260	.035	2.487	.569	2.632
113	23050	.010	.340	1.486	.563	-.267	2.136	.290	1.261	.034	2.490	.567	2.643
114	23254	.007	.343	1.484	.567	-.271	2.139	.282	1.263	.032	2.494	.564	2.656
115	23458	.004	.344	1.481	.571	-.274	2.143	.276	1.265	.029	2.498	.561	2.669
116	23662	.001	.344	1.479	.574	-.279	2.144	.271	1.267	.026	2.499	.557	2.680
117	23866	-.002	.345	1.477	.578	-.283	2.144	.266	1.268	.024	2.502	.553	2.688
118	24070	-.005	.346	1.475	.583	-.287	2.144	.261	1.270	.020	2.503	.547	2.696
119	24274	-.007	.347	1.474	.587	-.290	2.144	.258	1.271	.015	2.505	.540	2.705
120	24478	-.009	.348	1.471	.591	-.292	2.144	.256	1.273	.013	2.506	.533	2.712
121	24682	-.012	.349	1.467	.594	-.297	2.143	.252	1.274	.009	2.508	.524	2.718
122	24886	-.015	.349	1.465	.598	-.300	2.143	.250	1.276	.005	2.510	.515	2.724
123	25090	-.018	.350	1.463	.603	-.302	2.144	.247	1.279	-.000	2.513	.507	2.729
124	25294	-.021	.350	1.461	.606	-.305	2.143	.245	1.281	-.006	2.514	.498	2.735
125	25498	-.025	.350	1.459	.610	-.308	2.143	.242	1.284	-.012	2.517	.490	2.741
126	25702	-.029	.349	1.457	.612	-.312	2.140	.241	1.287	-.017	2.518	.484	2.744
127	25906	-.032	.348	1.455	.616	-.315	2.137	.239	1.290	-.022	2.521	.475	2.747
128	26110	-.034	.349	1.454	.620	-.317	2.135	.238	1.292	-.028	2.522	.469	2.752
129	26314	-.034	.349	1.453	.623	-.320	2.133	.237	1.295	-.033	2.525	.465	2.756
130	26518	-.035	.349	1.452	.627	-.322	2.131	.237	1.297	-.037	2.526	.461	2.759
131	26722	-.036	.348	1.451	.629	-.326	2.128	.236	1.298	-.043	2.526	.454	2.763
132	26926	-.035	.348	1.451	.632	-.329	2.126	.235	1.298	-.049	2.528	.447	2.765
133	27130	-.035	.348	1.451	.635	-.333	2.124	.234	1.299	-.057	2.529	.438	2.768
134	27334	-.035	.347	1.452	.638	-.337	2.122	.233	1.299	-.064	2.530	.429	2.773
135	27538	-.036	.347	1.453	.640	-.342	2.121	.231	1.301	-.073	2.534	.420	2.777
136	27742	-.035	.346	1.454	.642	-.347	2.119	.231	1.303	-.079	2.536	.412	2.790
137	27946	-.035	.346	1.455	.644	-.351	2.118	.230	1.305	-.085	2.538	.404	2.794
138	28150	-.033	.346	1.456	.646	-.356	2.117	.230	1.308	-.090	2.541	.398	2.799
139	28354	-.031	.345	1.456	.648	-.360	2.116	.229	1.309	-.095	2.543	.393	2.792
140	28558	-.029	.344	1.457	.645	-.363	2.115	.228	1.309	-.100	2.543	.386	2.797
141	28762	-.028	.343	1.458	.644	-.367	2.113	.226	1.309	-.105	2.543	.379	2.801
142	28966	-.025	.342	1.457	.643	-.371	2.111	.224	1.309	-.111	2.546	.371	2.806
143	29170	-.023	.340	1.458	.641	-.376	2.109	.223	1.308	-.118	2.546	.360	2.810
144	29374	-.021	.339	1.459	.639	-.381	2.108	.220	1.307	-.126	2.548	.349	2.816
145	29578	-.019	.338	1.459	.637	-.385	2.106	.218	1.304	-.134	2.548	.339	2.820

THE ABOVE DATA WAS PLOTTED (X VERSUS Z) FOR FRAME NUMBER 5 TO FRAME NUMBER 145



DATE: 9 JUN 72

TEST NUMBER: 1039

RSD STUDY, SUBJECT C-2, RUN 1039, 754117, NYLON

11 POINT QUADRATIC FIT

THE FOLLOWING IS A LISTING OF THE ANGULAR MOTION OF THE HEAD AND SHOULDER:

FRAME NO.	TIME (SEC)	SHOULDER - HIP			HEAD PT. 1 - HEAD PT. 2		
		THETA (RAD/SEC)	W (RAD/SEC)	W-ACC (RAD/SEC SQ)	THETA (RAD/SEC)	W (RAD/SEC)	W-ACC (RAD/SEC SQ)
15	0.03060	1.826	0.09	3.238	4.245	.314	-123.689
16	0.03264	1.826	0.15	3.559	4.238	.183	-71.885
17	0.03468	1.826	0.11	4.948	4.237	.225	-30.479
18	0.03672	1.825	0.17	6.848	4.239	.198	-5.766
19	0.03876	1.825	0.19	8.727	4.242	.785	.313
20	0.04080	1.825	0.45	10.361	4.246	.897	-9.816
21	0.04284	1.826	0.69	11.615	4.250	.974	-30.971
22	0.04488	1.826	1.11	12.700	4.251	.660	-54.115
23	0.04692	1.826	1.57	11.838	4.256	.359	-72.928
24	0.04896	1.826	1.75	9.896	4.266	.058	-78.187
25	0.05100	1.827	1.94	6.764	4.253	-1.89	-67.430
26	0.05304	1.824	2.16	2.210	4.248	-.393	-45.350
27	0.05508	1.824	2.25	-3.726	4.248	-.476	-16.652
28	0.05712	1.828	2.20	-10.365	4.247	-.446	13.359
29	0.05916	1.829	2.05	-19.079	4.247	-.305	40.800
30	0.06120	1.829	1.67	-29.604	4.247	-.096	62.486
31	0.06324	1.830	1.08	-39.750	4.245	.103	75.077
32	0.06528	1.830	0.21	-49.760	4.246	.268	75.868
33	0.06731	1.830	-.109	-58.457	4.249	.463	63.996
34	0.06935	1.830	-.264	-64.906	4.248	.670	42.411
35	0.07139	1.830	-.428	-68.230	4.249	.831	13.715
36	0.07343	1.829	-.604	-68.239	4.251	.881	-18.547
37	0.07547	1.827	-.757	-65.068	4.255	.804	-52.677
38	0.07751	1.825	-.901	-59.511	4.257	.580	-85.525
39	0.07955	1.823	-1.022	-53.106	4.261	.316	-114.251
40	0.08159	1.821	-1.111	-46.762	4.262	-.014	-134.868
41	0.08363	1.818	-1.181	-41.813	4.260	-.370	-146.104
42	0.08567	1.816	-1.236	-38.064	4.259	-.749	-151.439
43	0.08771	1.813	-1.294	-37.640	4.254	-1.061	-152.442
44	0.08975	1.811	-1.354	-37.296	4.251	-1.374	-153.746
45	0.09179	1.808	-1.423	-37.115	4.249	-1.628	-156.628
46	0.09383	1.805	-1.529	-36.351	4.247	-1.852	-161.180
47	0.09587	1.802	-1.636	-34.047	4.243	-2.193	-167.862
48	0.09791	1.798	-1.721	-29.605	4.239	-2.521	-178.070
49	0.09995	1.795	-1.788	-20.847	4.233	-2.931	-191.741
50	0.10199	1.791	-1.824	-9.059	4.227	-3.387	-207.970
51	0.10403	1.786	-1.855	5.722	4.220	-3.800	-222.968
52	0.10607	1.782	-1.852	22.395	4.208	-4.231	-234.342
53	0.10811	1.779	-1.801	40.248	4.201	-4.705	-244.451
54	0.11015	1.775	-1.697	58.553	4.191	-5.270	-252.862
55	0.11219	1.772	-1.542	75.783	4.181	-5.860	-262.048
56	0.11423	1.768	-1.351	89.592	4.171	-6.399	-273.047
57	0.11627	1.765	-1.138	97.451	4.158	-6.912	-284.622
58	0.11831	1.763	-.978	97.962	4.142	-7.466	-296.547
59	0.12035	1.761	-.601	90.873	4.122	-8.051	-316.581
60	0.12239	1.760	-.348	76.837	4.105	-8.699	-350.725
61	0.12443	1.760	-.165	57.856	4.089	-9.387	-397.080
62	0.12647	1.760	-.067	35.824	4.071	-10.117	-451.762
63	0.12851	1.762	-.043	13.910	4.052	-10.880	-507.644
64	0.13055	1.763	-.034	-3.899	4.029	-12.003	-556.958



DATE: 9 JUN 77

TEST NUMBER: 1039

PSO STUDY, SUBJECT C-2, 20N1039, 751117, NYLON

11 POINT QUADRATIC FIT

THE FOLLOWING IS A LISTING OF THE ANGULAR MOTION OF THE HEAD AND SHOULDER:

FRAME NO.	TIME (SEC)	SHOULDER - HIP			HEAD PT. 1 - HEAD PT. 2		
		THETA (RAD/SEC)	W (RAD/SEC)	W-ACC (RAD/SEC SQ)	THETA (RAD/SEC)	W (RAD/SEC)	W-ACC (RAD/SEC SQ)
65	13259	1.763	-1.75	-14.743	4.003	-13.408	-591.529
66	13463	1.761	-1.264	-17.532	3.976	-14.885	-601.486
67	13667	1.760	-1.392	-13.639	3.945	-16.417	-576.300
68	13871	1.759	-1.453	-4.705	3.915	-17.858	-608.092
69	14075	1.757	-1.444	6.953	3.869	-19.088	-403.173
70	14279	1.756	-1.375	18.884	3.826	-20.049	-278.699
71	14483	1.755	-1.278	28.817	3.783	-20.565	-150.738
72	14687	1.755	-1.174	35.122	3.736	-20.537	-30.220
73	14891	1.755	-1.073	36.912	3.691	-19.959	72.227
74	15095	1.755	-0.920	34.869	3.648	-19.765	150.015
75	15299	1.755	-0.94	30.233	3.607	-18.837	200.912
76	15503	1.756	-1.48	24.263	3.573	-18.362	228.483
77	15707	1.756	-1.81	17.312	3.544	-17.914	244.644
78	15911	1.757	-2.02	9.335	3.519	-17.493	267.248
79	16115	1.757	-2.21	1.614	3.471	-17.085	317.325
80	16319	1.757	-2.28	-9.268	3.424	-16.561	389.602
81	16523	1.758	-2.22	-20.094	3.397	-16.070	476.951
82	16727	1.759	-1.80	-31.125	3.361	-15.166	570.100
83	16931	1.759	-1.06	-41.974	3.332	-13.832	657.955
84	17135	1.760	-0.403	-51.345	3.304	-11.951	730.141
85	17339	1.760	-1.144	-57.824	3.280	-10.065	775.077
86	17543	1.760	-3.12	-60.314	3.263	-8.163	783.670
87	17747	1.759	-4.68	-57.744	3.248	-6.329	756.393
88	17951	1.758	-6.22	-51.279	3.238	-4.715	697.214
89	18155	1.756	-7.41	-41.958	3.231	-3.275	617.266
90	18359	1.754	-8.23	-31.114	3.231	-2.144	534.977
91	18563	1.752	-9.58	-20.385	3.228	-1.295	458.171
92	18767	1.749	-8.43	-11.293	3.228	-0.541	393.038
93	18971	1.747	-8.37	-4.461	3.229	0.049	342.121
94	19175	1.746	-8.19	4.403	3.229	0.558	305.297
95	19379	1.745	-8.05	1.637	3.227	1.074	281.731
96	19583	1.744	-7.97	2.885	3.229	1.662	266.213
97	19786	1.742	-8.03	3.706	3.234	2.248	254.886
98	19990	1.740	-8.16	6.057	3.239	2.768	245.136
99	20194	1.738	-8.25	9.198	3.245	3.283	233.282
100	20398	1.736	-8.13	12.749	3.256	3.750	220.808
101	20602	1.735	-7.81	16.621	3.264	4.158	210.246
102	20806	1.733	-7.16	20.478	3.275	4.589	204.351
103	21010	1.731	-6.47	23.673	3.280	4.932	202.070
104	21214	1.730	-5.90	25.807	3.291	5.224	199.520
105	21418	1.729	-5.41	26.925	3.301	5.620	195.078
106	21622	1.728	-4.87	27.661	3.314	6.100	186.473
107	21826	1.728	-4.34	28.631	3.330	6.608	170.565
108	22030	1.727	-3.83	30.577	3.340	7.056	163.411
109	22234	1.725	-3.32	32.942	3.354	7.381	119.088
110	22438	1.725	-2.70	34.811	3.373	7.601	77.922
111	22642	1.725	-1.90	35.832	3.390	7.717	32.650
112	22846	1.724	-0.93	35.744	3.408	7.693	-11.725
113	23050	1.724	-0.10	33.916	3.421	7.648	-52.458
114	23254	1.724	-0.91	29.939	3.438	7.437	-88.205

DATE 9 JUN 77 TEST NUMBER 1039 11 POINT QUADRATIC FIT

RSO STUDY, SUBJECT C-2, SUMMIT, 75117, NYLON

THE FOLLOWING IS A LISTING OF THE ANGULAR MOTION OF THE HEAD AND SHOULDER:

FRAME NO.	TIME (SEC)	SHOULDER - HIP			HEAD PT. 1 - HEAD PT. 2		
		THETA (RAD/SEC)	W (RAD/SEC)	W-ACC (RAD/SEC SQ)	THETA (RAD/SEC)	W (RAD/SEC)	W-ACC (RAD/SEC SQ)
115	23658	1.724	.168	23.624	3.453	7.101	-118.900
116	23662	1.725	.193	15.672	3.469	6.817	-144.709
117	23866	1.725	.232	7.165	3.480	6.521	-165.617
118	24070	1.726	.234	.235	3.493	6.159	-183.657
119	24274	1.727	.211	-5.360	3.506	5.755	-196.935
120	24478	1.727	.163	-7.955	3.518	5.331	-207.965
121	24682	1.728	.114	-7.519	3.529	4.876	-215.525
122	24886	1.728	.071	-3.465	3.540	4.412	-216.960
123	25090	1.729	.055	4.921	3.546	3.935	-210.148
124	25294	1.729	.063	15.678	3.555	3.398	-195.997
125	25498	1.727	.090	27.727	3.560	2.929	-175.375
126	25702	1.728	.154	39.435	3.566	2.546	-150.315
127	25906	1.728	.275	49.649	3.569	2.299	-121.739
128	26110	1.728	.418	52.945	3.575	2.121	-93.084
129	26314	1.729	.572	62.411	3.576	2.005	-65.917
130	26518	1.730	.726	64.864	3.579	1.949	-43.845
131	26722	1.732	.871	62.757	3.586	1.896	-23.606
132	26926	1.735	1.064	58.592	3.588	1.912	-4.575
133	27130	1.737	1.126	53.162	3.592	1.884	13.874
134	27334	1.739	1.224	47.536	3.599	1.826	33.023
135	27538	1.742	1.315	42.320	3.601	1.920	54.079

THE ABOVE VEL AND ACCEL DATA ARE PLOTTED: YMIN=-2.00 DY= .40 ZMIN=-80.00 DZ= 20.00

THE ABOVE VEL AND ACCEL DATA ARE PLOTTED: YMIN=-28.00 DY= 4.00 ZMIN=-800.00 DZ= 200.00

DATE: 9 JUN 77

TEST NUMBER: 1039

RSD STUDY, SUBJECT C-2, PUN183, 764117, NYLON

11 POINT QUADRATIC FIT

## HIP MOTION RELATIVE TO THE SLED

FRAME NO.	TIME (SEC)	X (FEET)	DISPLACEMENT Z (FEET)	VELOCITY RESULTANT (FT/SEC)	ACCELERATION RESULTANT (FT/SEC <sup>2</sup> )	ACCELERATION RESULTANT (G)
15	.03050	-.001	-.001	.023	-7.061	-.219
16	.03254	-.001	-.002	-.019	-5.713	-.177
17	.03458	-.001	-.001	-.032	-2.754	-.046
18	.03672	-.001	-.002	-.030	.415	.013
19	.03876	-.001	-.001	-.024	-4.962	-.154
20	.04030	-.000	-.001	-.016	10.425	.324
21	.04234	-.000	-.000	.025	16.436	.510
22	.04438	.001	-.001	.070	22.309	.693
23	.04632	.001	.001	.091	28.798	.894
24	.04835	.001	.001	.155	36.117	1.122
25	.05039	.001	.001	.233	44.059	1.348
26	.05274	.002	.002	.332	52.225	1.622
27	.05538	.002	.002	.443	61.046	1.896
28	.05712	.002	.002	.580	69.379	2.155
29	.05916	.004	.002	.736	75.723	2.352
30	.06120	.006	.003	.910	80.949	2.514
31	.06324	.008	.004	1.098	84.843	2.655
32	.06528	.011	.004	1.301	80.286	2.742
33	.06731	.013	.004	1.440	91.660	2.847
34	.06935	.017	.004	1.647	95.600	2.969
35	.07139	.021	.002	1.831	100.663	3.126
36	.07343	.025	.000	2.013	106.909	3.320
37	.07547	.029	.002	2.240	113.934	3.548
38	.07751	.033	.003	2.473	121.089	3.761
39	.07955	.038	.004	2.741	126.464	3.927
40	.08159	.044	.003	3.036	128.596	3.994
41	.08363	.050	.002	3.340	126.287	3.922
42	.08567	.058	.000	3.636	118.556	3.682
43	.08771	.065	.002	3.946	105.893	3.289
44	.08975	.074	.002	4.132	89.146	2.769
45	.09179	.083	.001	4.316	69.381	2.155
46	.09383	.093	.001	4.430	48.147	1.495
47	.09587	.102	.000	4.488	26.808	.833
48	.09791	.112	.001	4.501	6.257	.194
49	.09995	.121	.001	4.481	-13.024	-.406
50	.10199	.130	.003	4.425	-31.201	-.969
51	.10403	.138	.002	4.343	-48.537	-1.509
52	.10607	.148	.003	4.234	-66.777	-2.074
53	.10811	.156	.003	4.093	-85.165	-2.676
54	.11015	.165	.003	3.915	-107.090	-3.326
55	.11219	.173	.002	3.693	-129.302	-4.016
56	.11423	.181	.001	3.426	-152.272	-4.729
57	.11627	.188	.001	3.075	-174.818	-5.429
58	.11831	.194	.002	2.680	-195.437	-6.069
59	.12035	.200	.004	2.234	-212.277	-6.592
60	.12239	.204	.005	1.747	-224.026	-6.957
61	.12443	.207	.005	1.233	-229.455	-7.126
62	.12647	.209	.006	.713	-228.544	-7.098
63	.12851	.210	.005	.204	-221.892	-6.691
64	.13055	.210	.004	-.264	-210.315	-6.532



DATE: 9 JUN 77 TEST NUMBER: 1039 11 POINT QUADRATIC FIT

ESD STUDY, SUBJECT C-2, SUMMIT, 34417, NATION

HIP MOTION RELATIVE TO THE SLED

FRAME NO.	TIME (SEC)	DISPLACEMENT		VELOCITY		ACCELERATION		ACCELERATION	
		X (FEET)	Z (FEET)	RESULTANT (FEET)	RESULTANT (FT/SEC)	RESULTANT (FT/SEC SOI)	RESULTANT (G)	RESULTANT	RESULTANT
55	13.250	.208	.203	.208	-1.593	-134.796	-6.050		
56	13.253	.205	.206	.206	-1.072	-176.506	-5.482		
57	13.257	.203	.203	.203	-1.413	-156.527	-4.861		
58	13.271	.199	.199	.199	-1.702	-135.565	-4.210		
59	13.275	.196	.196	.196	-1.963	-114.263	-3.549		
70	14.273	.191	.191	.191	-2.180	-92.648	-2.877		
71	14.277	.187	.187	.187	-2.354	-71.280	-2.214		
72	14.281	.181	.181	.181	-2.481	-50.968	-1.583		
73	14.284	.176	.176	.176	-2.556	-33.244	-1.032		
74	15.033	.170	.170	.170	-2.583	-19.104	-.593		
75	15.223	.164	.164	.164	-2.556	-9.736	-.302		
76	15.513	.159	.159	.159	-2.522	-4.994	-.155		
77	15.727	.154	.154	.154	-2.481	-3.977	-.123		
78	15.911	.149	.149	.149	-2.469	-5.239	-.163		
79	16.115	.145	.145	.145	-2.494	-6.573	-.204		
80	16.313	.140	.140	.140	-2.554	-5.868	-.182		
81	16.523	.135	.135	.135	-2.620	-1.177	-.037		
82	16.727	.130	.130	.130	-2.656	8.594	.267		
83	16.931	.123	.123	.123	-2.678	22.997	.714		
84	17.135	.116	.116	.117	-2.631	40.451	1.256		
85	17.333	.111	.111	.111	-2.521	58.412	1.814		
86	17.543	.105	.105	.106	-2.351	74.700	2.320		
87	17.747	.101	.101	.101	-2.132	87.749	2.725		
88	17.951	.097	.097	.097	-1.836	96.723	3.004		
89	18.155	.090	.090	.094	-1.456	101.275	3.145		
90	18.353	.091	.091	.091	-1.440	102.113	3.171		
91	18.553	.088	.088	.089	-1.233	100.119	3.109		
92	18.757	.086	.086	.086	-1.035	96.053	2.983		
93	18.921	.083	.083	.084	-.846	90.351	2.806		
94	19.175	.082	.082	.082	-.656	83.100	2.581		
95	19.273	.081	.081	.081	-.487	74.552	2.315		
96	19.543	.080	.080	.080	-.317	63.997	1.987		
97	19.745	.080	.080	.080	-.173	51.805	1.609		
98	19.931	.080	.080	.080	-.074	38.557	1.197		
99	20.120	.080	.080	.080	-.015	25.101	.780		
100	20.328	.080	.080	.081	.015	12.609	.385		
101	20.642	.081	.081	.081	.000	1.363	.042		
102	20.875	.080	.080	.081	-.033	-7.485	-.232		
103	21.040	.080	.080	.081	-.078	-14.116	-.438		
104	21.214	.079	.079	.081	-.124	-18.967	-.589		
105	21.413	.079	.079	.081	-.161	-22.632	-.700		
106	21.623	.077	.077	.080	-.201	-25.296	-.786		
107	21.825	.076	.076	.079	-.249	-28.218	-.876		
108	22.030	.075	.075	.079	-.308	-31.175	-.968		
109	22.234	.073	.073	.078	-.375	-33.503	-1.040		
110	22.443	.072	.072	.078	-.447	-34.497	-1.071		
111	22.642	.070	.070	.077	-.534	-33.507	-1.041		
112	22.845	.068	.068	.075	-.633	-30.503	-.947		
113	23.050	.065	.065	.074	-.721	-25.663	-.797		
114	23.254	.062	.062	.073	-.777	-19.794	-.615		



DATE: 9 JUN 77 TEST NUMBER: 1039 11 POINT QUADRATIC FIT  
 PSD STUDY, SUBJECT: C 2, RUN: 1039, 751117, NYLON

HIP MOTION RELATIVE TO THE SLED

FRAME NO.	TIME (SEC)	DISPLACEMENT X (FEET)	DISPLACEMENT Z (FEET)	VELOCITY RESULTANT (FT/SEC)	ACCELERATION RESULTANT (FT/SEC SQ)	ACCELERATION RESULTANT (G)
115	23438	.059	.019	-.802	-13.936	-.433
116	23662	.056	.039	-.804	-8.641	-.268
117	23856	.053	.043	-.795	-5.193	-.161
118	24070	.050	.041	-.773	-3.594	-.112
119	24274	.048	.042	-.761	-3.100	-.096
120	24479	.046	.043	-.772	-2.445	-.076
121	24682	.043	.044	-.790	-.745	-.023
122	24896	.040	.044	-.837	2.621	.081
123	25030	.037	.045	-.851	7.788	.242
124	25294	.034	.045	-.851	15.043	.467
125	25438	.030	.045	-.804	23.415	.727
126	25732	.026	.044	-.731	31.234	.970
127	25835	.023	.043	-.640	37.356	1.160
128	26110	.021	.044	-.537	40.379	1.254
129	26314	.021	.044	-.418	40.481	1.257
130	26518	.020	.044	-.311	38.433	1.194
131	26722	.019	.043	-.233	34.904	1.084
132	26925	.020	.043	-.180	30.483	.947
133	27130	.019	.043	-.141	28.031	.888
134	27314	.020	.042	-.103	22.368	.695
135	27538	.019	.042	-.051	20.038	.622

MAXIMUM POSITIVE X DISPLACEMENT: .210 AT TIME .12851

MAXIMUM NEGATIVE X DISPLACEMENT: -.001 AT TIME .03672

MAXIMUM POSITIVE Z DISPLACEMENT: .045 AT TIME .25294

MAXIMUM NEGATIVE Z DISPLACEMENT: -.009 AT TIME .17543

MAXIMUM RESULTANT DISPLACEMENT: .210 AT TIME .12851

DATE: 9 JUN 72 TEST NUMBER: 1039 11 POINT QUADRATIC FIT

RSD STUDY, SUBJECT C-2, RUN#133, 754117, NYLON

KNEE MOTION RELATIVE TO THE SLED

FRAME NO.	TIME (SEC)	X (FEET)	Z (FEET)	DISPLACEMENT RESULTANT (FEET)	VELOCITY RESULTANT (FT/SEC)	ACCELERATION RESULTANT (FT/SEC SO)	ACCELERATION RESULTANT (G)
15	.03053	.006	.005	.008	.130	21.088	.655
16	.03254	.035	.004	.007	.037	28.307	.879
17	.03454	.005	.003	.006	.068	30.862	.958
18	.03672	.006	.002	.006	.151	28.949	.899
19	.03875	.008	.003	.009	.213	26.813	.746
20	.04033	.009	.001	.009	.266	18.240	.566
21	.04234	.009	.003	.009	.291	14.165	.440
22	.04488	.010	.002	.010	.277	12.735	.396
23	.04632	.010	.004	.010	.257	15.376	.478
24	.04835	.012	.004	.011	.254	21.858	.679
25	.05199	.011	.004	.012	.276	32.432	1.007
26	.05314	.010	.004	.011	.351	46.891	1.456
27	.05599	.010	.005	.012	.454	58.581	1.975
28	.05712	.011	.006	.012	.608	79.998	2.484
29	.05946	.013	.007	.014	.709	94.640	2.939
30	.06123	.014	.007	.016	1.027	106.551	3.309
31	.06324	.016	.009	.018	1.299	115.891	3.574
32	.06528	.018	.010	.021	1.576	120.304	3.736
33	.06731	.021	.011	.024	1.838	122.387	3.881
34	.06935	.025	.012	.028	2.094	122.526	3.805
35	.07133	.031	.012	.033	2.343	121.719	3.780
36	.07343	.037	.012	.038	2.583	121.972	3.788
37	.07547	.043	.011	.044	2.806	124.179	3.856
38	.07751	.049	.011	.050	3.033	128.486	3.990
39	.07955	.055	.010	.056	3.275	134.141	4.166
40	.08159	.061	.011	.062	3.549	139.755	4.340
41	.08363	.069	.012	.070	3.864	143.504	4.457
42	.08567	.076	.012	.077	4.192	144.129	4.476
43	.08771	.085	.014	.086	4.533	139.038	4.318
44	.08975	.095	.014	.096	4.870	126.916	3.941
45	.09179	.106	.014	.107	5.168	106.964	3.322
46	.09383	.118	.013	.119	5.400	79.678	2.474
47	.09587	.129	.013	.130	5.683	46.512	1.444
48	.09791	.141	.011	.142	5.659	8.855	.275
49	.09995	.154	.011	.154	5.642	-31.187	-.969
50	.10199	.166	.010	.166	5.521	-71.503	-2.221
51	.10403	.177	.009	.178	5.313	-111.012	-3.448
52	.10607	.189	.008	.189	5.023	-148.279	-4.605
53	.10811	.200	.005	.200	4.660	-181.552	-5.638
54	.11015	.209	.004	.209	4.238	-210.315	-6.532
55	.11219	.217	.002	.217	3.762	-234.050	-7.269
56	.11423	.224	.000	.224	3.219	-253.012	-7.858
57	.11627	.230	.003	.230	2.652	-267.279	-8.301
58	.11831	.236	.005	.236	2.062	-276.587	-8.590
59	.12035	.240	.007	.240	1.468	-280.366	-8.707
60	.12239	.242	.008	.242	.877	-278.112	-8.637
61	.12443	.243	.009	.243	.283	-270.863	-8.412
62	.12647	.243	.007	.243	-.304	-259.737	-8.066
63	.12851	.241	.006	.241	-.857	-245.002	-7.609
64	.13055	.238	.005	.239	-1.350	-227.813	-7.075

DATE: 9 JUN 77

TEST NUMBER: 1039

RSD STUDY, SUBJECT C-2, BUNIFIA, 76117, NYLON

11 POINT QUADRATIC FIT

## KNEE MOTION RELATIVE TO THE SLED

FRAME NO.	TIME (SEC)	X (FEET)	DISPLACEMENT Z (FEET)	RESULTANT (FFFT)	VELOCITY RESULTANT (FT/SEC)	ACCELERATION RESULTANT (FT/SEC <sup>2</sup> )	ACCELERATION RESULTANT (G)
55	.11219	.235	.005	.235	-1.775	-208.858	-6.486
56	.11349	.230	.005	.231	-2.181	-189.088	-5.872
57	.11477	.225	.005	.225	-2.545	-169.685	-5.270
58	.11601	.219	.006	.220	-2.835	-151.542	-4.706
59	.11725	.214	.007	.214	-3.139	-134.696	-4.183
70	.11849	.207	.007	.207	-3.387	-117.919	-3.662
71	.11973	.199	.006	.199	-3.614	-100.238	-3.113
72	.12097	.192	.003	.192	-3.813	-82.512	-2.562
73	.12221	.184	.001	.184	-3.985	-64.663	-2.008
74	.12345	.175	.002	.175	-4.114	-45.979	-1.428
75	.12469	.167	.004	.167	-4.178	-26.370	-.819
76	.12593	.157	.006	.157	-4.193	-5.130	-.159
77	.12717	.148	.008	.148	-4.187	17.785	.552
78	.12841	.139	.009	.140	-4.147	42.616	1.323
79	.12965	.131	.011	.131	-4.057	69.576	2.161
80	.13089	.123	.012	.123	-3.916	98.592	3.062
81	.13213	.114	.015	.115	-3.710	130.158	4.042
82	.13337	.105	.018	.107	-3.419	163.402	5.075
83	.13461	.097	.021	.100	-3.052	196.468	6.101
84	.13585	.089	.026	.093	-2.599	226.537	7.035
85	.13709	.082	.031	.087	-2.073	251.263	7.803
86	.13833	.075	.037	.084	-1.474	268.483	8.338
87	.13957	.068	.044	.081	-.840	276.352	8.582
88	.14081	.062	.051	.080	-.184	273.507	8.494
89	.14205	.056	.059	.081	.433	260.241	8.082
90	.14329	.050	.065	.083	1.002	237.996	7.391
91	.14453	.044	.074	.086	1.508	208.605	6.478
92	.14577	.036	.082	.090	1.914	174.618	5.423
93	.14701	.030	.093	.095	2.218	138.336	4.296
94	.14825	.024	.097	.100	2.438	102.502	3.183
95	.14949	.019	.104	.106	2.589	68.795	2.136
96	.15073	.016	.111	.112	2.675	38.684	1.201
97	.15197	.012	.117	.118	2.710	14.015	.435
98	.15321	.010	.123	.123	2.670	-5.054	-.157
99	.15445	.008	.128	.128	2.605	-18.798	-.584
100	.15569	.006	.134	.134	2.518	-27.152	-.863
101	.15693	.005	.139	.139	2.413	-30.480	-.947
102	.15817	.003	.144	.144	2.333	-29.412	-.913
103	.15941	.003	.149	.149	2.262	-25.154	-.781
104	.16065	.001	.153	.153	2.206	-19.233	-.597
105	.16189	.000	.157	.157	2.161	-13.173	-.409
106	.16313	.001	.161	.161	2.175	-8.357	-.260
107	.16437	.003	.165	.165	2.185	-5.840	-.181
108	.16561	.006	.170	.170	2.201	-5.089	-.158
109	.16685	.008	.174	.175	2.212	-5.807	-.180
110	.16809	.010	.180	.180	2.204	-7.454	-.231
111	.16933	.013	.184	.185	2.173	-9.077	-.282
112	.17057	.016	.188	.189	2.126	-9.966	-.310
113	.17181	.018	.192	.193	2.085	-9.559	-.297
114	.17305	.020	.196	.197	2.035	-7.923	-.246



DATE: 9 JUN 77 TEST NUMBER: 1039 11 POINT QUADRATIC FIT  
 RSD STUDY, SUBJECT C 2, DUNLOP, 761117, NYLON

KNEE MOTION RELATIVE TO THE SLED

FRAME NO.	TIME (SEC)	DISPLACEMENT			VELOCITY		ACCELERATION	
		X (FEET)	Y (FEET)	Z (FEET)	RESULTANT (FT/SEC)	RESULTANT (G)	RESULTANT (FT/SEC SQ)	RESULTANT (G)
115	23.633	-.022	.200	.204	2.040	-1.168	-5.1417	-1.095
116	23.652	-.024	.213	.204	2.037	-1.095	-5.1417	-1.095
117	23.666	-.026	.217	.209	2.049	-1.060	-5.1417	-1.060
118	23.679	-.028	.211	.213	2.059	-1.068	-5.1417	-1.068
119	23.693	-.030	.216	.218	2.082	-1.119	-5.1417	-1.119
120	23.707	-.032	.220	.222	2.083	-1.205	-5.1417	-1.205
121	23.721	-.034	.223	.226	2.053	-1.317	-5.1417	-1.317
122	23.735	-.036	.227	.230	2.016	-1.450	-5.1417	-1.450
123	23.749	-.040	.231	.235	1.980	-1.584	-5.1417	-1.584
124	23.763	-.042	.235	.239	1.936	-1.698	-5.1417	-1.698
125	23.777	-.045	.239	.243	1.892	-1.803	-5.1417	-1.803
126	23.791	-.047	.241	.246	1.840	-1.899	-5.1417	-1.899
127	23.805	-.048	.245	.250	1.773	-1.910	-5.1417	-1.910
128	23.819	-.049	.249	.254	1.705	-1.144	-5.1417	-1.144
129	23.833	-.051	.252	.257	1.639	-1.296	-5.1417	-1.296
130	23.847	-.051	.256	.261	1.552	-1.482	-5.1417	-1.482
131	23.861	-.052	.258	.264	1.455	-1.699	-5.1417	-1.699
132	23.875	-.052	.261	.267	1.334	-1.946	-5.1417	-1.946
133	23.889	-.052	.264	.269	1.212	-2.221	-5.1417	-2.221
134	23.903	-.052	.267	.272	1.059	-2.500	-5.1417	-2.500
135	23.917	-.051	.269	.274	.889	-2.755	-5.1417	-2.755

MAXIMUM POSITIVE X DISPLACEMENT= .243 AT TIME 126.7

MAXIMUM NEGATIVE X DISPLACEMENT= -.052 AT TIME 26926

MAXIMUM POSITIVE Z DISPLACEMENT= .275 AT TIME 28150

MAXIMUM NEGATIVE Z DISPLACEMENT= -.009 AT TIME 12443

MAXIMUM RESULTANT DISPLACEMENT= .279 AT TIME 28150



DATE: 9 JUN 77

TEST NUMBER: 1039

FSD STUDY, SUBJECT C 2, RUN 010, 761117, NYLON

11 POINT QUADRATIC FIT

## SHOULDER MOTION RELATIVE TO THE SLED

FRAME NO.	TIME (SEC)	DISPLACEMENT		VELOCITY		ACCELERATION	
		X (FEET)	Z (FEET)	RESULTANT (FT/SEC)	RESULTANT (FT/SEC SQ)	RESULTANT (G)	RESULTANT (G)
15	.03030	-.002	-.002	-.056	-4.115	-4.128	-4.128
16	.03254	-.002	-.003	.044	-9.131	-9.284	-9.284
17	.03468	-.001	-.002	.024	-10.270	-10.334	-10.334
18	.03672	-.001	-.002	-.038	-9.515	-9.295	-9.295
19	.03875	-.000	-.002	-.084	-6.202	-6.193	-6.193
20	.04090	-.000	-.002	-.114	-2.008	-.062	-.062
21	.04234	.000	-.002	-.111	2.901	.890	.890
22	.04438	.001	-.001	-.072	8.876	.276	.276
23	.04632	.000	-.000	-.034	15.337	.495	.495
24	.04836	.000	-.000	.005	22.730	.706	.706
25	.05100	-.001	-.001	.050	30.126	.936	.936
26	.05374	-.001	-.001	.099	39.148	1.216	1.216
27	.05538	-.001	-.001	.169	51.442	1.598	1.598
28	.05712	-.002	-.002	.267	67.981	2.111	2.111
29	.05916	-.001	-.002	.378	88.829	2.759	2.759
30	.06120	.000	-.003	.543	113.012	3.510	3.510
31	.06324	.001	-.003	.778	139.404	4.329	4.329
32	.06528	.004	-.002	1.099	155.775	5.148	5.148
33	.06731	.007	-.003	1.485	190.527	5.947	5.947
34	.06935	.010	-.003	1.944	212.168	6.589	6.589
35	.07139	.014	-.003	2.443	228.128	7.103	7.103
36	.07343	.019	-.003	2.975	239.342	7.433	7.433
37	.07547	.026	-.003	3.501	243.666	7.567	7.567
38	.07751	.034	-.004	4.024	242.515	7.532	7.532
39	.07955	.043	-.003	4.539	236.311	7.339	7.339
40	.08159	.053	-.003	5.032	226.357	7.030	7.030
41	.08363	.064	-.002	5.497	213.376	6.627	6.627
42	.08557	.076	-.001	5.924	198.278	6.158	6.158
43	.08771	.089	-.001	6.322	180.363	5.601	5.601
44	.08975	.102	-.002	6.677	159.615	4.957	4.957
45	.09179	.116	-.003	6.996	135.961	4.222	4.222
46	.09383	.131	-.003	7.272	109.871	3.412	3.412
47	.09587	.146	-.005	7.504	81.296	2.525	2.525
48	.09791	.162	-.006	7.652	49.575	1.540	1.540
49	.09995	.178	-.006	7.727	14.353	-.446	-.446
50	.10199	.195	-.006	7.720	-24.825	-2.771	-2.771
51	.10403	.211	-.006	7.656	-67.656	-2.101	-2.101
52	.10607	.228	-.005	7.510	-113.935	-3.538	-3.538
53	.10811	.242	-.005	7.260	-163.036	-5.063	-5.063
54	.11015	.257	-.005	6.892	-214.259	-6.654	-6.654
55	.11219	.271	-.004	6.403	-264.813	-8.224	-8.224
56	.11423	.285	-.004	5.801	-310.396	-9.640	-9.640
57	.11627	.298	-.004	5.076	-345.747	-10.737	-10.737
58	.11831	.308	-.004	4.232	-366.893	-11.394	-11.394
59	.12035	.316	-.003	3.305	-371.123	-11.526	-11.526
60	.12239	.322	-.002	2.375	-358.020	-11.119	-11.119
61	.12443	.326	-.002	1.536	-329.300	-10.227	-10.227
62	.12647	.327	-.002	.836	-288.477	-8.959	-8.959
63	.12851	.325	-.002	.285	-241.419	-7.497	-7.497
64	.13055	.323	-.003	-.101	-195.804	-6.081	-6.081

DATE: 9 JUN 77

TEST NUMBER: 1039

11 POINT QUADRATIC FIT

RSD STUDY, SUBJECT C-2, RUN#139, 76117, NYLON

## SHOULDER MOTION RELATIVE TO THE SLED

FRAME NO.	TIME (SEC)	X (FEET)	DISPLACEMENT Z (FEET)	VELOCITY RESULTANT (FT/SEC)	ACCELERATION RESULTANT (FT/SEC SQ)	ACCELERATION RESULTANT (G)
55	13259	.322	-.004	.322	-157.742	-4.899
56	13263	.322	-.005	.322	-130.516	-4.053
57	13267	.321	-.006	.321	-113.790	-3.524
58	13271	.320	-.007	.320	-105.289	-3.270
59	13275	.319	-.008	.320	-99.498	-3.090
60	13279	.318	-.011	.318	-94.916	-2.948
61	13283	.315	-.013	.315	-86.535	-2.687
62	13287	.311	-.015	.311	-74.518	-2.344
63	13291	.305	-.020	.306	-60.900	-1.891
64	13295	.299	-.025	.299	-49.199	-1.525
65	13299	.294	-.030	.294	-41.307	-1.283
66	13303	.289	-.035	.291	-37.424	-1.162
67	13307	.284	-.039	.287	-35.844	-1.113
68	13311	.280	-.043	.283	-33.930	-1.054
69	13315	.275	-.047	.279	-28.625	-.889
70	13319	.270	-.050	.275	-17.184	-.534
71	13323	.264	-.053	.268	1.184	.037
72	13327	.258	-.054	.264	26.080	.809
73	13331	.251	-.056	.258	54.801	1.702
74	13335	.244	-.057	.251	83.554	2.595
75	13339	.238	-.057	.244	108.599	3.373
76	13343	.232	-.055	.238	126.882	3.940
77	13347	.224	-.051	.234	138.337	4.296
78	13351	.226	-.047	.231	143.881	4.468
79	13355	.225	-.042	.228	145.256	4.511
80	13359	.224	-.035	.227	144.649	4.492
81	13363	.224	-.029	.226	143.961	4.471
82	13367	.224	-.020	.225	142.442	4.454
83	13371	.224	-.013	.224	142.569	4.458
84	13375	.223	-.004	.223	139.782	4.339
85	13379	.223	.005	.223	132.401	4.112
86	13383	.223	.015	.224	118.392	3.677
87	13387	.224	.025	.225	97.058	3.014
88	13391	.227	.035	.229	70.215	2.181
89	13395	.229	.046	.234	40.516	1.258
90	13399	.232	.054	.238	-18.378	-.571
91	13403	.234	.064	.242	-43.083	-1.338
92	13407	.236	.073	.246	-62.668	-1.946
93	13411	.237	.082	.250	-76.848	-2.388
94	13415	.237	.089	.253	-86.867	-2.698
95	13419	.237	.096	.256	-94.892	-2.947
96	13423	.236	.103	.258	-102.844	-3.194
97	13427	.234	.107	.259	-109.915	-3.414
98	13431	.235	.111	.262	-114.866	-3.567
99	13435	.238	.114	.264	-117.033	-3.636
100	13439	.238	.117	.265	-115.903	-3.599
101	13443	.236	.121	.265	-110.584	-3.434
102	13447	.234	.124	.265	-100.881	-3.133
103	13451	.231	.127	.264		
104	13455	.228	.130	.263		

DATE: 9 JUN 77 TEST NUMBER: 1039 11 POINT QUADRATIC FIT  
 RSO STUDY, SUBJECT C 2, PUNIC19, 76117, NYLON

SHOULDER MOTION RELATIVE TO THE SLED

FRAME NO.	TIME (SEC)	DISPLACEMENT		VELOCITY		ACCELERATION	
		X (FEET)	Z (FEET)	RESULTANT (FT/SEC)	RESULTANT (FT/SEC SQ)	ACCELERATION RESULTANT (G)	ACCELERATION RESULTANT
115	23458	.224	.134	.261	.936	.87184	-2.708
116	23652	.220	.135	.258	-1.173	-70.481	-2.189
117	23856	.215	.135	.254	-1.298	-51.292	-1.655
118	24070	.212	.134	.251	-1.363	-38.769	-1.204
119	24274	.209	.135	.249	-1.389	-28.271	-.878
120	24478	.206	.135	.246	-1.387	-20.996	-.652
121	24682	.202	.134	.242	-1.390	-18.886	-.524
122	24896	.199	.134	.240	-1.403	-16.993	-.528
123	25030	.196	.135	.238	-1.462	-26.223	-.628
124	25234	.193	.134	.235	-1.516	-24.512	-.761
125	25438	.190	.134	.233	-1.551	-28.718	-.892
126	25702	.187	.131	.228	-1.604	-31.755	-.986
127	25906	.184	.128	.224	-1.703	-33.273	-1.033
128	26110	.181	.126	.221	-1.799	-33.678	-1.046
129	26314	.179	.124	.218	-1.868	-33.109	-1.028
130	26518	.177	.122	.215	-1.934	-30.796	-.956
131	26722	.173	.119	.210	-1.993	-25.918	-.805
132	26926	.169	.117	.206	-2.054	-19.394	-.602
133	27130	.165	.115	.201	-2.112	-12.980	-.403
134	27334	.161	.113	.197	-2.139	-7.497	-.233
135	27538	.156	.112	.192	-2.132	-2.926	-.091

MAXIMUM POSITIVE X DISPLACEMENT= .327 AT TIME .12647

MAXIMUM NEGATIVE X DISPLACEMENT= -.002 AT TIME .03254

MAXIMUM POSITIVE Z DISPLACEMENT= .135 AT TIME .23662

MAXIMUM NEGATIVE Z DISPLACEMENT= -.057 AT TIME .17135

MAXIMUM RESULTANT DISPLACEMENT= .327 AT TIME .12647



DATE: 9 JUN 77

TEST NUMBER: 1039

ESD STUDY, SUBJECT C-2, RUN 19, 24117, NYLON

11 POINT QUADRATIC FIT

## FLOW MOTION RELATIVE TO THE SLED

FRAME NO.	TIME (SEC)	X (FEET)	DISPLACEMENT (FEET)	VELOCITY RESULTANT (FT/SEC)	ACCELERATION RESULTANT (FT/SEC <sup>2</sup> )	ACCELERATION RESULTANT (G)
15	.01030	.002	.004	.005	4.041	.125
16	.01264	.003	.007	.004	10.385	.323
17	.01498	.003	.003	.005	14.465	.449
18	.01732	.003	.003	.004	16.049	.498
19	.01966	.003	.003	.004	15.073	.468
20	.02200	.002	.004	.005	12.466	.387
21	.02434	.002	.003	.005	9.756	.303
22	.02668	.003	.005	.006	8.390	.261
23	.02902	.003	.006	.007	10.232	.318
24	.03136	.003	.006	.007	16.397	.509
25	.03370	.004	.006	.007	28.971	.898
26	.03604	.004	.006	.007	41.785	1.298
27	.03838	.004	.006	.007	60.593	1.882
28	.04072	.005	.005	.007	82.651	2.567
29	.04306	.006	.005	.008	106.783	3.314
30	.04540	.006	.005	.009	131.499	4.084
31	.04774	.006	.005	.010	155.530	4.849
32	.05008	.007	.005	.012	177.671	5.518
33	.05242	.007	.004	.016	197.469	6.133
34	.05476	.007	.003	.020	214.387	6.658
35	.05710	.007	.002	.025	227.782	7.023
36	.05944	.007	.002	.031	237.077	7.383
37	.06178	.007	.002	.038	242.048	7.518
38	.06412	.007	.001	.047	243.494	7.562
39	.06646	.006	.001	.056	242.246	7.524
40	.06880	.006	.001	.067	239.071	7.425
41	.07114	.006	.001	.078	234.928	7.296
42	.07348	.005	.000	.091	230.971	7.173
43	.07582	.004	.000	.105	228.427	7.054
44	.07816	.004	.000	.119	226.107	7.084
45	.08050	.003	.001	.134	229.467	7.127
46	.08284	.003	.001	.150	231.425	7.187
47	.08518	.003	.001	.166	232.602	7.224
48	.08752	.003	.002	.184	231.449	7.188
49	.08986	.003	.002	.204	228.685	7.039
50	.09220	.003	.001	.223	216.990	6.739
51	.09454	.002	.001	.244	201.379	6.254
52	.09688	.002	.000	.267	179.698	5.581
53	.09922	.002	.000	.291	153.424	4.766
54	.10156	.003	.003	.315	126.822	3.876
55	.10390	.005	.005	.339	98.436	2.997
56	.10624	.008	.008	.364	70.666	2.195
57	.10858	.011	.011	.389	49.486	1.537
58	.11092	.014	.014	.415	34.376	1.068
59	.11326	.017	.017	.440	26.356	.819
60	.11560	.022	.022	.464	24.517	.762
61	.11794	.027	.027	.488	26.053	.809
62	.12028	.032	.032	.513	27.528	.855
63	.12262	.036	.036	.538	25.968	.806
64	.12496	.047	.047	.562	18.596	.578



DATE: 9 JUN 77 TEST NUMBER: 1039 11 POINT QUADRATIC FIT  
 PSD STUDY SUBJECT C. 2. 20N1033, 751117, NYLON

ELROW MOTION RELATIVE TO THE SLED

FRAME NO.	TIME (SEC)	DISPLACEMENT X (FEET)	DISPLACEMENT Z (FEET)	VELOCITY RESULTANT (FT/SEC)	ACCELERATION RESULTANT (FT/SEC SQ)	ACCELERATION RESULTANT (G)
65	13.233	.524	.556	12.548	3.622	.112
66	13.453	.610	.613	12.630	-19.692	-.612
67	13.657	.636	.640	12.574	-50.292	-1.562
68	13.871	.661	.667	12.466	-85.636	-2.660
69	14.025	.686	.694	12.246	-123.140	-3.824
70	14.279	.709	.719	11.927	-159.528	-4.954
71	14.433	.731	.743	11.512	-193.236	-6.001
72	14.637	.751	.766	11.036	-224.273	-6.965
73	14.831	.770	.788	10.529	-253.476	-7.872
74	15.035	.788	.808	9.989	-281.772	-8.751
75	15.239	.804	.829	9.423	-310.435	-9.641
76	15.453	.819	.848	8.830	-339.601	-10.547
77	15.677	.833	.865	8.208	-368.507	-11.444
78	15.911	.845	.882	7.559	-394.888	-12.264
79	16.115	.856	.897	6.883	-416.008	-12.920
80	16.319	.864	.910	6.185	-429.308	-13.333
81	16.523	.870	.920	5.464	-432.666	-13.735
82	16.727	.875	.929	4.727	-425.520	-13.215
83	16.931	.877	.934	3.982	-408.826	-12.696
84	17.135	.877	.930	3.230	-385.009	-11.957
85	17.339	.875	.930	2.479	-357.499	-11.102
86	17.543	.872	.927	1.726	-329.216	-10.224
87	17.747	.869	.920	1.000	-302.835	-9.405
88	17.951	.866	.916	.327	-278.902	-8.662
89	18.155	.862	.916	-.343	-256.870	-7.977
90	18.359	.857	.914	-1.055	-235.624	-7.318
91	18.563	.851	.913	-1.759	-213.666	-6.636
92	18.767	.844	.910	-2.430	-189.684	-5.891
93	18.971	.836	.906	-3.083	-163.739	-5.085
94	19.175	.828	.900	-3.710	-136.728	-4.246
95	19.379	.819	.891	-4.317	-110.218	-3.423
96	19.583	.810	.883	-4.903	-86.163	-2.676
97	19.785	.801	.874	-5.466	-65.617	-2.038
98	19.990	.792	.866	-6.013	-49.752	-1.545
99	20.194	.782	.857	-6.544	-38.136	-1.184
100	20.398	.773	.850	-7.059	-29.757	-.924
101	20.602	.765	.841	-7.559	-23.591	-.720
102	20.806	.756	.831	-8.042	-16.243	-.504
103	21.010	.747	.823	-8.509	-6.753	-.210
104	21.214	.738	.815	-8.959	6.060	.188
105	21.418	.728	.806	-9.390	22.345	.594
106	21.622	.719	.806	-9.751	41.291	1.282
107	21.826	.708	.806	-10.042	61.546	1.911
108	22.030	.699	.806	-10.271	81.494	2.531
109	22.234	.689	.806	-10.439	99.874	3.102
110	22.438	.682	.806	-10.548	115.708	3.593
111	22.642	.673	.806	-10.600	128.206	3.982
112	22.846	.666	.806	-10.606	136.388	4.236
113	23.050	.658	.806	-10.555	140.616	4.367
114	23.254	.650	.806	-10.448	141.088	4.382

DATE: 9 JUN 77

TEST NUMBER: 1099

RSD STUDY, SUBJECT C-2, RUN 1039, 764447, NYLON

14 POINT QUADRATIC FIT

## FLBOM MOTION RELATIVE TO THE SLED

FRAME NO.	TIME (SEC)	X (FEET)	Z (FEET)	DISPLACEMENT RESULTANT (FEET)	VELOCITY RESULTANT (FT/SEC)	ACCELERATION RESULTANT (FT/SEC SQ)	ACCELERATION RESULTANT (G)
115	.23458	.644	.367	.741	-2.141	137.829	4.280
116	.23652	.639	.368	.737	-1.846	131.894	4.096
117	.23846	.634	.370	.734	-1.578	124.814	3.851
118	.24070	.629	.372	.731	-1.317	114.974	3.571
119	.24274	.626	.373	.729	-1.090	105.419	3.274
120	.24478	.624	.375	.728	-.899	95.998	2.981
121	.24682	.620	.376	.725	-.725	87.133	2.706
122	.24886	.618	.378	.724	-.569	78.204	2.429
123	.25090	.615	.381	.724	-.424	68.750	2.135
124	.25294	.613	.383	.723	-.282	59.007	1.833
125	.25498	.610	.386	.722	-.149	48.545	1.508
126	.25702	.609	.388	.722	-.032	37.617	1.168
127	.25906	.607	.391	.722	.032	26.904	.836
128	.26110	.606	.394	.723	.062	17.203	.534
129	.26314	.605	.397	.724	.065	9.113	.283
130	.26518	.605	.399	.724	.036	3.098	.096
131	.26722	.604	.399	.724	.012	-.857	-.827
132	.26926	.603	.400	.724	-.005	-3.271	-1.02
133	.27130	.602	.401	.723	-.003	-5.593	-1.74
134	.27334	.601	.401	.722	.008	-9.365	-2.91
135	.27538	.599	.403	.722	.017	-16.962	-4.99

MAXIMUM POSITIVE X DISPLACEMENT= .877 AT TIME .16931

MAXIMUM NEGATIVE X DISPLACEMENT= .002 AT TIME .02244

MAXIMUM POSITIVE Z DISPLACEMENT= .411 AT TIME .28558

MAXIMUM NEGATIVE Z DISPLACEMENT= -.002 AT TIME .09791

MAXIMUM RESULTANT DISPLACEMENT= .939 AT TIME .17747

DATE: 9 JUN 77

TEST NUMBER: 1039

RSD STUDY, SUBJECT C-2, RUN 1013, 761117, NYLON

11 POINT QUADRATIC FIT

## HEAD PT. 1 MOTION RELATIVE TO THE SLED

FRAME NO.	TIME (SEC)	DISPLACEMENT		VELOCITY RESULTANT (FT/SEC)	ACCELERATION RESULTANT (FT/SEC SO)	ACCELERATION RESULTANT (G)
		X (FEET)	Z (FEET)			
15	.03050	-.005	-.001	.005	-.027	-.409
16	.03254	-.008	-.001	.008	-.17596	-.546
17	.03458	-.008	-.002	.008	-.110	-.501
18	.03672	-.006	-.002	.007	-.194	-.266
19	.03876	-.004	-.003	.005	-.246	-.077
20	.04090	-.002	-.003	.004	13.525	.420
21	.04237	.001	-.003	.003	22.749	.706
22	.04438	-.001	-.002	.002	28.476	.884
23	.04642	-.001	-.002	.002	28.365	.881
24	.04835	-.001	-.003	.003	21.059	.654
25	.05130	-.003	-.002	.004	9.690	.301
26	.05314	-.006	-.001	.006	-1.951	-.061
27	.05538	-.007	-.001	.007	-6.884	-.214
28	.05712	-.007	-.001	.008	-.508	-.016
29	.05916	-.007	-.001	.007	19.894	.618
30	.06120	-.006	-.001	.006	53.184	1.652
31	.06324	-.007	-.001	.007	96.447	2.995
32	.06528	-.006	-.001	.006	148.191	4.602
33	.06731	-.003	-.002	.003	203.121	6.314
34	.06935	-.001	-.001	.001	253.032	7.858
35	.07139	.003	-.003	.004	289.413	8.988
36	.07343	.008	-.004	.009	310.727	9.650
37	.07547	.016	-.005	.017	315.880	9.810
38	.07751	.024	-.006	.025	309.415	9.609
39	.07955	.035	-.006	.035	293.680	9.120
40	.08159	.045	-.007	.045	272.927	8.476
41	.08363	.056	-.006	.056	249.993	7.764
42	.08557	.069	-.006	.070	227.216	7.056
43	.08771	.082	-.005	.082	209.293	6.500
44	.08975	.095	-.007	.095	197.013	6.118
45	.09173	.110	-.009	.111	188.244	5.846
46	.09333	.126	-.010	.127	180.634	5.610
47	.09537	.142	-.012	.143	172.674	5.363
48	.09731	.159	-.014	.160	161.165	5.005
49	.09935	.176	-.015	.177	143.539	4.458
50	.10139	.194	-.015	.195	116.711	3.625
51	.10403	.214	-.016	.214	78.612	2.441
52	.10607	.234	-.018	.235	28.897	.897
53	.10811	.254	-.021	.255	-31.563	-.980
54	.11015	.275	-.023	.276	-99.233	-3.082
55	.11213	.296	-.022	.297	-169.726	-5.271
56	.11423	.317	-.024	.318	-236.021	-7.330
57	.11627	.336	-.027	.337	-249.670	-8.996
58	.11831	.353	-.030	.355	-325.095	-10.096
59	.12035	.368	-.032	.369	-338.264	-10.505
60	.12239	.380	-.034	.381	-329.459	-10.232
61	.12443	.389	-.040	.391	-301.676	-9.369
62	.12647	.397	-.044	.400	-261.063	-8.108
63	.12851	.402	-.051	.406	-214.897	-6.674
64	.13055	.407	-.056	.411	-171.199	-5.317



DATE: 9 JUN 77

TEST NUMBER: 1039

RSD STUDY, SUBJECT C-2, SUMMIT 13, 754117, NYLON

11 POINT QUADRATIC FIT

MOTION RELATIVE TO THE SLED

FRAME NO.	TIME (SEC)	X (FEET)	Y (FEET)	DISPLACEMENT RESULTANT (FEET)	VELOCITY RESULTANT (FT/SEC SQ)	ACCELERATION RESULTANT (FT/SEC SQ)	ACCELERATION RESULTANT (G)
64	13230	.412	-.031	.416	3.348	-137.142	-4.259
65	13633	.418	-.059	.424	3.238	-115.890	-3.599
66	13637	.430	-.077	.432	3.133	-105.565	-3.274
67	13641	.430	-.085	.439	2.992	-101.818	-3.162
68	13871	.430	-.085	.439	2.992	-101.818	-3.162
69	14023	.436	-.032	.446	2.762	-100.242	-3.112
70	14273	.441	-.100	.452	2.444	-95.678	-2.971
71	14433	.444	-.109	.457	2.123	-85.413	-2.653
72	14637	.445	-.116	.460	1.873	-57.850	-2.107
73	14831	.445	-.126	.462	1.717	-44.863	-1.393
74	15035	.444	-.133	.464	1.574	-20.569	-.639
75	15239	.444	-.139	.465	1.733	-33.9	-.611
76	15437	.444	-.147	.469	1.952	10.937	.340
77	15631	.449	-.153	.474	2.012	12.121	.376
78	15811	.451	-.160	.479	2.130	5.193	.161
79	16013	.456	-.166	.485	2.162	-6.219	-.193
80	16319	.459	-.173	.490	2.039	-17.425	-.541
81	16623	.464	-.178	.495	1.936	-24.442	-.759
82	16727	.465	-.182	.499	1.795	-24.628	-.765
83	16931	.465	-.187	.504	1.630	-16.580	-.515
84	17135	.467	-.188	.503	1.567	-2.108	-.065
85	17339	.469	-.194	.505	1.539	14.175	.440
86	17543	.472	-.187	.508	1.700	27.123	.842
87	17747	.476	-.185	.511	1.858	33.459	1.039
88	17951	.481	-.194	.515	2.037	31.478	.978
89	18155	.488	-.182	.521	2.188	21.921	.681
90	18359	.494	-.132	.566	2.243	7.701	.239
91	18563	.497	-.174	.531	2.197	-7.790	-.242
92	18757	.507	-.177	.537	2.106	-21.176	-.658
93	18921	.512	-.174	.541	1.970	-29.561	-.918
94	19175	.518	-.159	.505	1.834	-32.146	-.998
95	19379	.522	-.163	.507	1.741	-30.064	-.934
96	19583	.526	-.157	.509	1.681	-26.988	-.838
97	19786	.531	-.153	.513	1.670	-26.362	-.819
98	19990	.536	-.149	.516	1.699	-30.101	-.935
99	20194	.541	-.146	.520	1.713	-39.769	-1.235
100	20398	.546	-.142	.524	1.676	-54.443	-1.691
101	20602	.551	-.136	.528	1.552	-72.108	-2.239
102	20805	.557	-.134	.532	1.360	-89.571	-2.782
103	21010	.561	-.129	.536	1.195	-103.348	-3.210
104	21214	.565	-.123	.538	.802	-111.077	-3.450
105	21418	.566	-.117	.538	.507	-112.624	-3.498
106	21622	.567	-.112	.538	.219	-109.219	-3.392
107	21826	.568	-.108	.539	-.004	-102.560	-3.185
108	22030	.568	-.104	.538	-.162	-94.267	-2.928
109	22234	.567	-.100	.536	-.292	-87.212	-2.708
110	22438	.568	-.097	.536	-.429	-82.845	-2.573
111	22642	.567	-.093	.531	-.591	-81.008	-2.516
112	22846	.568	-.091	.535	-.750	-81.627	-2.535
113	23050	.567	-.088	.534	-.907	-82.862	-2.573
114	23254	.565	-.084	.532	-1.110	-83.046	-2.579



DATE: 9 JUN 77

TEST NUMBER: 1039

RSD STUDY, SUBJECT C. 2, RUN 1139, 764117, NYLON

11 POINT QUADRATIC FIT

## HEAD PT. 1 MOTION RELATIVE TO THE SLED

FRAME NO.	TIME (SEC)	DISPLACEMENT X (FEET)	DISPLACEMENT Z (FEET)	VELOCITY RESULTANT (FT/SEC)	ACCELERATION RESULTANT (FT/SEC SQ)	ACCELERATION RESULTANT (G)
115	23438	.562	-.050	-1.310	-82.157	-2.551
116	23652	.559	-.079	.565	-80.630	-2.504
117	23856	.557	-.076	.562	-78.566	-2.440
118	24070	.553	-.075	.558	-75.429	-2.343
119	24274	.549	-.073	.553	-71.008	-2.205
120	24478	.545	-.072	.550	-66.055	-2.051
121	24632	.542	-.071	.546	-60.449	-1.877
122	24836	.538	-.069	.543	-54.625	-1.696
123	25030	.533	-.066	.537	-48.694	-1.512
124	25234	.528	-.064	.531	-43.193	-1.341
125	25438	.524	-.061	.525	-38.902	-1.211
126	25712	.516	-.050	.519	-37.277	-1.158
127	25906	.511	-.057	.514	-37.666	-1.170
128	26110	.505	-.056	.508	-38.884	-1.208
129	26314	.500	-.053	.503	-39.374	-1.223
130	26518	.496	-.052	.499	-38.066	-1.182
131	26722	.491	-.052	.493	-32.855	-1.031
132	26926	.484	-.050	.486	-23.197	-.720
133	27130	.476	-.049	.479	-11.059	-.304
134	27334	.469	-.048	.471	1.538	.048
135	27538	.460	-.044	.463	11.955	.371

MAXIMUM POSITIVE X DISPLACEMENT= .568 AT TIME .21826

MAXIMUM NEGATIVE X DISPLACEMENT= -.008 AT TIME .03264

MAXIMUM POSITIVE Z DISPLACEMENT= .002 AT TIME .02244

MAXIMUM NEGATIVE Z DISPLACEMENT= -.188 AT TIME .17339

MAXIMUM RESULTANT DISPLACEMENT= .579 AT TIME .21826

DATE: 9 JUN 77

TEST NUMBER: 1029

RSD STUDY, SUBJECT C-2, RUN#13, 25117, NYLON

11 POINT QUADRATIC FIT

## HEAD PM. 2 MOTION RELATIVE TO THE SLED

FRAME NO.	TIME (SEC)	X (FEET)	DISPLACEMENT Z (FEET)	VELOCITY RESULTANT (FT/SEC)	ACCELERATION RESULTANT (FT/SEC SQ)	ACCELERATION RESULTANT (G)
15	.03652	-.032	.015	.042	-.92.825	-2.884
16	.03254	-.020	.014	-.130	-.61.569	-1.912
17	.03454	-.029	.014	-.165	-.29.260	-.909
18	.03572	-.129	.013	-.082	-.1.757	-.055
19	.03875	-.029	.013	-.061	17.246	.536
20	.04030	-.029	.013	.167	25.571	.794
21	.04234	-.130	.013	.284	23.688	.736
22	.04388	-.031	.014	.359	14.279	.443
23	.04632	-.032	.015	.376	.446	.014
24	.04935	-.033	.015	.341	-.14.158	-.440
25	.05199	-.034	.015	.367	-.28.211	-.876
26	.05394	-.034	.015	.169	-.42.291	-1.313
27	.05518	-.035	.015	.063	-.56.170	-1.744
28	.05712	-.034	.015	-.055	-.69.863	-2.170
29	.05915	-.034	.015	-.067	-.83.934	-2.607
30	.06120	-.033	.015	-.331	-.93.935	-2.917
31	.06224	-.033	.015	-.338	-.58.101	-2.894
32	.06529	-.033	.014	-.810	-.75.189	-2.335
33	.06731	-.032	.013	-.110	-.35.829	-1.113
34	.06935	-.030	.012	-.142	25.972	.807
35	.07139	-.027	.011	-.179	18.862	.381
36	.07343	-.022	.010	-.193	206.484	6.413
37	.07547	-.017	.009	-.234	309.896	9.624
38	.07751	-.011	.007	.052	407.000	12.640
39	.07955	-.003	.007	1.198	445.496	15.078
40	.08159	.107	.007	2.529	531.603	16.509
41	.08363	.019	.007	3.926	542.655	16.853
42	.08557	.033	.006	5.286	555.035	16.305
43	.08771	.048	.006	6.494	487.705	15.146
44	.08975	.064	.006	7.480	440.468	13.679
45	.09179	.081	.005	8.143	391.865	12.170
46	.09393	.098	.003	8.651	348.878	10.835
47	.09587	.116	.000	9.187	315.534	9.800
48	.09731	.134	-.004	9.748	292.683	9.090
49	.09935	.154	-.007	10.357	276.734	8.594
50	.10139	.175	-.010	10.981	260.219	8.081
51	.10433	.197	-.013	11.592	242.658	7.225
52	.10607	.224	-.016	12.163	188.147	5.843
53	.10841	.249	-.019	12.646	127.941	3.975
54	.11015	.277	-.020	12.980	55.129	1.712
55	.11219	.304	-.020	13.369	-.23.537	-.733
56	.11423	.332	-.024	12.895	-.90.165	-3.080
57	.11627	.359	-.027	12.475	-.161.757	-5.024
58	.11831	.387	-.032	11.894	-.201.833	-6.268
59	.12035	.412	-.039	11.193	-.211.545	-6.570
60	.12239	.432	-.046	10.488	-.188.656	-5.859
61	.12443	.451	-.056	9.937	-.138.184	-4.288
62	.12647	.467	-.067	9.541	-.67.621	-2.100
63	.12851	.480	-.082	9.456	11.201	.348
64	.13055	.491	-.097	9.698	84.819	2.634

DATE: 9 JUN 77

TEST NUMBER: 1033

11 POINT QUADRATIC FIT

RSD STUDY, SUBJECT C-2, RUN 133, 761117, NYLON

HEAD PT. 2 RELATIVE TO THE SLED

FRAME NO.	TIME (SEC)	DISPLACEMENT		VELOCITY RESULTANT (FT/SEC)	ACCELERATION RESULTANT (FT/SEC <sup>2</sup> )	ACCELERATION RESULTANT (G)
		X (FEET)	Y (FEET)			
55	1323	509	-114	10.171	340.843	4.368
56	1343	526	-134	10.744	169.821	5.274
57	1363	545	-154	11.381	168.549	5.234
58	1381	568	-171	11.956	138.347	4.296
59	1403	587	-202	12.317	88.326	2.743
70	1423	503	-232	12.444	30.041	.933
71	1443	619	-263	12.344	-27.118	-.842
72	1463	535	-293	12.046	-76.164	-2.365
73	1483	648	-324	11.615	-112.669	-3.499
74	1503	658	-353	11.242	-137.034	-4.256
75	1523	668	-381	10.938	-154.854	-4.800
76	1553	678	-406	10.670	-171.809	-5.336
77	1573	688	-427	10.446	-194.255	-6.033
78	1591	697	-447	10.184	-226.650	-7.039
79	1613	703	-481	9.739	-270.946	-8.414
80	1631	710	-508	9.243	-320.570	-9.956
81	1653	718	-534	8.488	-367.530	-11.414
82	1673	726	-558	7.583	-404.045	-12.548
83	1691	727	-579	6.541	-421.920	-13.103
84	1713	727	-596	5.424	-418.328	-12.992
85	1733	726	-610	4.394	-394.625	-12.255
86	1753	726	-619	3.508	-355.213	-11.031
87	1772	726	-625	2.814	-306.070	-9.530
88	1791	727	-630	2.348	-255.345	-7.930
89	1813	732	-632	2.005	-206.857	-6.424
90	1833	736	-632	1.734	-166.884	-5.183
91	1853	744	-630	1.494	-137.219	-4.261
92	1873	749	-628	1.251	-116.947	-3.632
93	1891	755	-625	1.033	-103.636	-3.219
94	1913	761	-620	.836	-94.685	-2.941
95	1933	766	-615	.653	-89.784	-2.788
96	1953	772	-608	.472	-89.380	-2.776
97	1973	778	-600	.329	-94.405	-2.932
98	1993	785	-594	.214	-104.572	-3.248
99	2013	792	-587	.058	-117.941	-3.663
100	2033	799	-577	-.171	-132.966	-4.129
101	2053	806	-567	-.482	-148.805	-4.615
102	2073	811	-559	-.881	-162.853	-5.058
103	2101	816	-550	-1.295	-172.092	-5.344
104	2121	819	-539	-1.686	-173.720	-5.395
105	2143	821	-528	-2.057	-167.858	-5.213
106	2162	821	-515	-2.456	-155.586	-4.832
107	2185	822	-503	-2.739	-139.386	-4.329
108	2203	822	-493	-3.056	-122.659	-3.809
109	2223	822	-481	-3.254	-106.777	-3.316
110	2243	822	-467	-3.425	-91.705	-2.848
111	2262	820	-454	-3.559	-79.478	-2.468
112	2285	817	-443	-3.686	-71.910	-2.233
113	2303	816	-432	-3.825	-68.343	-2.122
114	2323	812	-419	-3.955	-66.521	-2.066



DATE: 9 JUN 77 TEST NUMBER: 1039 11 POINT QUADRATIC FIT  
 PSD STUDY, SUBJECT C 2, RUN#039, 761117, NYLON

HEAD PT. 2 ON RELATIVE TO THE SLED

FRAME NO.	TIME (SEC)	X (FEET)	Y (FEET)	Z (FEET)	DISPLACEMENT RESULTANT (FEET)	VELOCITY RESULTANT (FT/SEC)	ACCELERATION RESULTANT (FT/SEC SQ)	ACCELERATION RESULTANT (G)
115	23.453	.800	.806	.806	.806	-4.035	-65.296	-2.028
116	23.652	.806	.806	.806	.806	-4.198	-62.992	-1.956
117	23.856	.801	.801	.801	.801	-4.367	-58.279	-1.810
118	24.070	.795	.795	.795	.795	-4.517	-49.322	-1.532
119	24.274	.784	.784	.784	.784	-4.630	-35.453	-1.101
120	24.479	.781	.781	.781	.781	-4.734	-16.505	-.513
121	24.682	.772	.772	.772	.772	-4.777	6.544	.206
122	24.895	.763	.763	.763	.763	-4.779	30.165	.937
123	25.090	.755	.755	.755	.755	-4.679	49.883	1.552
124	25.294	.747	.747	.747	.747	-4.490	63.385	1.968
125	25.499	.739	.739	.739	.739	-4.248	68.152	2.117
126	25.702	.732	.732	.732	.732	-3.989	63.344	1.967
127	25.905	.723	.723	.723	.723	-3.787	50.262	1.561
128	26.110	.718	.718	.718	.718	-3.669	30.516	.948
129	26.314	.713	.713	.713	.713	-3.636	8.952	.278
130	26.519	.710	.710	.710	.710	-3.712	-10.324	-.321
131	26.722	.702	.702	.702	.702	-3.833	-22.944	-.713
132	26.926	.695	.695	.695	.695	-3.973	-28.485	-.885
133	27.130	.686	.686	.686	.686	-4.109	-28.448	-.883
134	27.334	.678	.678	.678	.678	-4.176	-25.637	-.796
135	27.538	.668	.668	.668	.668	-4.199	-22.713	-.705

MAXIMUM POSITIVE X DISPLACEMENT= .822 AT TIME .22030

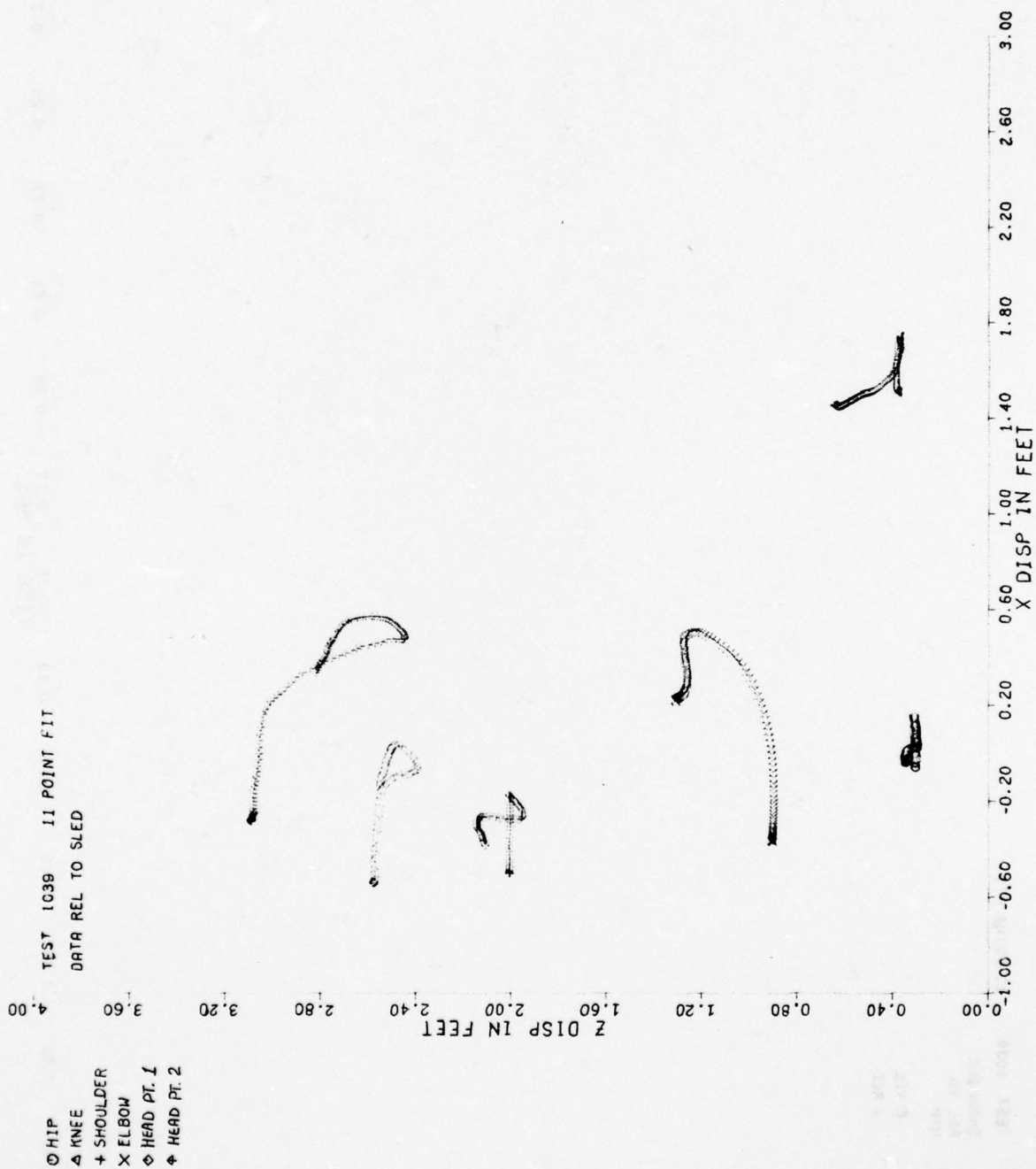
MAXIMUM NEGATIVE X DISPLACEMENT= -.035 AT TIME .05508

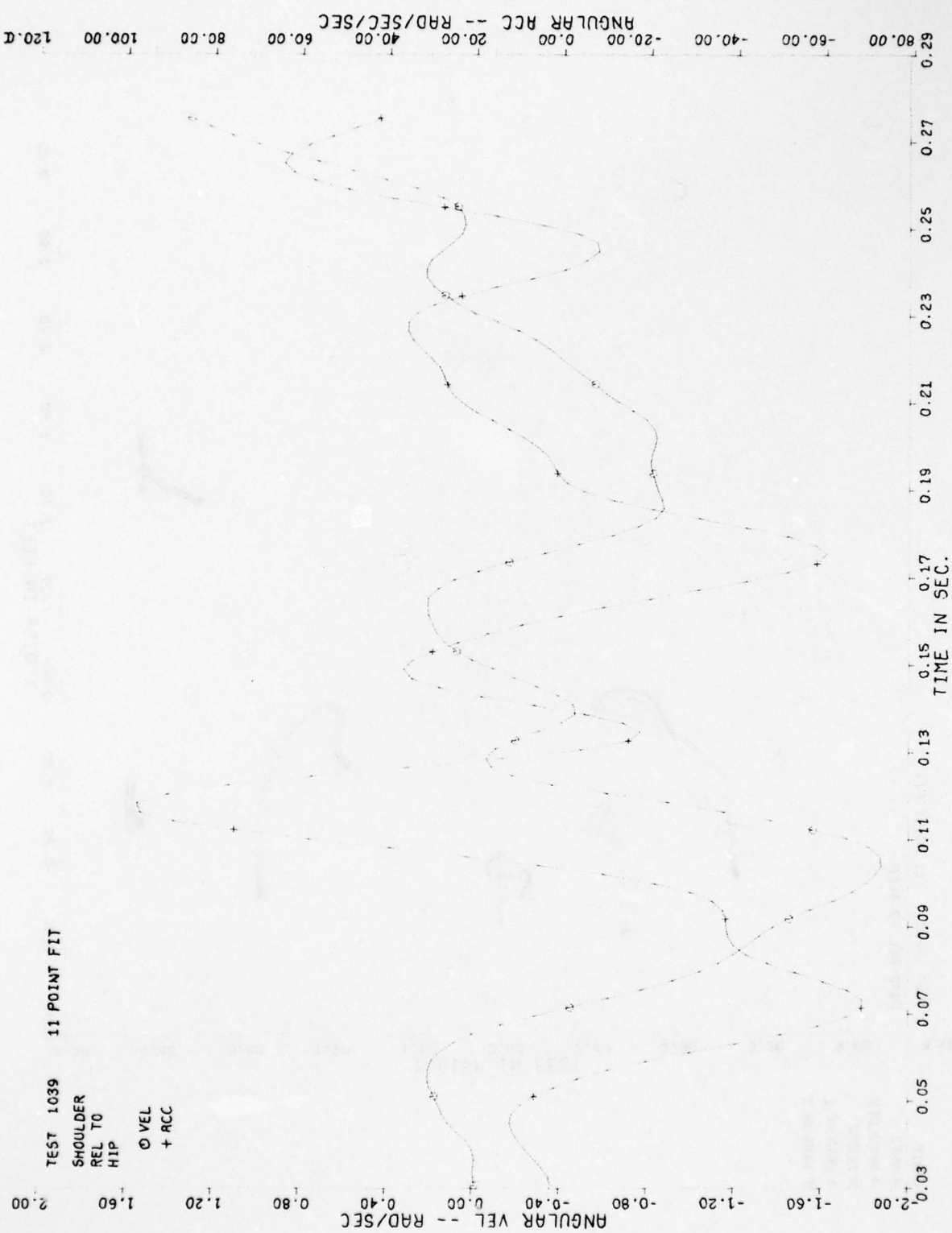
MAXIMUM POSITIVE Z DISPLACEMENT= .017 AT TIME .02652

MAXIMUM NEGATIVE Z DISPLACEMENT= -.632 AT TIME .18155

MAXIMUM RESULTANT DISPLACEMENT= .986 AT TIME .20194





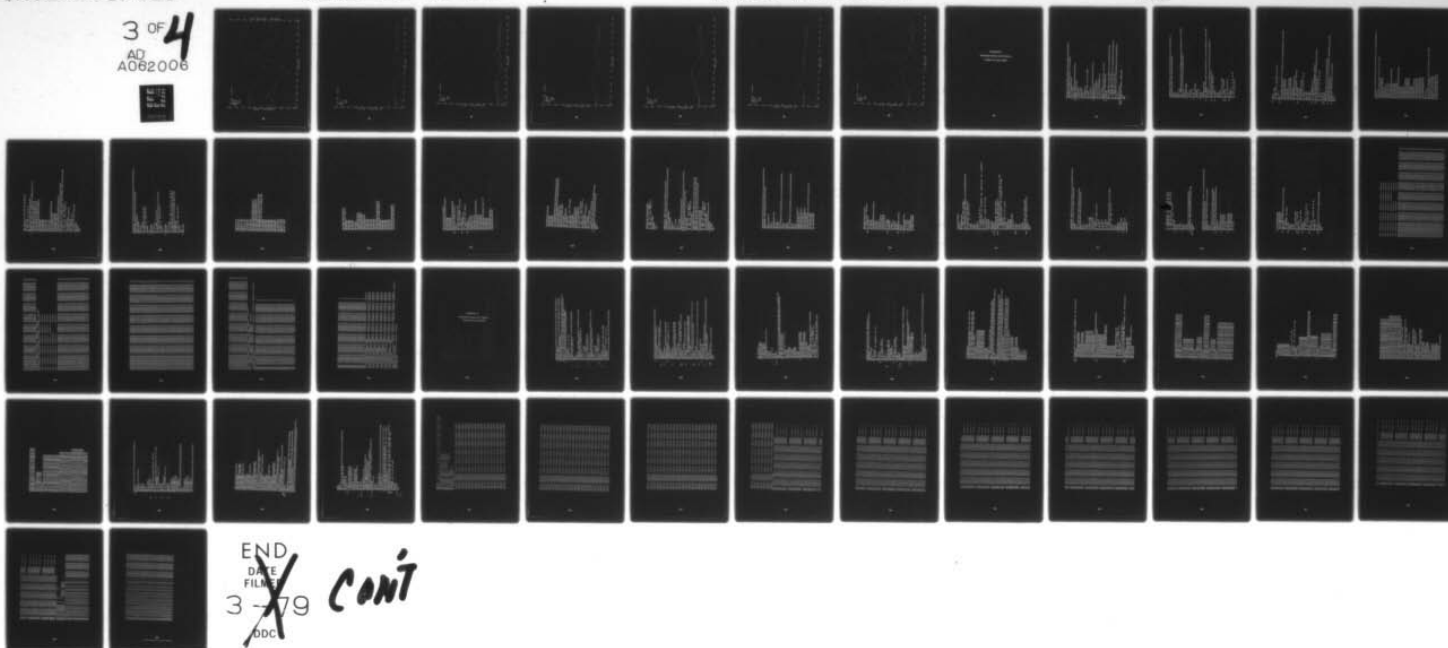


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DAYTON UNIV OHIO RESEARCH INST  
PHOTOMETRIC METHODS FOR THE ANALYSIS OF HUMAN KINEMATIC RESPONSE--ETC(U)  
OCT 78 P A GRAF, H T MOHLMAN, R C REBOULET F33615-73-C-4157  
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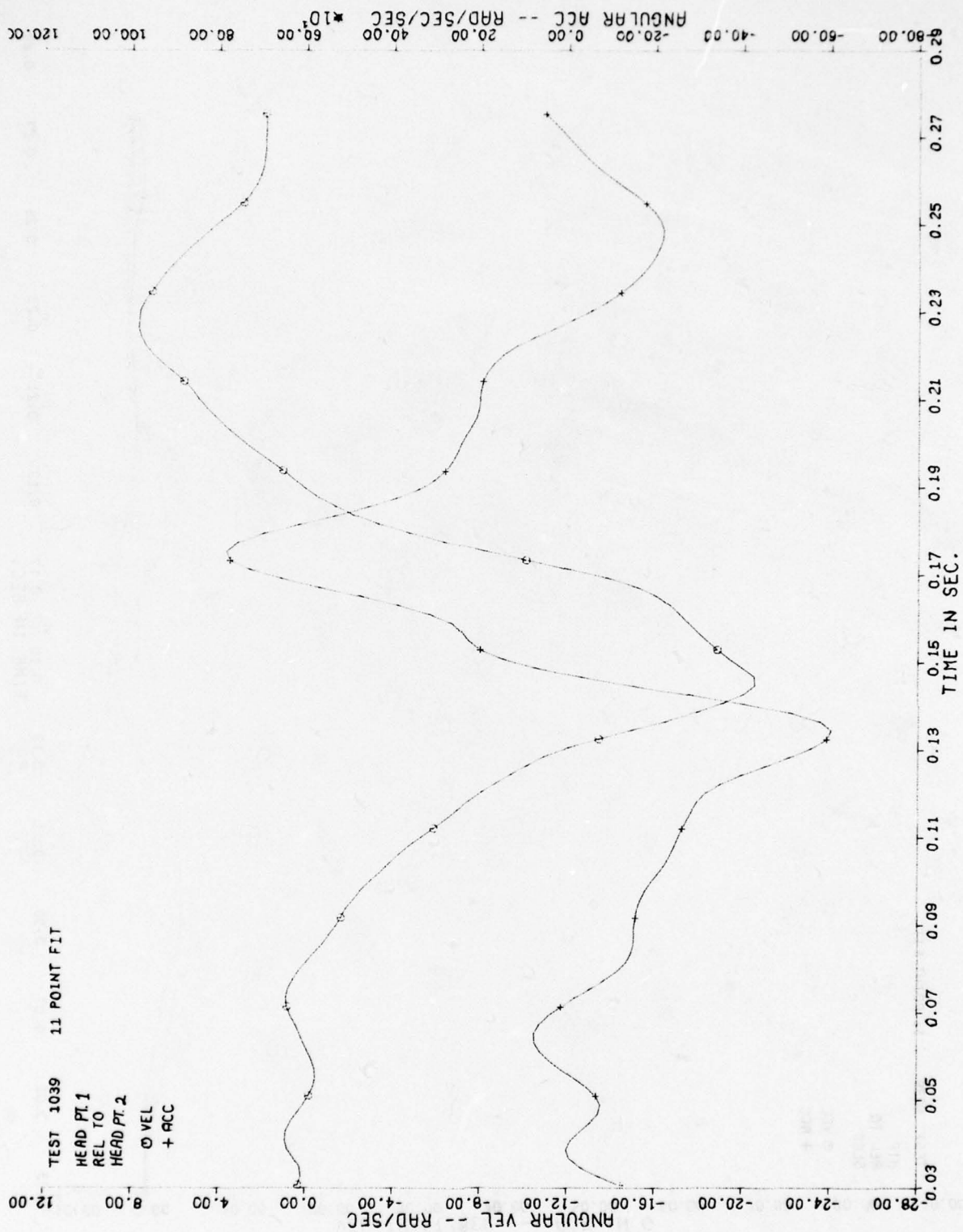
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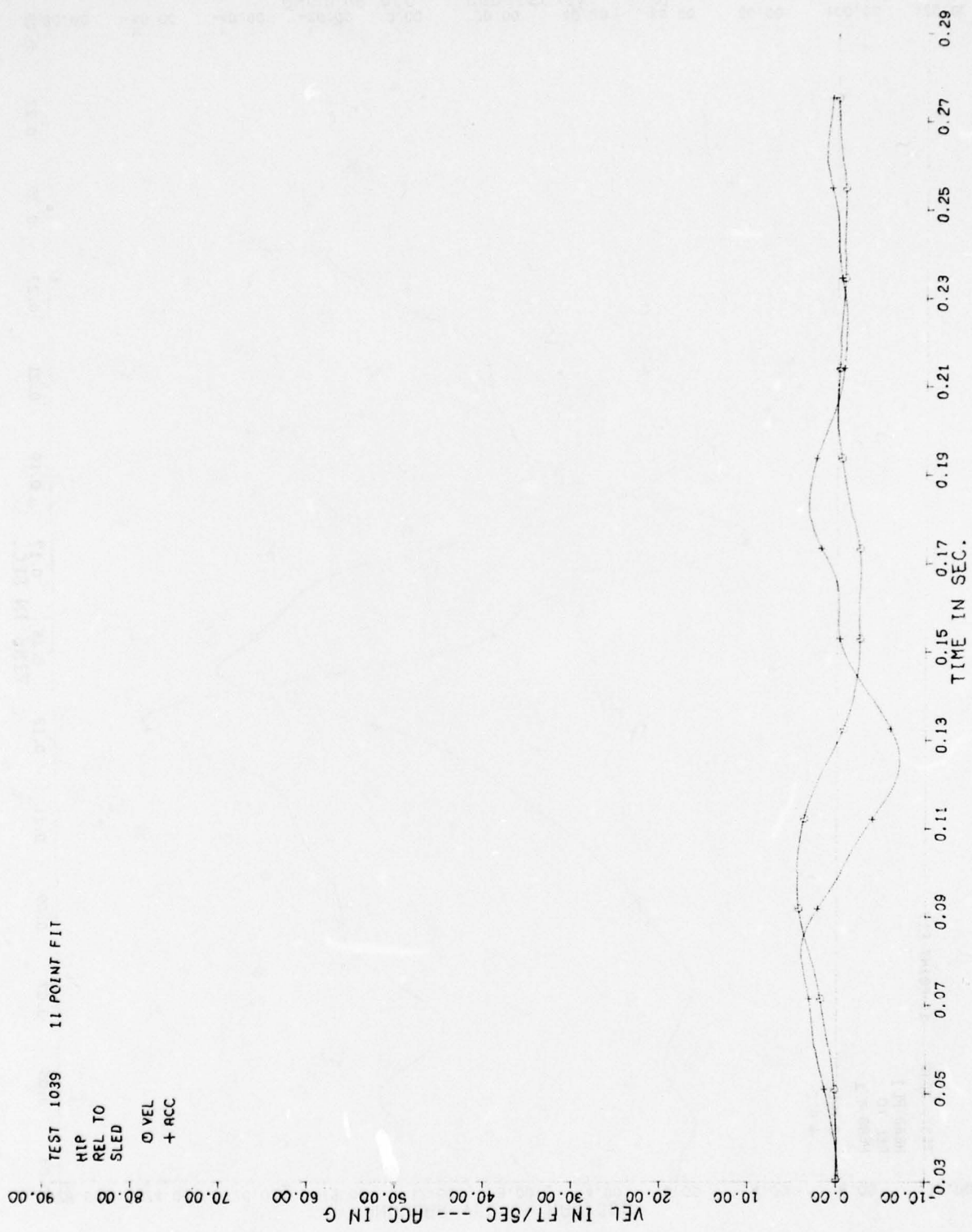


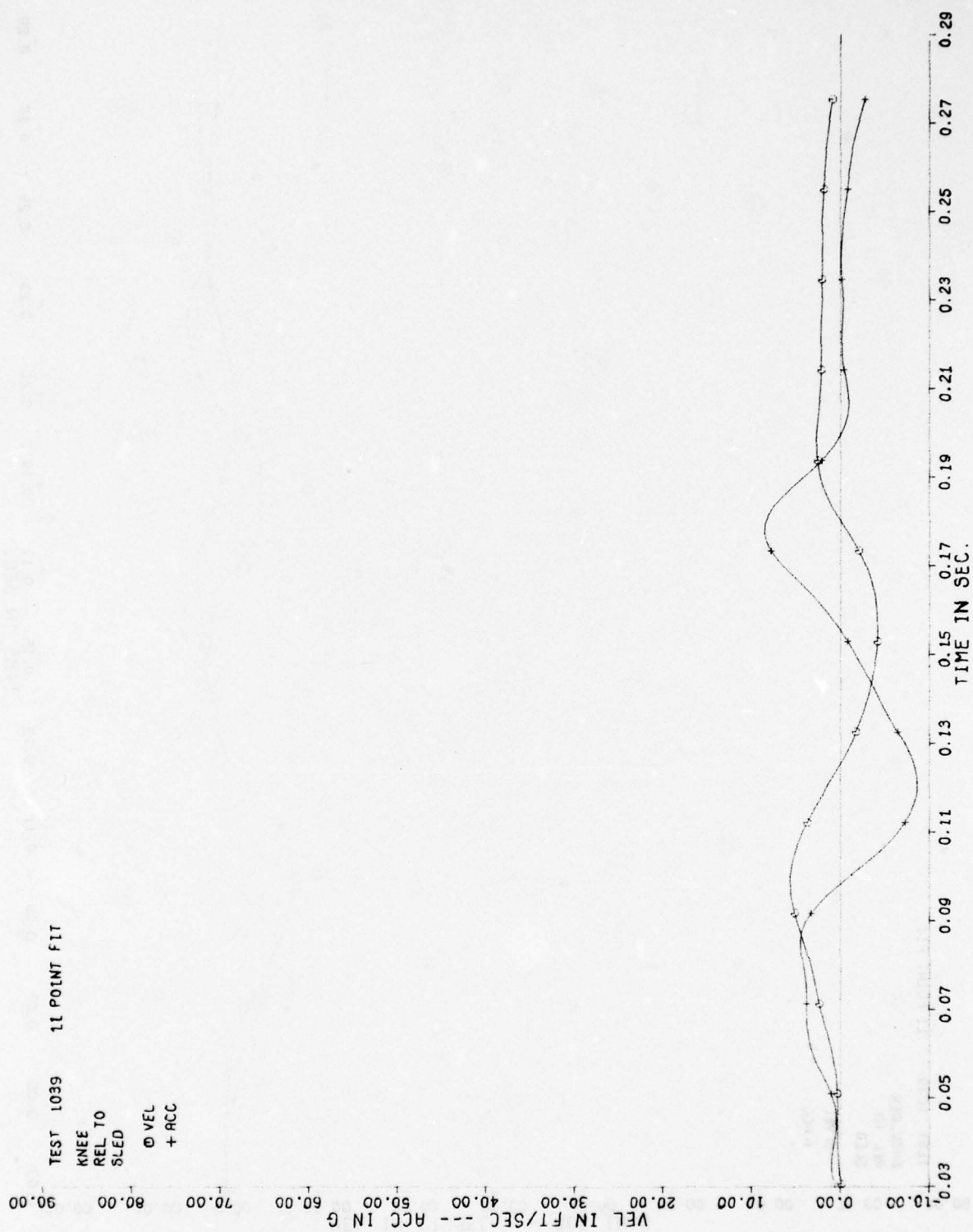
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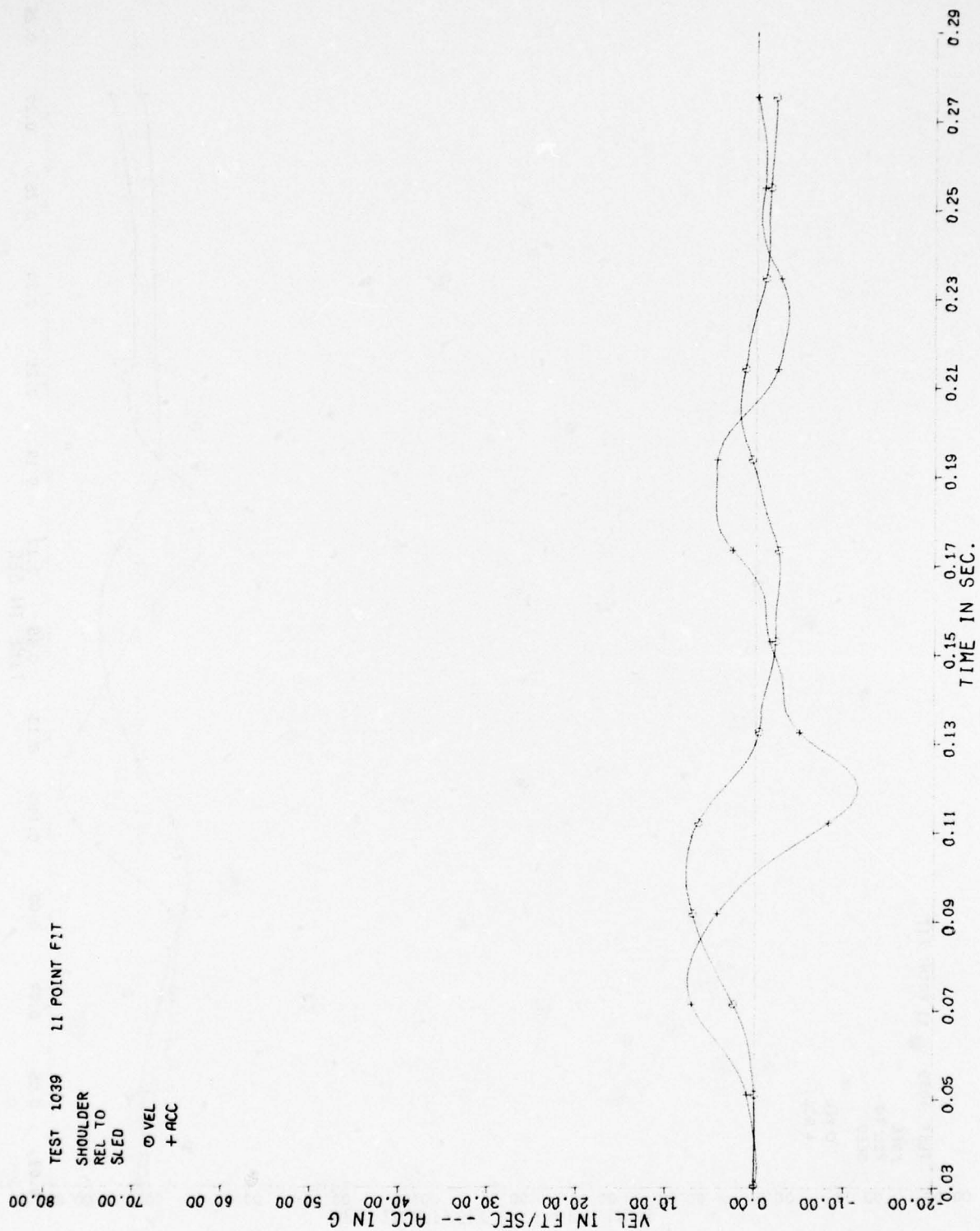
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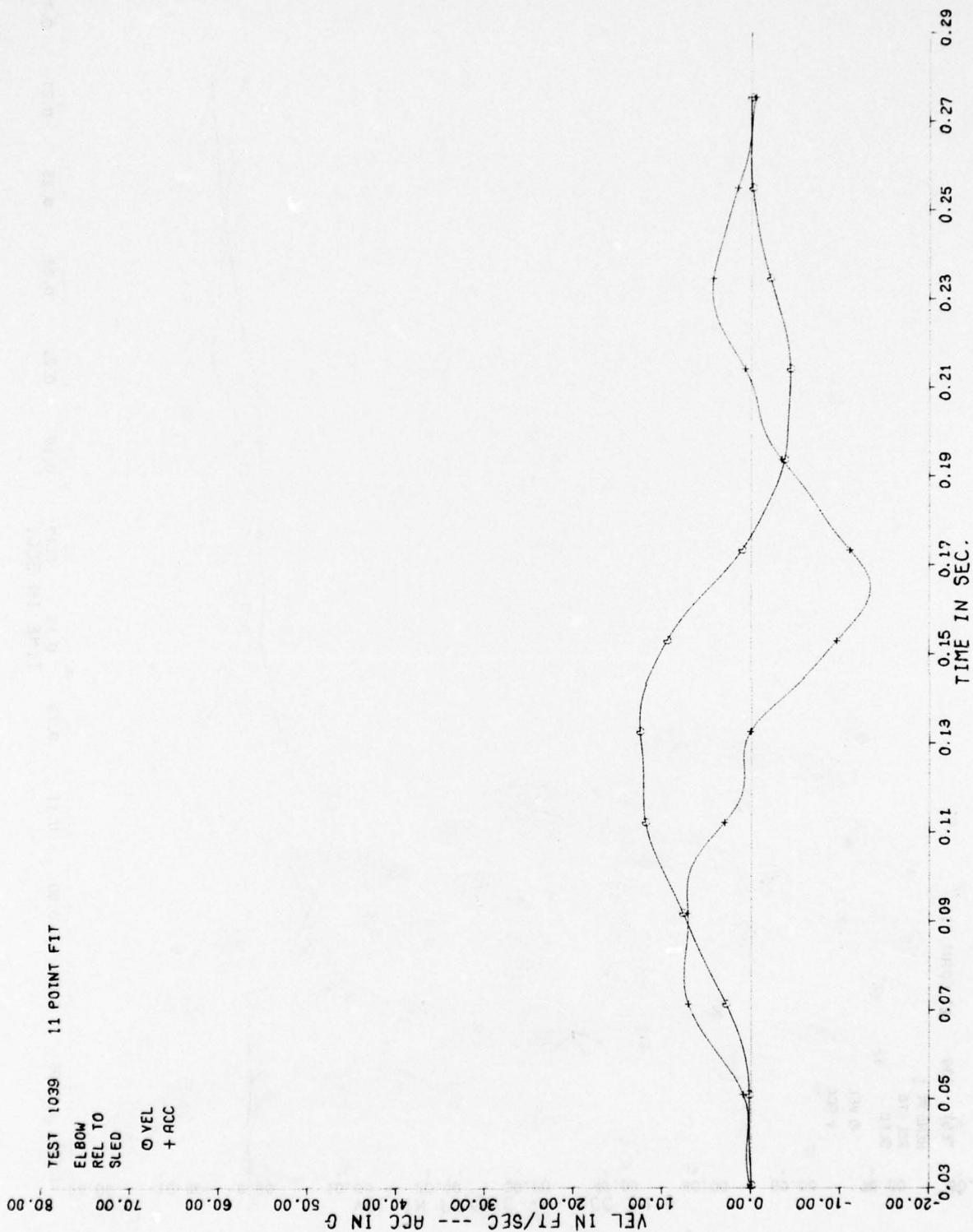




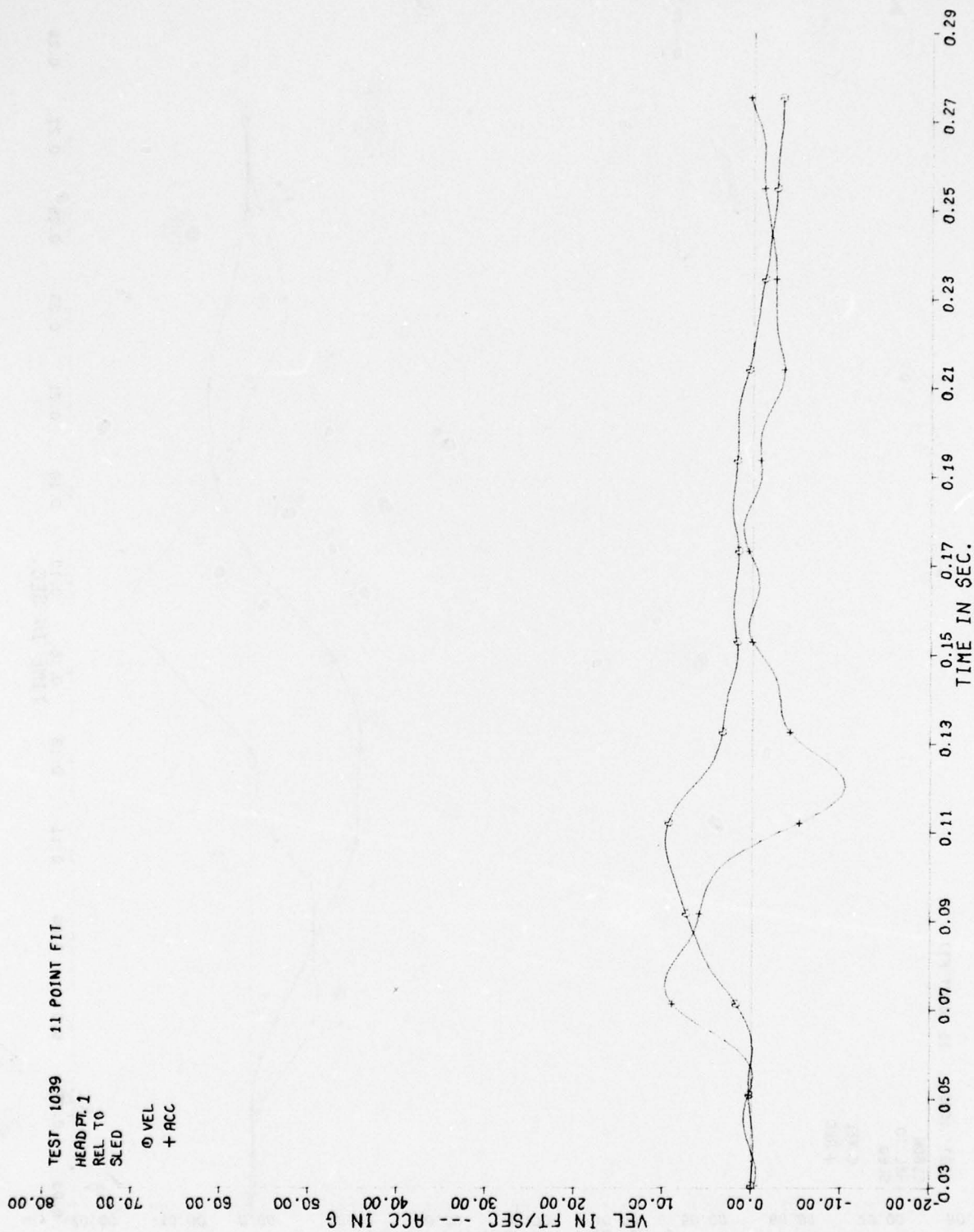


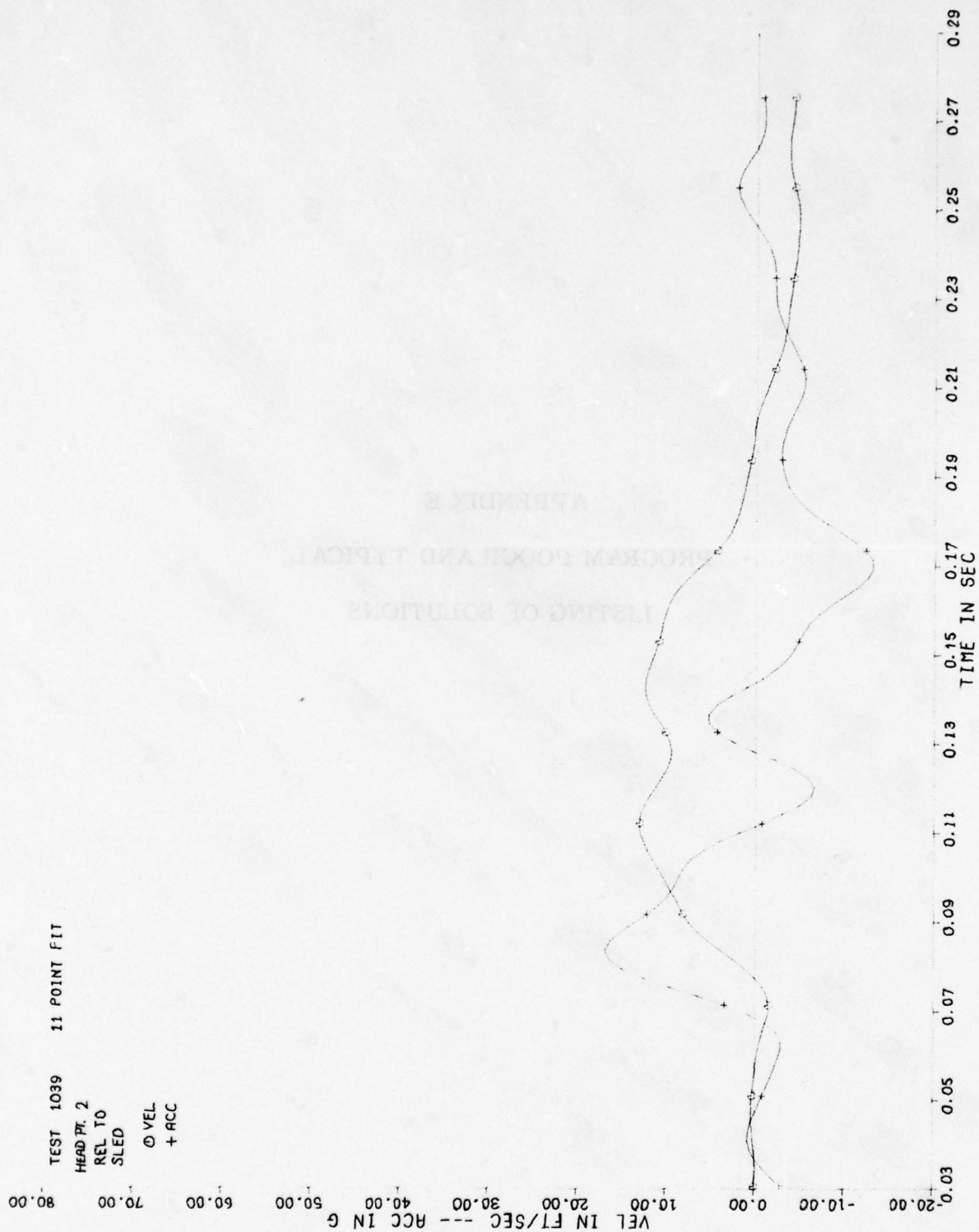












**APPENDIX E**  
**PROGRAM POOCH AND TYPICAL**  
**LISTING OF SOLUTIONS**

```

PROGRAM POOCH(INPUT,OUTPUT,TAPE5=INPUT,TAPE6=OUTPUT)
DIMENSION X(20),Y(20),Z(20),P(20),Q(20)
DIR=3.14159265/180.0
RTD=1.0/DTR
1 READ(5,2)XX,YY,ZZ,FF,FP,FQ,XSR,N
2 FORMAT(7F10.0,I5)
FF=FF/12.0
FP=FP/12.0
FQ=FQ/12.0
YY=-YY
ICLK=EOF(5)
IF (ICLK .NE. 0) GO TO 2000
NSTOP=0
DO 3 I=1,N
  READ(5,4) P(I),Q(I),X(I),Y(I),Z(I)
4 FORMAT(5F10.0)
  P(I)=-P(I)/12000.0
  Q(I)=Q(I)/12000.0
  Q(I)=Q(I)*(1.0-XSR*P(I))
  Y(I)=-Y(I)
  WRITE(6,6)P(I),Q(I),X(I),Y(I),Z(I)
6 FORMAT(6H POCJ,5E13.6/)
3 CONTINUE
CALL FIND(XX,YY,ZZ,FF,ERR,X,Y,Z,P,Q,N,NSTOP,FP,FQ)
IF (NSTOP .EQ. 1) GO TO 1
CALL SERCH(XX,YY,ZZ,FF,X,Y,Z,P,Q,N,NSTOP,TH,PH,GAM,K,L)
IF (NSTOP .EQ. 1) GO TO 1
CALL DANG(XX,YY,ZZ,FF,TH,PH,GAM,X,Y,Z,P,Q,N,DNG,K,L)
GO TO 1
2000 WRITE(6,2001)
2001 FORMAT(18H NORMAL COMPLETION )
STOP
END

```



```

SUBROUTINE DANG(XX,YY,ZZ,FF,TH,PH,3AM,X,Y,Z,P,Q,N,DNG,K,L)
DIMENSION X(20),Y(20),Z(20),P(20),Q(20)
NRE=0
KTR=1
NTR=0
DNG=0.03
CALL WRANG(XX,YY,ZZ,FF,TH,PH,GAM,X,Y,Z,P,Q,N,ERR,NRE,K,L,THI,PHI)
WRITE(6,11)XX,YY,ZZ,FF,TH,PH,GAM,ERR,NTR
XMO=1.0
1 TS=TH+XMO*DNG
PS=PH
GAS=GAM
GO TO 20
2 TS=TH
PS=PH+XMO*DNG
GAS=GAM
GO TO 20
3 TS=TH
PS=PH
GAS=GAM+XMO*DNG
20 CALL WRANG(XX,YY,ZZ,FF,TS,PS,GAS,X,Y,Z,P,Q,N,ERS,NRE,K,L,THI,PHI)
NTR=NTR+1
IF (NTR.LT. 51) WRITE(6,100)TS,PS,GAS,ERS,DNG,XMO,KTR
100 FORMAT(5H DANG,6E13.6,I5)
IF (ERR-ERS) 22,22,21
21 ERR=ERS
TH=TS
PH=PS
GAM=GAS
GO TO (1,2,3),KTR
22 IF (XMO) 24,23,23
23 XMO=-1.0
GO TO (1,2,3),KTR
24 XMO=1.0
KTR=KTR+1
IF (KTR.GT. 3) GO TO 25
GO TO (1,2,3),KTR

```

```

25 KTR=1
   ONG=J.1*DNG
   IF (ONG.LT. 0.00000029) GO TO 26
   GO TO 1
26 NRE=1
   CALL WRANG(XX,YY,ZZ,FF,TH,PH,GAM,X,Y,Z,P,Q,N,ERR,NRE,K,L,THI,PHI)
   RFA=COS(TH)*COS(PH)
   RFB=SIN(TH)*COS(PH)
   RFC=SIN(PH)
   RIA=COS(THI)*COS(PHI)
   RIB=SIN(THI)*COS(PHI)
   RIC=SIN(PHI)
   RFM=SQRT(RFA**2+RFB**2)
   IF (RFM-0.00000001) 30,30,31
31 SIA=-RFB/RFM
   SIB=RFA/RFM
   HAG=SIA*RIA+SIB*RIB
   IF (HAG.GT. 0.0) GO TO 34
   SIA=-SIA
   SIB=-SIB
   SIC=-SIC
   HAG=-HAG
34 CALL AKOS(HAG,TILT)
   IF (ABS(TILT)-0.000000001) 30,30,32
32 TELL=RFA*(SIB*RIC-RIB*SIC)-RFB*(SIA*RIC-SIC*RIA)+
   1RFC*(SIA*RIB-SIB*RIA)
   IF (TELL.LT. 0.0) TILT=-TILT
   GO TO 33
30 TILT=0.0
33 CONTINUE
11 WRITE(6,11)XX,YY,ZZ,FF,TH,PH,GAM,ERR,NIR
11 FORMAT(19H X,Y,Z,F,AZ,EL,TILT,7E13.6/12H ERRORBITER.,E13.6,I5)
11 WRITE(6,10)THI,PHI,TILT
11 FORMAT(18H OAMS,THI,PHI,TILT,3E13.6)
11 RETURN
END

```

```

SUBROUTINE WRANG(XX,YY,ZZ,FF,TH,PH,GAM,X,Y,Z,P,Q,N,ERR,NRE,K,L,
1THI,PHI)
  DIMENSION X(20),Y(20),Z(20),P(20),Q(20)
  FN1=COS(TH)*COS(PH)
  FN2=SIN(TH)*COS(PH)
  FN3=SIN(PH)
  PIPA=X(K)-X(L)
  PIPB=Y(K)-Y(L)
  PIPC=Z(K)-Z(L)
  A=FN1*PIPA+FN2*PIPB+FN3*PIPC
  PIA=PIPA-A*FN1
  PIB=PIPB-A*FN2
  PIC=PIPC-A*FN3
  PIJ=SQR(PIA**2+PIB**2+PIC**2)
  PIA=PIA/PIJ
  PIB=PIB/PIJ
  PIC=PIC/PIJ
  PJA=FN2*PIC-FN3*PIB
  PJB=FN3*PIA-FN1*PIC
  PJC=FN1*PIB-FN2*PIA
  COG=COS(GAM)
  SIG=SIN(GAM)
  TIA=COG*PIA+SIG*PJA
  TIB=COG*PIB+SIG*PJB
  TIC=COG*PIC+SIG*PJC
  TJA=-SIG*PIA+COG*PJA
  TJB=-SIG*PIB+COG*PJB
  TJC=-SIG*PIC+COG*PJC
  ERR=J.0
  DO 1 I=1,N
    W=FF/((X(I)-XX)*FN1+(Y(I)-YY)*FN2+(Z(I)-ZZ)*FN3)
    RA=W*(X(I)-XX)-FF*FN1
    RB=W*(Y(I)-YY)-FF*FN2
    RC=W*(Z(I)-ZZ)-FF*FN3
    PA=RA*TIA+RB*TIB+RC*TIC
    QA=RA*TJA+RB*TJB+RC*TJC
  
```

```

ERA=SQRT((P(I)-PA)**2+(Q(I)-QA)**2)
ERR=ERR+ERA
IF (NRE .EQ. 0) GO TO 1
WRITE(6,2) I, P(I), Q(I), PA, QA, ERA
2 FORMAT(26H READ PT. PIERCE PT., ERROR, I5, 5E13.6)
PHA=FF*FN1+P(I)*TIA+Q(I)*TJA
PHB=FF*FN2+P(I)*TIB+Q(I)*TJB
PHC=FF*FN3+P(I)*TIC+Q(I)*TJC
OPH=SQRT(PHA**2+PHB**2+PHC**2)
PHA=PHA/OPH
PHB=PHB/OPH
PHC=PHC/OPH
SHA=X(I)-XX
SHB=Y(I)-YY
SHC=Z(I)-ZZ
ACOF=PHA*SHA+PHB*SHB+PHC*SHC
DISA=ACOF*PHA-SHA
DISB=ACOF*PHB-SHB
DISC=ACOF*PHC-SHC
DIS=SQRT(DISA**2+DISB**2+DISC**2)
WRITE(6,3) I, X(I), Y(I), Z(I), DISA, DISB, DISC, DIS
3 FORMAT(37H ITH OBJECT POINT AND DISTANCE VECTOR/I5, 7E13.6)
IF (TIC .GT. 1.0) TIC=1.0
IF (TIC .LT. -1.0) TIC=-1.0
PHI=ASIN(TIC)
TUM=SQRT(TIA**2+TIB**2)
ARG=TIA/TUM
CALL AKOS(ARG, THI)
IF (TIB .LT. 0.0) THI=-THI
1 CONTINUE
RETURN
END

```



```

SUBROUTINE SERCH(XX,YY,ZZ,FF,X,Y,Z,P,Q,N,NSTOP,TH,PH,GAM,K,L)
DIMENSION X(20),Y(20),Z(20),P(20),Q(20)
DIR=.01745329252
RTD=1.0/DIR
STO=0.0
DO 1 I=1,N
STA=SQRT(P(I)**2+Q(I)**2)
IF (STA .LE. STO) GO TO 1
STO=STA
K=I
1 CONTINUE
STO=0.0
DO 2 I=1,N
IF (K .EQ. I) GO TO 2
STA=SQRT((P(K)-P(I))**2+(Q(K)-Q(I))**2)
IF (STA .LE. STO) GO TO 2
STO=STA
L=I
2 CONTINUE
STO=0.0
DO 3 I=1,N
IF ((I .EQ. K) .OR. (I .EQ. L)) GO TO 3
STA=SQRT((P(I)-P(K))**2+(Q(I)-Q(K))**2)
STB=SQRT((P(I)-P(L))**2+(Q(I)-Q(L))**2)
STA=STA+STB
IF (STA .LE. STO) GO TO 3
STO=STA
M=I
3 CONTINUE

```

FAA=X(K)-XX  
 FAB=Y(K)-YY  
 FAC=Z(K)-ZZ  
 FBA=X(L)-XX  
 FBB=Y(L)-YY  
 FBC=Z(L)-ZZ  
 FCA=X(M)-XX  
 FCB=Y(M)-YY  
 FCC=Z(M)-ZZ  
 DAM=SQRT(FAA\*\*2+FAB\*\*2+FAC\*\*2)  
 DBM=SQRT(FBA\*\*2+FBB\*\*2+FBC\*\*2)  
 DCM=SQRT(FCA\*\*2+FCB\*\*2+FCC\*\*2)  
 DAM=DAM/SQRT(FF\*\*2+P(K)\*\*2+Q(K)\*\*2)  
 DBM=DBM/SQRT(FF\*\*2+P(L)\*\*2+Q(L)\*\*2)  
 DCM=DCM/SQRT(FF\*\*2+P(M)\*\*2+Q(M)\*\*2)  
 FAA=FAA/DAM  
 FAB=FAB/DAM  
 FAC=FAC/DAM  
 FBA=FBA/DBM  
 FBB=FBB/DBM  
 FBC=FBC/DBM  
 FCA=FCA/DCM  
 FCB=FCB/DCM  
 FCC=FCC/DCM  
 MA=P(K)-P(M)  
 MB=Q(K)-Q(M)  
 UA=P(L)-P(M)  
 UB=Q(L)-Q(M)

WAB=SQRT(WA\*\*2+WB\*\*2)  
 UAB=SQRT(UA\*\*2+UB\*\*2)  
 WA=WA/WAB  
 WB=WB/WAB  
 UA=UA/UAB  
 UB=UB/UAB  
 CA=-P(M)  
 CB=-Q(M)  
 FLAM=WA\*UB-WB\*UA  
 COFA=CA\*UB-CB\*UA  
 COFB=WA\*CB-WB\*CA  
 COFA=COFA/FLAM  
 COFB=COFB/FLAM  
 WA=FAA-FCA  
 WB=FAB-FCB  
 MC=FAC-FCC  
 UA=FBA-FCA  
 UB=FBB-FCB  
 UC=FBC-FCC  
 WAB=SQRT(WA\*\*2+WB\*\*2+WC\*\*2)  
 UAB=SQRT(UA\*\*2+UB\*\*2+UC\*\*2)  
 WA=WA/WAB  
 WB=WB/WAB  
 MC=MC/WAB  
 UA=UA/UAB  
 UB=UB/UAB  
 UC=UC/UAB  
 FN1=FCA+COFA\*WA+COFB\*UA  
 FN2=FCB+COFA\*WB+COFB\*JB

```

FN3=FCC+COFA*WC+COFB*UC
DCKN=SQRT(FN1**2+FN2**2+FN3**2)
FN1=FN1/DCKN
FN2=FN2/DCKN
FN3=FN3/DCKN
WRITE(6,12)FN1,FN2,FN3,DCKN
12 FORMAT(6H SERCH,4E13.6)
TH=0.0
DINH=SQRT(FN1**2+FN2**2)
IF (DINH -0.00000001) 13,13,14
14 ARG=FN1/DINH
CALL AKOS(ARG,TH)
IF (FN2 .LT. 0.0) TH=-TH
13 CONTINUE
PH=ASIN(FN3)
PIPA=X(K)-X(L)
PIPB=Y(K)-Y(L)
PIPC=Z(K)-Z(L)
A=FN1*PIPA+FN2*PIPB+FN3*PIPC
PIA=PIPA-A*FN1
PIB=PIPB-A*FN2
PIC=PIPC-A*FN3
PIO=SQRT(PIA**2+PIB**2+PIC**2)
PIA=PIA/PIO
PIB=PIB/PIO
PIC=PIC/PIO
PJA=FN2*PIC-FN3*PIB
PJB=FN3*PIA-FN1*PIC

```



```

PJC=FN1*PIB-FN2*PIA
FFA=FF*FN1
FFB=FF*FN2
FFC=FF*FN3
ELA=(FAA-FFA)*PIA+(FAB-FFB)*PIB+(FAC-FFC)*PIC
ELB=(FAA-FFA)*PIA+(FAB-FFB)*PIB+(FAC-FFC)*PIC
DEL=P(K)**2+Q(K)**2
DSA=P(K)*ELB-Q(K)*ELA
DCA=P(K)*ELA+Q(K)*ELB
ARG=DCA/DEL
CALL AKOS(ARG,GAM)
ARG=DSA/DEL
IF (ARG .LT. 0.0) GAM=-GAM
COG=COS(GAM)
SIG=SIN(GAM)
GIA=COG*PIA+SIS*PJA
GIB=COG*PIB+SIS*PJB
GIC=COG*PIC+SIS*PJC
IF (GIC .GT. 1.0) GIC=1.0
IF (GIC .LT. -1.0) GIC=-1.0
PHI=ASIN(GIC)
GDM=SQRT(GIA**2+GIB**2)
ARG=GIA/GDM
CALL AKOS(ARG,IHI)
IF (GIB .LT. 0.0) THI=-THI
WRITE(6,20) XX,YY,ZZ,FF,TH,PH,GAM,IHI,PHI
20 FORMAT(6H SERCH,5E13.6/6X,4E13.6)
RETURN
END

```

```

SUBROUTINE AKOS(ARG,ANG)
IF (ARG .GT. 1.0) ARG=1.0
IF (ARG .LT. -1.0) ARG=-1.0
ANG=ACOS(ARG)
RETURN
END

```

```

SUBROUTINE ANGLE (XX,YY,ZZ,FF,ERR,X,Y,Z,P,Q,N)
DIMENSION X(20),Y(20),Z(20),P(20),Q(20),G(20,20),H(20,20)
DTR=0.01745329252
RT0=1.0/DTR
ERR=0.0
M=N-1
DO 1 I=1,M
K=I+1
DO 1 J=K,N
ROM=FF**2+P(I)*P(J)+Q(I)*Q(J)
ORAD=SQRT(FF**4+(P(I)**2+Q(I)**2+P(J)**2+Q(J)**2)*FF**2
1+(P(I)**2+Q(I)**2)*(P(J)**2+Q(J)**2))
ARG=ROM/RAD
IF (ARG .GT. 1.0) ARG=1.0
IF (ARG .LT. -1.0) ARG=-1.0
G(I,J)=ACOS(ARG)
RAD1=SQRT((X(I)-XX)**2+(Y(I)-YY)**2+(Z(I)-ZZ)**2)
RAD2=SQRT((X(J)-XX)**2+(Y(J)-YY)**2+(Z(J)-ZZ)**2)
DOM=(X(I)-XX)*(X(J)-XX)+(Y(I)-YY)*(Y(J)-YY)+(Z(I)-ZZ)*
1(Z(I)-ZZ)*(Z(J)-ZZ)
ARG=DOM/(RAD1*RAD2)
IF (ARG .LT. -1.0) ARG=-1.0
IF (ARG .GT. 1.0) ARG=1.0
H(I,J)=ACOS(ARG)
ERR=ERR+(G(I,J)-H(I,J))**2
1 CONTINUE
RETURN
END

```

```

SUBROUTINE FIND(XX,YY,ZZ,FF,ERR,X,Y,Z,P,Q,N,NSTOP,FP,FQ)
DIMENSION X(20),Y(20),Z(20),P(20),Q(20)
M=6
ERS=1000000.0
XM=M
NTRY=1
DUST=(FQ-FP)/XM
DP=1.5
DF=30.1
DPP=DP
CALL HORSY(XX,YY,ZZ,FP,ERR,X,Y,Z,P,Q,N,NSTOP,DPP,DF)
XA=XX
YA=YY
ZA=ZZ
DPP=DP
CALL HORSY(XX,YY,ZZ,FQ,ERR,X,Y,Z,P,Q,N,NSTOP,DPP,DF)
XB=XX
YB=YY
ZB=ZZ
COXB=(XB-XA)/(FQ-FP)
COXA=XA-COXB*FP
COYB=(YB-YA)/(FQ-FP)
COYA=YA-COYB*FP
COZB=(ZB-ZA)/(FQ-FP)
COZA=ZA-COZB*FP
DAST=SQRT((XB-XA)**2+(YB-YA)**2+(ZB-ZA)**2)
SX=(XB-XA)/DAST
SY=(YB-YA)/DAST
SZ=(ZB-ZA)/DAST

```

```

DOM=SQRT(SX**2+SY**2)
IF (DOM-0.0001) 50,50,51
50 TX=1.0-SX**2
   TY=-SX*SY
   TZ=-SX*SZ
   TD=SQRT(TX**2+TY**2+TZ**2)
   TX=TX/TD
   TY=TY/TD
   TZ=TZ/TD
   UX=SY*TZ-SZ*TY
   UY=SZ*TX-SX*TZ
   UZ=SX*TY-SY*TX
   GO TO 52
51 TX=-SY/DOM
   TY=TX/DOM
   TZ=0.0
   UX=-TY*SZ
   UY=TX*SZ
   UZ=DOM
52 CDDP=DAST/(FQ-FP)
   FS=FP
   K=M+1
   2 DIST=(FQ-FP)/XM
   FF=FP-DIST
   DO 3 I=1,K
   FF=FF+DIST
   XX=COXA+COXB*FF
   YY=COYA+COYB*FF

```



```

ZZ=COZA+COZB*FF
OPP=DP
OPCK=CODP*DIST
IF (OPCK .LT. DPP) OPP=OPCK
CALL REFIN(XX,YY,ZZ,FF,ERR,X,Y,Z,P,Q,N,NSTOP,OPP,DF,
1SX,SY,SZ,IX,IY,IZ,UX,UY,UZ)
IF (ERR .GT. ERS) GO TO 1
XS=XX
YS=YY
ZS=ZZ
FS=FF
ERS=ERR
1 IF (I .LT. K) GO TO 3
IF ((ABS(FS-FP) .LT. 0.5*DIST) .OR. (ABS(FS-FQ) .LT. 0.5*DIST))
1GO TO 1000
IF (DIST .LT. 0.001) GO TO 900
FP=FS-DIST
FQ=FS+DIST
GO TO 2
3 CONTINUE
1000 NSTOP=1
WRITE(6,1001) FS,FP,FQ,DIST
1001 FORMAT(11H NO BRACKET,4E13.6)
IF (ABS(DIST-DIST+0.000001) .GT. 0.00001) GO TO 900
IF (ABS(FS-FQ+0.000001) .GT. 0.00001) GO TO 300
NTRY=NTRY+1
IF (NTRY .GT. 3) GO TO 900
NSTOP=0
TEMP=FQ-FP
FP=FQ-DIST
FQ=FQ+TEMP-DIST
GO TO 2
900 XX=XS
YY=YS
ZZ=ZS
FF=FS
ERR=ERS
WRITE(6,901) XX,YY,ZZ,FF,ERR
901 FORMAT(13H NEW POSITION,5E13.6)
RETURN
END

```

```

SUBROUTINE HORSY (XX,YY,ZZ,FF,ERR,X,Y,Z,P,Q,N,NSTOP,DP,DF)
DIMENSION X(20),Y(20),Z(20),P(20),Q(20),N(20)
NTR=DF
KTR=0
CALL ANGLE (XX,YY,ZZ,FF,ERR,X,Y,Z,P,Q,N)
WRITE(6,8) XX,YY,ZZ,FF,ERR,DP,DF,KTR
XS=XX
YS=YY
ZS=ZZ
FT=FF
1 XT=XX-2.0*DP
YT=YY-2.0*DP
ZT=ZZ-2.0*DP
KTR=KTR+1
IF (KTR.GT. NTR) GO TO 7
DO 2 I=1,3
XT=XT+DP
DO 3 J=1,3
YT=YT+DP
DO 4 K=1,3
ZT=ZT+DP
CALL ANGLE (XT,YT,ZT,FT,ERR,X,Y,Z,P,Q,N)
IF (ERR .GE. ERR) GO TO 4
XS=XT
YS=YT
ZS=ZT
ERR=ERR
4 CONTINUE
ZT=ZT-3.0*DP
3 CONTINUE
YT=YT-3.0*DP
2 CONTINUE

```

```

IF (ABS (XX-XS) .GT. 0.01) GO TO 6
IF (ABS (YY-YS) .GT. 0.01) GO TO 6
IF (ABS (ZZ-ZS) .GT. 0.01) GO TO 6
IF (OP .LT. 0.01) GO TO 7
OP=0.1*DP
6 XX=XS
  YY=YS
  ZZ=ZS
  GO TO 1
7 XX=XS
  YY=YS
  ZZ=ZS
  WRITE(6,8) XX,YY,ZZ,FF,ERR,DP,DF,KTR
8 FORMAT(20H HARSY,XYZFERR,DP,DF,7E13.6,I5)
1000 RETURN
      END

```

```

SUBROUTINE REFIN(XX,YY,ZZ,FF,ERR,X,Y,Z,P,Q,N,NSTOP,DP,DF,
1SX,SY,SZ,TX,TY,TZ,UX,UY,UZ)
  DIMENSION X(20),Y(20),Z(20),P(20),Q(20)
  NTR=0
  KTR=1
  CALL ANGLE (XX,YY,ZZ,FF,ERR,X,Y,Z,P,Q,N)
  WRITE(6,11)XX,YY,ZZ,FF,ERR,DP,DF,KTR
11 FORMAT(20H REFIN,XYZFERR,DP,DF,7E13.6,I5)
  OP0=DP/3.0
  XM0=1.0
  1 XS=XX+XM0*SX*DP
    YS=YY+XM0*SY*DP
    ZS=ZZ+XM0*SZ*DP
    GO TO 20
  2 XS=XX+XM0*TX*DP0
    YS=YY+XM0*TY*DP0
    ZS=ZZ+XM0*TZ*DP0
    GO TO 20

```

```

3  XS=XX+XMO*UX*DPO
   YS=YY+XMO*UY*DPO
   ZS=ZZ+XMO*UZ*DPO
20  CALL ANGLE(XS,YS,ZS,FF,ERS,X,Y,Z,P,Q,N)
    NTR=NTR+1
    IF (ERR-ERS) 22,22,21
21  ERR=ERS
    XX=XS
    YY=YS
    ZZ=ZS
    GO TO (1,2,3),KTR
22  IF (XMO) 24,23,23
23  XMO=-1.0
    GO TO (1,2,3),KTR
24  XMO=1.0
    KTR=KTR+1
    IF (KTR.GT. 3) GO TO 25
    GO TO (1,2,3),KTR
25  KTR=1
    DP=0.1*DP
    IF (DP.LT. 0.0009) GO TO 26
    DPO=DP/3.0
    GO TO 1
26  WRITE(6,11)XX,YY,ZZ,FF,ERR,DP,DF,NTR
    RETURN
    END

```





KEFIN,XYZFERR,UP,DF	-.460494E+01	.397950E+01	.433650E+01	.814815E+00	.199988E-03	.174604E+00	.301000E+02	1
KEFIN,XYZFERR,UP,DF	-.455237E+01	.406197E+01	.419542E+01	.814815E+00	.129183E-03	.174604E-03	.301000E+02	125
KEFIN,XYZFERR,UP,DF	-.474650E+01	.407392E+01	.437507E+01	.833333E+00	.199998E-03	.174604E+00	.301000E+02	1
KEFIN,XYZFERR,UP,DF	-.469295E+01	.415643E+01	.423799E+01	.833333E+00	.137415E-03	.174604E-03	.301000E+02	120
KEFIN,XYZFERR,UP,DF	-.488806E+01	.416834E+01	.441484E+01	.851852E+00	.201888E-03	.174604E+00	.301000E+02	1
KEFIN,XYZFERR,UP,DF	-.483515E+01	.424988E+01	.428432E+01	.851852E+00	.148211E-03	.174604E-03	.301000E+02	113
KEFIN,XYZFERR,UP,DF	-.502961E+01	.426275E+01	.445400E+01	.870370E+00	.205168E-03	.174604E+00	.301000E+02	1
KEFIN,XYZFERR,UP,DF	-.497616E+01	.434394E+01	.432693E+01	.870370E+00	.157835E-03	.174604E-03	.301000E+02	108
KEFIN,XYZFERR,UP,DF	-.517117E+01	.435712E+01	.449317E+01	.888889E+00	.209450E-03	.174604E+00	.301000E+02	1
KEFIN,XYZFERR,UP,DF	-.511750E+01	.443751E+01	.436093E+01	.888889E+00	.167817E-03	.174604E-03	.301000E+02	102
NO BRACKET	.777778E+00	.777778E+00	.688889E+00	.185185E-01				
NEW POSITION	-.426765E+01	.387836E+01	.410252E+01	.777778E+00	.113512E-03			
P00CJ	-.400833E-01	.215833E+00	.378908E+01	.149210E+01	.376825E+01			
P00CJ	-.120750E+00	.218000E+00	.380208E+01	.325500E+00	.376300E+01			
P00CJ	-.230583E+00	.220917E+00	.380992E+01	-.841167E+00	.376567E+01			
P00CJ	.156833E+00	-.158417E+00	.546670E-01	.109370E+01	.487000E+00			
P00CJ	.110833E+00	-.159167E+00	.729170E-01	.583330E+00	.648417E+00			
P00CJ	.672500E-01	-.170917E+00	.833330E-01-0.	.677083E+00				
P00CJ	.695833E-01	-.224083E+00	.783300E-02-0.	.291667E+00				
HARSY,XYZFERR,UP,DF	-.344942E+01	-.349358E+01	.357292E+01	.333333E+00	.379146E+01	.150000E+01	.301000E+02	0
HARSY,XYZFERR,UP,DF	-.100592E+01	-.125258E+01	.318592E+01	.333333E+00	.107208E-01	.150000E-02	.301000E+02	30
HARSY,XYZFERR,UP,DF	-.100592E+01	-.125258E+01	.318592E+01	.133333E+01	.915475E+01	.150000E+01	.301000E+02	0
HARSY,XYZFERR,UP,DF	-.815942E+01	-.719558E+01	.407392E+01	.133333E+01	.459038E-03	.150000E-02	.301000E+02	29
KEFIN,XYZFERR,UP,DF	-.100592E+01	-.125258E+01	.318592E+01	.333333E+00	.107208E-01	.150000E+01	.301000E+02	1
KEFIN,XYZFERR,UP,DF	-.100018E+01	-.125214E+01	.318641E+01	.333333E+00	.107208E-01	.150000E-03	.301000E+02	26
KEFIN,XYZFERR,UP,DF	-.219817E+01	-.224308E+01	.343392E+01	.500000E+00	.102213E-02	.150000E+01	.301000E+02	1
KEFIN,XYZFERR,UP,DF	-.219119E+01	-.226580E+01	.328146E+01	.500000E+00	.901431E-04	.150000E-03	.301000E+02	103
KEFIN,XYZFERR,UP,DF	-.339042E+01	-.323356E+01	.360192E+01	.666667E+00	.739412E-04	.150000E+01	.301000E+02	1
KEFIN,XYZFERR,UP,DF	-.336763E+01	-.326210E+01	.357316E+01	.666667E+00	.268528E-04	.150000E-03	.301000E+02	125
KEFIN,XYZFERR,UP,DF	-.458267E+01	-.422408E+01	.392992E+01	.833333E+00	.213020E-03	.150000E+01	.301000E+02	1
KEFIN,XYZFERR,UP,DF	-.453619E+01	-.423402E+01	.386451E+01	.833333E+00	.194705E-03	.150000E-03	.301000E+02	54
KEFIN,XYZFERR,UP,DF	-.577492E+01	-.521458E+01	.417792E+01	.100000E+01	.365068E-03	.150000E+01	.301000E+02	1
KEFIN,XYZFERR,UP,DF	-.574110E+01	-.524489E+01	.411802E+01	.100000E+01	.359933E-03	.150000E-03	.301000E+02	54
KEFIN,XYZFERR,UP,DF	-.696717E+01	-.620506E+01	.442592E+01	.116667E+01	.438761E-03	.150000E+01	.301000E+02	1
KEFIN,XYZFERR,UP,DF	-.694958E+01	-.622752E+01	.441137E+01	.116667E+01	.437847E-03	.150000E-03	.301000E+02	48
KEFIN,XYZFERR,UP,DF	-.815942E+01	-.719558E+01	.467392E+01	.133333E+01	.459038E-03	.150000E+01	.301000E+02	1
KEFIN,XYZFERR,UP,DF	-.815910E+01	-.719598E+01	.467392E+01	.133333E+01	.459038E-03	.150000E-03	.301000E+02	25
KEFIN,XYZFERR,UP,DF	-.219817E+01	-.224308E+01	.343392E+01	.500000E+00	.102213E-02	.150000E+01	.301000E+02	1
KEFIN,XYZFERR,UP,DF	-.219752E+01	-.226295E+01	.332459E+01	.500000E+00	.906490E-03	.150000E-03	.301000E+02	55
KEFIN,XYZFERR,UP,DF	-.259559E+01	-.257328E+01	.351859E+01	.555556E+00	.387812E-03	.150000E+01	.301000E+02	1
KEFIN,XYZFERR,UP,DF	-.258990E+01	-.259573E+01	.342104E+01	.555556E+00	.305357E-03	.150000E-03	.301000E+02	59
KEFIN,XYZFERR,UP,DF	-.299300E+01	-.290341E+01	.359825E+01	.611111E+00	.137382E-03	.150000E+01	.301000E+02	1
KEFIN,XYZFERR,UP,DF	-.297755E+01	-.293594E+01	.351059E+01	.611111E+00	.874531E-04	.150000E+01	.301000E+02	54





REFIN,XYZFERR,OP,DF	--.337570E+01	--.322135E+01	.367886E+01	.664609E+00	.743395E-04	.645980E-02	.301000E+02	1
REFIN,XYZFERR,OP,DF	--.336058E+01	--.324457E+01	.362996E+01	.664609E+00	.459363E-04	.645980E-03	.301000E+02	40
REFIN,XYZFERR,OP,DF	--.338061E+01	--.322543E+01	.367988E+01	.665295E+00	.741942E-04	.645980E-02	.301000E+02	1
REFIN,XYZFERR,OP,DF	--.337123E+01	--.322843E+01	.363310E+01	.665295E+00	.459637E-04	.645980E-03	.301000E+02	39
REFIN,XYZFERR,OP,DF	--.338551E+01	--.322950E+01	.368090E+01	.665981E+00	.740615E-04	.645980E-02	.301000E+02	1
REFIN,XYZFERR,OP,DF	--.337613E+01	--.325251E+01	.363112E+01	.665981E+00	.460005E-04	.645980E-03	.301000E+02	39
REFIN,XYZFERR,OP,DF	--.339042E+01	--.323356E+01	.368192E+01	.666667E+00	.739412E-04	.645980E-02	.301000E+02	1
REFIN,XYZFERR,OP,DF	--.338104E+01	--.325656E+01	.363514E+01	.666667E+00	.460490E-04	.645980E-03	.301000E+02	39
REFIN,XYZFERR,OP,DF	--.339533E+01	--.323766E+01	.368294E+01	.667353E+00	.738335E-04	.645980E-02	.301000E+02	1
REFIN,XYZFERR,OP,DF	--.338595E+01	--.326066E+01	.363616E+01	.667353E+00	.461092E-04	.645980E-03	.301000E+02	39
REFIN,XYZFERR,OP,DF	--.340023E+01	--.324173E+01	.368336E+01	.668038E+00	.737376E-04	.645980E-02	.301000E+02	1
REFIN,XYZFERR,OP,DF	--.339085E+01	--.326473E+01	.363718E+01	.668038E+00	.461809E-04	.645980E-03	.301000E+02	39
REFIN,XYZFERR,OP,DF	--.340514E+01	--.324581E+01	.368498E+01	.668724E+00	.736540E-04	.645980E-02	.301000E+02	1
REFIN,XYZFERR,OP,DF	--.339576E+01	--.326881E+01	.363820E+01	.668724E+00	.462641E-04	.645980E-03	.301000E+02	39
NEW POSITION	--.336763E+01	--.326210E+01	.357316E+01	.666667E+00	.268528E-04			
SERCH	.705517E+00	.576095E+00	.286528E+00	.666650E+00				
SERCH	--.336763E+01	--.326210E+01	.357316E+01	.666667E+00				
	--.290601E+00	--.236612E+01	.221354E+01	.799274E-02				
X,Y,Z,F,AZ,EL,TILT	--.336763E+01	--.326210E+01	.357316E+01	.666667E+00	.645135E+00	--.290601E+00	--.236612E+01	
UNKNOWN	.553967E-02							
DANG	.675135E+00	--.290601E+00	--.236612E+01	.142770E+00	.300000E-01	.100000E+01		1
DANG	.615135E+00	--.290601E+00	--.236612E+01	.137032E+00	.300000E-01	--.100000E+01		1
DANG	.645135E+00	--.260601E+00	--.236612E+01	.151804E+00	.300000E-01	.100000E+01		2
DANG	.645135E+00	--.290601E+00	--.236612E+01	.151804E+00	.300000E-01	--.100000E+01		2
DANG	.645135E+00	--.290601E+00	--.236612E+01	.542399E-01	.300000E-01	.100000E+01		3
DANG	.645135E+00	--.290601E+00	--.236612E+01	.391179E-01	.300000E-01	--.100000E+01		3
DANG	.645135E+00	--.290601E+00	--.236612E+01	.171195E-01	.300000E-02	.100000E+01		1
DANG	.642135E+00	--.290601E+00	--.236612E+01	.129730E-01	.300000E-02	--.100000E+01		1
DANG	.645135E+00	--.287601E+00	--.236612E+01	.174169E-01	.300000E-02	.100000E+01		2
DANG	.645135E+00	--.293601E+00	--.236612E+01	.160607E-01	.300000E-02	--.100000E+01		2
DANG	.645135E+00	--.290601E+00	--.236312E+01	.102064E-01	.300000E-02	.100000E+01		3
DANG	.645135E+00	--.290601E+00	--.236912E+01	.484586E-02	.300000E-02	--.100000E+01		3
DANG	.645135E+00	--.290601E+00	--.237212E+01	.790717E-02	.300000E-02	.100000E+01		3
DANG	.645435E+00	--.290601E+00	--.236912E+01	.550630E-02	.300000E-03	.100000E+01		1
DANG	.645435E+00	--.290601E+00	--.236912E+01	.486589E-02	.300000E-03	--.100000E+01		1
DANG	.645135E+00	--.290301E+00	--.236912E+01	.513745E-02	.300000E-03	.100000E+01		2
DANG	.645135E+00	--.290901E+00	--.236912E+01	.510764E-02	.300000E-03	--.100000E+01		2
DANG	.645135E+00	--.290601E+00	--.236882E+01	.474646E-02	.300000E-03	.100000E+01		3
DANG	.645135E+00	--.290601E+00	--.236882E+01	.470477E-02	.300000E-03	.100000E+01		3
DANG	.645135E+00	--.290601E+00	--.236822E+01	.469106E-02	.300000E-03	--.100000E+01		3
DANG	.645135E+00	--.290601E+00	--.236792E+01	.469564E-02	.300000E-03	.100000E+01		3
DANG	.645135E+00	--.290601E+00	--.236852E+01	.470477E-02	.300000E-03	--.100000E+01		3
DANG	.645165E+00	--.290601E+00	--.236822E+01	.474774E-02	.300000E-04	.100000E+01		1
DANG	.645105E+00	--.290601E+00	--.236822E+01	.463811E-02	.300000E-04	--.100000E+01		1
DANG	.645075E+00	--.290601E+00	--.236822E+01	.458907E-02	.300000E-04	.100000E+01		1
DANG	.645045E+00	--.290601E+00	--.236822E+01	.454415E-02	.300000E-04	--.100000E+01		1
DANG	.645015E+00	--.290601E+00	--.236822E+01	.450367E-02	.300000E-04	.100000E+01		1
DANG	.644985E+00	--.290601E+00	--.236822E+01	.446817E-02	.300000E-04	--.100000E+01		1
DANG	.644955E+00	--.290601E+00	--.236822E+01	.443865E-02	.300000E-04	.100000E+01		1
DANG	.644925E+00	--.290601E+00	--.236822E+01	.441708E-02	.300000E-04	--.100000E+01		1



DANG	.644895E+00	-.290601E+00	-.236822E+01	.440655E-02	.300000E-04	-.100000E+01	1
DANG	.644895E+00	-.290601E+00	-.236822E+01	.440655E-02	.300000E-04	-.100000E+01	1
DANG	.644895E+00	-.290751E+00	-.236822E+01	.440655E-02	.300000E-04	-.100000E+01	2
DANG	.644895E+00	-.290631E+00	-.236822E+01	.435426E-02	.300000E-04	-.100000E+01	2
DANG	.644895E+00	-.290601E+00	-.236822E+01	.430416E-02	.300000E-04	-.100000E+01	2
DANG	.644895E+00	-.290691E+00	-.236822E+01	.429681E-02	.300000E-04	-.100000E+01	2
DANG	.644895E+00	-.290721E+00	-.236822E+01	.429358E-02	.300000E-04	-.100000E+01	2
DANG	.644895E+00	-.290751E+00	-.236822E+01	.429205E-02	.300000E-04	-.100000E+01	2
DANG	.644895E+00	-.290781E+00	-.236822E+01	.429495E-02	.300000E-04	-.100000E+01	2
DANG	.644895E+00	-.290751E+00	-.236819E+01	.428149E-02	.300000E-04	-.100000E+01	3
DANG	.644895E+00	-.290751E+00	-.236816E+01	.427080E-02	.300000E-04	-.100000E+01	3
DANG	.644895E+00	-.290751E+00	-.236813E+01	.426055E-02	.300000E-04	-.100000E+01	3
DANG	.644895E+00	-.290751E+00	-.236810E+01	.425169E-02	.300000E-04	-.100000E+01	3
DANG	.644895E+00	-.290751E+00	-.236807E+01	.424338E-02	.300000E-04	-.100000E+01	3
DANG	.644895E+00	-.290751E+00	-.236804E+01	.423594E-02	.300000E-04	-.100000E+01	3
DANG	.644895E+00	-.290751E+00	-.236801E+01	.422939E-02	.300000E-04	-.100000E+01	3
DANG	.644895E+00	-.290751E+00	-.236798E+01	.422373E-02	.300000E-04	-.100000E+01	3
DANG	.644895E+00	-.290751E+00	-.236795E+01	.421891E-02	.300000E-04	-.100000E+01	3
DANG	.644895E+00	-.290751E+00	-.236792E+01	.421490E-02	.300000E-04	-.100000E+01	3
DANG	.644895E+00	-.290751E+00	-.236789E+01	.421164E-02	.300000E-04	-.100000E+01	3
READ PT. PIERCE PT., ERROR	1	-.400033E-01	.215833E+00	-.395739E-01	.216441E+00	.793244E-03	
ITH OBJECT POINT AND DISTANCE VECTOR							
1	.378908E+01	.149210E+01	.376825E+01	.361395E-02	-.516666E-02	-.712783E-02	.951632E-02
READ PT. PIERCE PT., ERROR	2	-.126750E+00	.210000E+00	-.126736E+00	.217987E+00	.186950E-04	
ITH OBJECT POINT AND DISTANCE VECTOR							
2	.380208E+01	.325500E+00	.376300E+01	.619822E-04	-.131012E-03	.134775E-03	.197915E-03
READ PT. PIERCE PT., ERROR	3	-.230583E+00	.220917E+00	-.230635E+00	.220655E+00	.267077E-03	
ITH OBJECT POINT AND DISTANCE VECTOR							
3	.380992E+01	-.841167E+00	.376567E+01	-.294285E-03	.665930E-03	.256087E-02	.266235E-02
READ PT. PIERCE PT., ERROR	4	.156833E+00	-.158417E+00	.156881E+00	-.158629E+00	.217765E-03	
ITH OBJECT POINT AND DISTANCE VECTOR							
4	.540070E-01	.109370E+01	.487000E+00	.987714E-03	.340796E-03	.157745E-02	.189211E-02
READ PT. PIERCE PT., ERROR	5	.116833E+00	-.159187E+00	.116832E+00	-.159100E+00	.663036E-04	
ITH OBJECT POINT AND DISTANCE VECTOR							
5	.729170E-01	.583330E+00	.648417E+00	-.214034E-03	-.171378E-03	-.477003E-03	.550193E-03
READ PT. PIERCE PT., ERROR	6	.672500E-01	-.176917E+00	.652500E-01	-.177516E+00	.208735E-02	
ITH OBJECT POINT AND DISTANCE VECTOR							
6	.833330E-01-0.	.677003E+00	-.870255E-02	.134540E-01	.488198E-02	.167519E-01	
READ PT. PIERCE PT., ERROR	7	.695833E-01	-.224003E+00	.699013E-01	-.223508E+00	.657594E-03	
ITH OBJECT POINT AND DISTANCE VECTOR							
7	.783300E-02-0.	.291667E+00	-.264507E-03	-.353970E-02	-.378272E-02	.518737E-02	
X,Y,Z,F,AZ,EL,TILT	-.330763E+01	-.326210E+01	.327318E+01	.666667E+00	.644790E+00	-.236778E+01	
ERROR/LITER.	.410803E-02	137					
DANG, IHI, PHI, TILT	.221372E+01	.624950E-02	.652331E-02				
NORMAL COMPLETION							

APPENDIX F  
PROGRAM SLED AND TYPICAL  
LISTING OF SOLUTIONS

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PROGRAM SLED (INPUT, OUTPUT, PUNCH, TAPE5=INPUT, TAPE6=OUTPUT,
1 TAPE7=PUNCH)
COMMON RAA, RAB, RAC, FAC, THA, PHA, GA, RBA, RBB, RBC, FB, THB, PHB,
1GB, THIA, PHIA, THIB, PHIB
DIMENSION NFKA(150), NFRB(150), XA(150,8), YA(150,8), XB(150,8),
1YB(150,8), TA(150), TB(150), XX(10), YY(10), ZZ(10), TREFB(10),
2TREFB(10), NREFB(10), NREFB(10), SDEB(8), SDEB(8)
1 READ(5,2) RAA, RAB, RAC, FAC, THA, PHA, GA, THIA, PHIA
1 IF(ICHK.EQ.0) GO TO 999
NCHK=J
READ(2,2) RBA, RBB, RBC, FB, THB, PHB, GB, THIB, PHIB
FORMAT(4F10.0/5F10.0)
NA=J
NB=J
NA=NA+1
NFKA(NA), ((XA(NA,I), YA(NA,I)), I=1,8)
FORMAT(15,8F7.0/5X,8F7.0)
IF(NFKA(NA).NE.99999) GO TO 3
NA=NA+1
DO 100 I=1,NA
DO 100 J=1,8
XA(I,J)=-XA(I,J)/12000.0
YA(I,J)=YA(I,J)/12000.0
NB=NB+1
NFRB(NB), ((XB(NB,I), YB(NB,I)), I=1,8)
READ(2,4) NFRB(NB), ((XB(NB,I), YB(NB,I)), I=1,8)
IF(NFRB(NB).NE.99999) GO TO 5
NB=NB+1
DO 101 I=1,NB
DO 101 J=1,8
XB(I,J)=-XB(I,J)/12000.0
YB(I,J)=YB(I,J)/12000.0
NHP=NHP+1
NHP=NHP+1
READ(2,7) XX(NHP), YY(NHP), ZZ(NHP)
FORMAT(3F10.0)
IF(XX(NHP).LT.99999.0) GO TO 6
NHP=NHP+1
WRITE(6,6) RAA, RAB, RAC, FAC, THA, PHA, GA, THIA, PHIA

```

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      WRITE(6,8) KBA,KB,KB,FB,THB,PHB,GB,TH1B,PH1B
      FORMAT(12H CAMERA DATA/9E13.6)
      DO 9 I=1,NHP
      WRITE(6,10) XX(I),YY(I),ZZ(I)
      FORMAT(16H HAKO PI LOCATIONS,3E13.6)
      CONTINUE
      NTMA=J
      NTMA=NTMA+1
      READ(5,12) TREFB(NTMA),NREFA(NTMA)
      FORMAT(F10.0,16)
      IF(NREFA(NTMA).LT.99999) GO TO 11
      NTMA=NTMA-1
      NTMB=J
      NTMB=NTMB+1
      READ(5,12) TREFB(NTMB),NREFB(NTMB)
      IF(NREFB(NTMB).LT.99999) GO TO 13
      NTMB=NTMB-1
      DO 14 I=1,NTMA
      WRITE(6,15) TREFB(I),NREFA(I),NTMA
      FORMAT(20H REF TIMES&FRAME NOS,E13.6,2I5)
      CONTINUE
      DO 16 I=1,NTMB
      WRITE(6,15) TREFB(I),NREFB(I),NTMB
      CONTINUE
      CALL TMSGN(NTMA,NA,NREFA,TREFB,NFRA,IA)
      CALL TMSGN(NTMB,NB,NREFB,TREFB,NFRB,IB)
      DO 17 I=1,NA
      WRITE(6,18) I,NFRA(I),IA(I),((XA(I,J),YA(I,J)),J=1,8)
      FORMAT(2I6,E13.6/8E13.6)
      CONTINUE
      DO 19 I=1,NB
      WRITE(6,18) I,NFRB(I),IB(I),((XB(I,J),YB(I,J)),J=1,8)
      CONTINUE
      READ(5,20) DT,DESIG
      FORMAT(2F10.0)
      WRITE(6,21) DT
      FORMAT(6,21) DT
      CALL ALL(NA,NB,IA,IB,NFRA,NFRB,XA,YA,XB,YB,SMEAN,SSDEV,
      10I,XX,YY,ZZ,DESIG,NCHK)
      GO TO 1
      WRITE(6,1000)
      FORMAT(16H NORMAL COMPLETION)
      STOP
      END

```



```

1
1000
BOT=SIN(TH)
AA=SIN(TH)/BOT
BB=SIN(THS)/BOT
TF=AA*RF+BB*SF
TI=AA*KI+BB*SI
IJ=AA*KJ+BB*SJ
TIM=SFRT(TF**2+TI**2+IJ**2)
XK=TF/TI
P=XK*TI
Q=XK*IJ
GO TO 1000
P=PPA
Q=QQA
RETURN
END
SUBROUTINE SOLVE(PA,QA,PB,QB,NT,SOLA,SOLB,SOLC,D,J,NCHK,NTR)
COMMON KAA,RAB,KAC,FA,THA,PHA,GA,RBA,RBB,RBC,FB,PHB,PHB,
1GB,THIA,PHIA,THIB,PHIB
IF (NT.GT.0) GO TO 1
IF (NCHK.EQ.0) GO TO 2
THA=THAP
PHA=PHAP
THIA=THIAP
PHIA=PHIAP
THB=THBP
PHB=PHBP
THIB=THIBP
PHIB=PHIBP
GA=GAP
GB=GBP
FAA=FA*COS(THA)*COS(THA)
FAB=FA*SIN(THA)*COS(THA)
FAC=FA*SIN(THA)*SIN(THA)
FBA=FB*COS(THB)*COS(THB)
FBB=FB*SIN(THB)*COS(THB)
FBC=FB*SIN(THB)*SIN(THB)
FAAB=ABS(FA)
FBAAB=ABS(FB)
CHKA=(FAA*FBA+FA*FBB+FA*FBC)/(FAAB*FBAAB)
IF (CHKA.GT.1.0) CHKA=1.0
IF (CHKA.LT.-1.0) CHKA=-1.0
CHAN=ACOS(CHKA)
IF (CHAN.LT.1.57079) GO TO 101
WRITE(6,102) FA,THA,PHA,FB,THB,PHB,CHAN

```

```

SUBROUTINE IMSGN(NTM,N,NREF,TREF,NFR,I)
DIMENSION NREF(10),TREF(10),NFR(150),T(150)
NST=NTM-1
DO 2 J=1,NST
K=J+1
DO 4 L=1,N
IF (NFR(L).NE. NREF(K)) GO TO 4
M=L
GO TO 7
CONTINUE
4 IF (J.EQ. 1) NB=1
7 IF (K.EQ.NTM) GO TO 3
NE=M
GO TO 6
NE=N
3 DNU=TREF(K)-TREF(J)
6 DEN=NREF(K)-NREF(J)
FRA=DNU/DEN
DO 5 I=NB,NE,1
FAC=M-I
5 I(I)=TREF(K)-FRA*FAC
IF (NE.EQ.N) GO TO 1000
NB=NE
CONTINUE
RETURN
END
SUBROUTINE FIND(F,PPA,QQA,PPB,QQB,TS,TAS,TBS,P,Q)
R=ABS(PPA-PPB)
S=ABS(QQA-QQB)
IF (R.LT.0.000001).AND.(S.LT.0.000001)) GO TO 1
WRITE(6,100)TAS,PPA,QQA,PPB,QQB,TS
FORMAT(5H FIND,6E13.6)
100 R=SQRT(F**2+PPA**2+QQA**2)
S=SQRT(F**2+PPB**2+QQB**2)
RF=F/R
RI=PPA/R
RJ=QQA/K
SF=F/S
SI=PPB/S
SJ=QQB/S
ARGU=SQRT((RI*SJ-RJ*SI)**2+(RJ*SF-RF*SJ)**2+(RF*SI-RI*SF)**2)
TH=ASIN(ARGU)
IHS=(TS-TAS)*TH/(TBS-TAS)
THI=TH

```

```

RNC=RNC/DRN
D=(RAA-RBA)*RNA+(RAB-RBB)*RNB+(RAC-RBC)*RNC
O=(SAA+SBA+SAB+SBB+SAC+SBC)*SAA+(RBB-RAB)*SAB+(RBC-RAC)*SAC
P=(RBA-KAA)*SBA+(RBB-RAB)*SAB+(RBC-RAC)*SBC
Q=(RBA-KAA)*SBA+(RBB-RAB)*SAB+(RBC-RAC)*SBC
COB=(P+Q)/(1.0-0.2)
COA=P+COB*0
SOLA=RBA+COB*SBA+0.5*0.5*RNA
SOLB=RBB+COB*SBB+0.5*0.5*RNB
SOLC=RBC+COB*SBC+0.5*0.5*RNC
SOLD=RBA+COA*SAA-0.5*0.5*RNA
SOLE=RAB+COA*SAB-0.5*0.5*RNB
SOLF=RAC+COA*SAC-0.5*0.5*RNC
KRYA=D*RNA
KRYB=D*RNB
KRYC=D*RNC
IF (NCHK.GT. 0) GO TO 1000
CALL CORR(SOLA,SOLB,SOLC,PA,QA,PB,QB,D,J,NTR,NT,THAP,
1PHAP,THIAP,PHIAP,GAP,THBP,PHBP,GBP,SAA,SAB,
2SAC,SBA,SBB,SBC,AIA,AIB,AIC,AJA,AJB,AJC,BIA,BIB,BIC,BJA,BJB,BJC)
1000 RETURN
END
SUBROUTINE CORR(SOLA,SOLB,SOLC,PA,QA,PB,QB,D,J,NTR,NT,THAP,
1PHAP,THIAP,PHIAP,GAP,THBP,PHBP,GBP,SAA,SAB,
2SAC,SBA,SBB,SBC,AIA,AIB,AIC,AJA,AJB,AJC,BIA,BIB,BIC,BJA,BJB,BJC)
COMMON RAA,RAB,RAC,FA,THA,PHA,GA,RBA,RBB,RBC,FB,PHB,
1GB,THIA,PHIA,THIB,PHIB
DIMENSION T(3,4),SA(3,4),SB(3,4),DEKR(4),TA(3,4),TB(3,4),
1TAE(3),TAF(3),TBE(3),TBF(3),SAF(3),SBE(3),SBF(3),
2TAG(3),TBG(3),SAG(3),SBG(3),TAH(3),TBH(3),SAH(3),SBH(3),
3TAI(3),TBI(3),SAI(3),SBI(3)
IF (NT.GT. 0) GO TO 1
FA=COS(THA)*COS(PHA)
FAN=SIN(THA)*COS(PHA)
FBE=COS(THB)*COS(PHB)
FBN=SIN(THB)*COS(PHB)
STHAP=U.U
SGAP=U.U
STHBP=U.U
SGBP=U.U

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102 FORMAT(35H BAU CAMERA DATA PROBABLE SEE SOLVE/7E13.6)
101 CONTINUE
AIA=COS(THIA)*COS(PHIA)
AIB=SIN(THIA)*COS(PHIA)
AIC=SIN(THIA)*COS(PHIB)
BIA=COS(THIB)*COS(PHIB)
BIB=SIN(THIB)*COS(PHIB)
BIC=SIN(THIB)*COS(PHIB)
AJA=(FAB*AIC-FAC*AIB)/FA
AJB=(FAC*AIB-FAA*AIC)/FA
AJC=(FAA*AIB-FAB*AIC)/FA
BJA=(FBB*BIC-FBC*BIB)/FB
BJB=(FBC*BIA-FBA*BIB)/FB
BJC=(FBA*BIB-FBB*BIA)/FB
SAA=FAA+PA+IA+QA+AJA
WRITE(6,105) PA, QA, PB, QB, SOLA, SOLB, SOLC, NT
105 FORMAT(6H SOLVE,7E13.6,15)
SAB=FAB+PA+AI+QA+AJB
SAC=FAC+PA+AI+QA+AJC
SBA=FBA+PB+BI+QA+BJA
SBB=FBB+PB+BI+QA+BJB
SBC=FBC+PB+BI+QA+BJC
DSA=SQR1(SAA**2+SAB**2+SAC**2)
DSB=SQR1(SBA**2+SBB**2+SBC**2)
SAA=SAA/DSA
SAB=SAB/DSA
SAC=SAC/DSA
SBA=SBA/DSB
SBB=SBB/DSB
SBC=SBC/DSB
CHKA=3AA*SBA+SAB*SBB+SAC*SBC
IF (CHKA .GT. 1.0) CHKA=1.0
IF (CHKA .LT. -1.0) CHKA=-1.0
CHAN=ACOS(CHKA)
IF (CHAN .LT. 1.57079) GO TO 103
WRITE(6,104) PA, QA, PB, QB, CHAN
104 FORMAT(39H BAD FILM FRAME DATA PROBABLE SEE SOLVE,5E13.6)
103 CONTINUE
RNA=SAC*SBC-SAB*SBB
RNB=SAC*SBA-SAA*SBC
RNC=SAA*SBB-SAB*SBA
RDN=SQR1(RNA**2+RNB**2+RNC**2)
RNB=RNB/DRN

```



TBFF=SQRT(I(TBF(1)\*\*2+TBF(2)\*\*2+TBF(3)\*\*2)  
 DSAPF=SQRT(SAE(1)\*\*2+SAE(2)\*\*2+SAE(3)\*\*2)  
 DSBEF=SQRT(SBE(1)\*\*2+SBE(2)\*\*2+SBE(3)\*\*2)  
 DSBF=SQRT(SBF(1)\*\*2+SBF(2)\*\*2+SBF(3)\*\*2)  
 DO 8 I=1,3  
 TAE(I)=TAE(I)/DTAE  
 TAF(I)=TAF(I)/DTAF  
 TBE(I)=TBE(I)/DTBE  
 TBF(I)=TBF(I)/DTBF  
 SAE(I)=SAE(I)/DSAE  
 SBE(I)=SBE(I)/DSBE  
 SBF(I)=SBF(I)/DSBF

8

CONTINUE  
 DO 9 I=1,3  
 TAG(I)=TAG(I)+TAF(I)  
 TBG(I)=TBE(I)+TBF(I)  
 SAG(I)=SAE(I)+SBF(I)  
 SBG(I)=SBE(I)+SBF(I)

9

CONTINUE  
 DTAG=SQRT(TAG(1)\*\*2+TAG(2)\*\*2+TAG(3)\*\*2)  
 DTBG=SQRT(TBG(1)\*\*2+TBG(2)\*\*2+TBG(3)\*\*2)  
 DSAG=SQRT(SAG(1)\*\*2+SAG(2)\*\*2+SAG(3)\*\*2)  
 DSBG=SQRT(SBG(1)\*\*2+SBG(2)\*\*2+SBG(3)\*\*2)  
 DO 6 I=1,3  
 TAG(I)=TAG(I)/DTAG  
 TBG(I)=TBG(I)/DTBG  
 SAG(I)=SAG(I)/DSAG  
 SBG(I)=SBG(I)/DSBG

6

CONTINUE  
 TAF(1)=TAE(2)\*TAF(3)-TAE(3)\*TAF(2)  
 TAF(2)=TAE(3)\*TAF(1)-TAE(1)\*TAF(3)  
 TAF(3)=TAE(1)\*TAF(2)-TAE(2)\*TAF(1)  
 TBE(1)=TBE(3)\*TBF(2)-TBE(2)\*TBF(3)  
 TBE(2)=TBE(2)\*TBF(3)-TBE(3)\*TBF(2)  
 TBE(3)=TBE(1)\*TBF(2)-TBE(2)\*TBF(1)  
 TBF(1)=TBF(3)\*TBE(2)-TBF(2)\*TBE(3)  
 TBF(2)=TBF(2)\*TBE(3)-TBF(3)\*TBE(1)  
 TBF(3)=TBF(1)\*TBE(2)-TBF(2)\*TBE(3)  
 SAE(1)=SAE(3)\*SBF(2)-SAE(2)\*SBF(3)  
 SAE(2)=SAE(2)\*SBF(3)-SAE(3)\*SBF(2)  
 SAE(3)=SAE(1)\*SBF(2)-SAE(2)\*SBF(1)  
 SBE(1)=SBE(3)\*SBF(1)-SBE(2)\*SBF(3)  
 SBE(2)=SBE(1)\*SBF(3)-SBE(3)\*SBF(1)  
 SBE(3)=SBE(2)\*SBF(1)-SBE(1)\*SBF(2)  
 SBF(1)=SBF(3)\*SAG(2)-SBF(2)\*SAG(3)  
 SBF(2)=SBF(2)\*SAG(3)-SBF(3)\*SAG(1)  
 SBF(3)=SBF(1)\*SAG(2)-SBF(2)\*SAG(1)

```

1 K=J-4
  I(1,K)=SOLA
  I(2,K)=SOLC
  I(3,K)=SOLD
  SAI(1,K)=SAA
  SAI(2,K)=SAB
  SAI(3,K)=SAC
  SBI(1,K)=SBA
  SBI(2,K)=SBB
  SBI(3,K)=SBC
  DER(K)=0
  IF (K.LI.4) GO TO 1000
  DO 2 I=1,4
    IF (DERK(I).GT.0.75) GO TO 1000
2 CONTINUE
  NTR=NTR+1
  DO 3 I=1,4
    I(1,I)=I(1,I)-RAA
    I(2,I)=I(2,I)-RAB
    I(3,I)=I(3,I)-RBA
    IB(1,I)=I(1,I)-RBB
    IB(2,I)=I(2,I)-RBC
    UAM=SQR(I(1,I)**2+I(2,I)**2+I(3,I)**2)
    DBM=SQR(I(1,I)**2+I(2,I)**2+I(3,I)**2)
    IA(1,I)=IA(1,I)/OAM
    IA(2,I)=IA(2,I)/OAM
    IA(3,I)=IA(3,I)/OAM
    IB(1,I)=IB(1,I)/DBM
    IB(2,I)=IB(2,I)/DBM
    IB(3,I)=IB(3,I)/DBM
3 CONTINUE
  DO 4 I=1,3
    IAE(I)=IA(I,1)+IA(I,2)
    IAF(I)=IA(I,3)+IA(I,4)
    IBE(I)=IB(I,1)+IB(I,2)
    IBF(I)=IB(I,3)+IB(I,4)
    SAE(I)=SA(I,1)+SA(I,2)
    SAF(I)=SA(I,3)+SA(I,4)
    SBE(I)=SB(I,1)+SB(I,2)
    SBF(I)=SB(I,3)+SB(I,4)
4 CONTINUE
  DIAE=SQR(TIAE(1)**2+IAE(2)**2+IAE(3)**2)
  DIAF=SQR(TIAF(1)**2+IAF(2)**2+IAF(3)**2)
  DIBE=SQR(TIBE(1)**2+IBE(2)**2+IBE(3)**2)

```

BIGG=3IA\*SBG(1)+BIB\*SBG(2)+BIC\*SBG(3)  
 BII=3IA\*SBI(1)+BIB\*SBI(2)+BIC\*SBI(3)  
 BIH=3IA\*SBH(1)+BIB\*SBH(2)+BIC\*SBH(3)  
 BJGG=3JA\*SBG(1)+BJB\*SBG(2)+BJC\*SBG(3)  
 BJII=3JA\*SBI(1)+BJB\*SBI(2)+BJC\*SBI(3)  
 BJHH=3JA\*SBH(1)+BJB\*SBH(2)+BJC\*SBH(3)  
 FBXX=FBGG\*IBG(1)+FBI\*IBI(1)+FBHH\*IBH(1)  
 FBYY=FBGG\*IBG(2)+FBI\*IBI(2)+FBHH\*IBH(2)  
 FBZZ=FBGG\*IBG(3)+FBI\*IBI(3)+FBHH\*IBH(3)  
 BIYY=3IGG\*IBG(1)+BIII\*IBI(1)+BIHH\*IBH(1)  
 BIZZ=3IGG\*IBG(2)+BIII\*IBI(2)+BIHH\*IBH(2)  
 BJXX=3JGG\*IBG(1)+BJII\*IBI(1)+BJHH\*IBH(1)  
 BJYY=3JGG\*IBG(2)+BJII\*IBI(2)+BJHH\*IBH(2)  
 BJZZ=3JGG\*IBG(3)+BJII\*IBI(3)+BJHH\*IBH(3)  
 THBP=ACOS(FBXX/SQRT(FBXX\*\*2+FBYY\*\*2))  
 IF (FBYY.LT.0.0) THBP=-THBP  
 PHBP=ASIN(FBZZ)  
 THAP=ACOS(FAXX/SQRT(FAXX\*\*2+FAYY\*\*2))  
 IF (FAYY.LT.0.0) THAP=-THAP  
 PHAP=ASIN(FAXX\*\*2+FAYY\*\*2)  
 DFA=SQRT(FAXX\*\*2+FAYY\*\*2)  
 FAHX=FAXX/DFA  
 FAYH=FAYY/DFA  
 GAP=ACOS(AHX\*FAHX+AIYY\*FAHY)  
 IF (AIZZ.LT.0.0) GAP=-GAP  
 DFB=SQRT(FBXX\*\*2+FBYY\*\*2)  
 FBHX=FBXX/DFB  
 FBHY=FBYY/DFB  
 GBP=ACOS(BIXX\*FBHX+BIYY\*FBHY)  
 IF (BIZZ.LT.0.0) GBP=-GBP  
 STHAP=STHAP+THAP  
 SGAP=SGAP+GAP  
 STHBP=STHBP+THBP  
 SPHBP=SPHBP+PHBP  
 SGBP=SGBP+GBP  
 XNTR=XNTR  
 THAP=STHAP/XNTR  
 PHAP=SPHAP/XNTR  
 GAP=SGAP/XNTR  
 THBP=STHBP/XNTR  
 PHBP=SPHBP/XNTR  
 GBP=SGBP/XNTR  
 FAXX=COS(THAP)\*COS(PHAP)

```

DIAH=SQRT(IAH(1))*2+IAH(2))*2+IAH(3))*2)
DTBH=SQRT(TBH(1))*2+TBH(2))*2+TBH(3))*2)
DSAH=SQRT(SAH(1))*2+SAH(2))*2+SAH(3))*2)
DSBH=SQRT(SBH(1))*2+SBH(2))*2+SBH(3))*2)
DO 7 I=1,3
TAH(I)=TAH(I)/DIAH
TBH(I)=TBH(I)/DTBH
SAH(I)=SAH(I)/DSAH
SBH(I)=SBH(I)/DSBH
CONTINUE
TAI(1)=TAH(2)*TAG(3)-TAH(3)*TAG(2)
TAI(2)=TAH(3)*TAG(1)-TAH(1)*TAG(3)
TAI(3)=TAH(1)*TAG(2)-TAH(2)*TAG(1)
TBI(1)=TBH(2)*TBG(3)-TBH(3)*TBG(2)
TBI(2)=TBH(3)*TBG(1)-TBH(1)*TBG(3)
TBI(3)=TBH(1)*TBG(2)-TBH(2)*TBG(1)
SAI(1)=SAH(2)*SAG(3)-SAH(3)*SAG(2)
SAI(2)=SAH(3)*SAG(1)-SAH(1)*SAG(3)
SAI(3)=SAH(1)*SAG(2)-SAH(2)*SAG(1)
SBI(1)=SBH(2)*SBG(3)-SBH(3)*SBG(2)
SBI(2)=SBH(3)*SBG(1)-SBH(1)*SBG(3)
SBI(3)=SBH(1)*SBG(2)-SBH(2)*SBG(1)
FAJG=FAE*SAI(1)+FAN*SAI(2)+FAH*SAI(3)
FAJI=FAE*SAH(1)+FAN*SAH(2)+FAH*SAH(3)
FAJG=FAE*SAI(1)+AIB*SAI(2)+AIC*SAI(3)
FAJI=FAE*SAH(1)+AIB*SAH(2)+AIC*SAH(3)
AJGG=AJA*SAI(1)+AJB*SAI(2)+AJC*SAI(3)
AJJI=AJA*SAH(1)+AJB*SAH(2)+AJC*SAH(3)
AJXX=AJA*SAI(1)+FAJI*TAI(1)+FAH*TAH(1)
AJYY=AJA*SAI(1)+FAJI*TAI(2)+FAH*TAH(2)
FAZZ=AJA*SAI(1)+FAJI*TAI(3)+FAH*TAH(3)
AIYY=AIJGG*TAG(1)+FAJI*TAI(1)+AIHH*TAH(1)
ALZZ=AIJGG*TAG(2)+FAJI*TAI(2)+AIHH*TAH(2)
AJXX=AJJGG*TAG(3)+FAJI*TAI(3)+AJHH*TAH(3)
AJYY=AJJGG*TAG(1)+AJJI*TAI(1)+AJHH*TAH(1)
AJZZ=AJJGG*TAG(2)+AJJI*TAI(2)+AJHH*TAH(2)
FBJG=FBF*SBG(1)+FBN*SBG(2)+FBN*SBG(3)
FBJI=FBF*SBH(1)+FBN*SBH(2)+FBN*SBH(3)
FBFH=FBF*SBH(1)+FBN*SBH(2)+FBN*SBH(3)

```

7



```

2, IIM(150), X(150,4), Y(150,4), Z(150,4), OD(150,4)
9 NTR=-1
TS=AMAX1(TA(1), TB(1))
N=IS/OT
XN=XN+DT
NTSP=0
NAS=1
NBS=1
DO 8 J=1,8
SSMEAN(J)=0.0
SSDEV(J)=0.0
TS=IS+DT
IF(TS.GT.AMAX1(TA(1), TB(1))) GO TO 2
GO TO 1
IF(TS.GT.AMIN1(TA(NA), TB(NB))) GO TO 1000
DO 3 I=NAS,NA+1
IF(TS.GE.TA(I)) GO TO 3
GO TO 4
CONTINUE
NAS=I-1
DO 5 I=NBS,NB+1
IF(TS.GE.TB(I)) GO TO 5
GO TO 6
CONTINUE
NBS=I-1
DO 7 J=5,8,1
PPA=XA(NAS,J)
QQA=YA(NAS,J)
PPB=XA(NAS+1,J)
QQB=YA(NAS+1,J)
TAS=TA(NAS)
TBS=TB(NAS+1)
CALL FIND(FA,PPA,QQB,TS,TAS,TBS,P,Q)
PA=P
QA=Q
PPA=XB(NBS,J)
QQA=YB(NBS,J)
PPB=XB(NBS+1,J)
QQB=YB(NBS+1,J)
TAS=TB(NBS)
TBS=TB(NBS+1)
CALL FIND(FB,PPA,QQB,TS,TAS,TBS,P,Q)

```

8 1 2 3 4 5 6

```

FAYY=3IN(THAP)*COS(PHAP)
FAZZ=3IN(PHAP)
FBXX=COS(THBP)*COS(PHBP)
FBYY=3IN(THBP)*COS(PHBP)
FBZZ=3IN(PHBP)
DFA=SQRT(FAXX**2+FAYY**2)
FAHX=-FAYY/DFA
FAHY=FAXX/DFA
FAVX=-FAHY*FAZZ
FAVY=FAHX*FAZZ
FAVZ=FAHY*FAHX-FAHX*FAYY
COGAP=COS(GAP)
SIGAP=3IN(GAP)
AIXX=COGAP*FAHX+SIGAP*FAVX
AIYY=COGAP*FAHY+SIGAP*FAVY
AIZZ=SIGAP*FAVZ
THIAP=ACOS(AIXX/SQRT(AIXX**2+AIYY**2))
IF (AIYY.LT.0.0) THIAP=-THIAP
PHIAP=ASIN(AIZZ)
DFB=SQRT(FBXX**2+FBYY**2+FBZZ**2)
FBHX=-FBYY/DFB
FBHY=FBXX/DFB
FBVX=-FBHY*FBZZ
FBVY=FBHX*FBZZ
FBVZ=FBHY*FBXX-FBHX*FBYY
COGBP=COS(GBP)
SIGBP=3IN(GBP)
BIXX=COGBP*FBHX+SIGBP*FBVX
BIYY=COGBP*FBHY+SIGBP*FBVY
BIZZ=SIGBP*FBVZ
THIBP=ACOS(BIXX/SQRT(BIXX**2+BIYY**2))
IF (BIYY.LT.0.0) THIBP=-THIBP
PHIBP=ASIN(BIZZ)
WRITE(6,999)THAP,PHAP,THIAP,PHIAP,GAP,THBP,
1PHBP,THIBP,PHIBP,GBP
999 FORMAT(5H CORR,5E13.6/5X,5E13.6)
1000 RETURN
END
SUBROUTINE ALL(NA,NB,IA,IB,NFRA,NFRB,XA,YA,XB,YB,SMEAN,
1SSDEV,DI,XX,YY,ZZ,DESIG,NCHK)
COMMON RAA,RAB,KAC,FA,THA,PHA,GA,RBA,RBB,RBC,FB,THB,PHB,
1GB,THIA,PHIA,THIB,PHIB
DIMENSION TA(150),TB(120),NFRA(150),NFRB(150),XA(150,8),YA(150,8),
1XB(150,8),YB(150,8),SMEAN(8),SSDEV(8),XX(10),YY(10),ZZ(10)

```

```

PB=P
NT=NT+1
CALL SOLVE(PA,QA,PB,QB,NT,SOLA,SOLB,SOLC,D,J,NCHK,NTR)
IF (J.NE.5) GO TO 15
NTESP=NTESP+1
IIM(NTESP)=IS
15 ID=J-1
X(NTESP,ID)=SOLA*12.0
Y(NTESP,ID)=-SOLB*12.0
Z(NTESP,ID)=SOLC*12.0
D=ABS(D)
DD(NTESP,ID)=D*12.0
SMEAN(J)=SMEAN(J)+D
SSDEV(J)=SSDEV(J)+D**2
CONTINUE
GO TO 1
1000 XN=NTESP
DO 10 J=1,8
ARGA=SMEAN(J)**2/XN
SSDEV(J)=(SSDEV(J)-ARGA)/(XN-1.0)
SSDEV(J)=SQRT(SSDEV(J))*12.0
SMEAN(J)=SMEAN(J)*12.0/XN
WRITE(6,11) NTESP,J,SMEAN(J),SSDEV(J)
FORMAT(25H NO OF PTS,PT NO,MEAN,DEV,2I5,2E13.6)
11 10 CONTINUE
DO 12 J=5,7,2
K=J+1
ID=J-4
JD=J-3
I=1,NTESP
DO 12 I=1,NTESP
DIS=SQRT((X(I,JD)-X(I,ID))**2+(Y(I,JD)-Y(I,ID))**2+(Z(I,JD)-
12(I,ID))**2)
WRITE(6,14) IIM(I),X(I,ID),Y(I,ID),Z(I,ID),X(I,JD),Y(I,JD),
12(I,JD),DIS,J,K,DIS,DD(I,ID),DD(I,JD)
WRITE(7,13) IIM(I),X(I,ID),Y(I,ID),X(I,JD),Y(I,JD),
12(I,JD),DIS,J,K
12 CONTINUE
14 FORMAT(F5.3,6F6.2,5H RUN ,F5.0,5H PTS ,I2,5H AND ,I2,3E13.6)
13 FORMAT(F5.3,6F6.2,5H RUN ,F5.0,5H PTS ,I2,5H AND ,I2}
12 CONTINUE
IF (NCHK .GT. 0) GO TO 1001
NCHK=1
GO TO 9
1001 RETURN
END
" " " "

```



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152033E+00	.215333E+00	.59107E-01	.215333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
.55667E-01	.568333E-01	.601667E-01	.145333E-01	-.153000E+00	.610333E-01	-.110000E+00	.36167E-01
18	97	.177071E+00	.215333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
.151333E+00	.216000E+00	.216000E+00	.215333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
.563333E-01	.503197E-01	.503197E-01	.503000E-02	-.152500E+00	.736667E-01	-.116000E+00	.564167E-01
13	93	.179142E+00	.215333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
.15067E+00	.215417E+00	.215417E+00	.215417E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
.523333E-01	.461167E-01	.461167E-01	.215333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
20	93	.161213E+00	.215333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
.150750E+00	.215667E+00	.215667E+00	.215667E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
.517500E-01	.420000E-01	.420000E-01	.215333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
21	100	.183244E+00	.215333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
.150657E+00	.216000E+00	.216000E+00	.216000E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
.509333E-01	.361667E-01	.361667E-01	.215333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
22	101	.185355E+00	.215333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
.151433E+00	.216333E+00	.216333E+00	.216333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
.511657E-01	.340000E-01	.340000E-01	.215333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
23	102	.167426E+00	.215333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
.152417E+00	.215667E+00	.215667E+00	.215667E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
.509157E-01	.320833E-01	.320833E-01	.215333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
24	103	.189497E+00	.215333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
.152333E+00	.216250E+00	.216250E+00	.216250E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
.519333E-01	.316667E-01	.316667E-01	.215333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
25	104	.191566E+00	.215333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
.152157E+00	.216333E+00	.216333E+00	.216333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
.572500E-01	.212500E-01	.212500E-01	.212500E-01	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
25	105	.196333E+00	.215333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
.151317E+00	.215250E+00	.215250E+00	.215250E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
.543333E-01	.264167E-01	.264167E-01	.215333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
27	105	.195710E+00	.215333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
.151157E+00	.215250E+00	.215250E+00	.215250E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
.540000E-01	.234167E-01	.234167E-01	.215333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
28	107	.197818E+00	.215333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
.150750E+00	.215333E+00	.215333E+00	.215333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
.538333E-01	.239167E-01	.239167E-01	.215333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
29	108	.199655E+00	.215333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
.150250E+00	.215417E+00	.215417E+00	.215417E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
.557500E-01	.245833E-01	.245833E-01	.215333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
30	109	.201923E+00	.215333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
.150157E+00	.215667E+00	.215667E+00	.215667E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
.575657E-01	.244167E-01	.244167E-01	.215333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
31	110	.203944E+00	.215333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
.150750E+00	.216000E+00	.216000E+00	.216000E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
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32	111	.206055E+00	.215333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
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33	112	.208136E+00	.215333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
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-.391667E-01	.204417E+00	.204417E+00	.215333E+00	-.112500E+00	-.217500E+00	-.250333E+00	-.197250E+00
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FIND 141900E+00 732500E-01 133333E+00 713333E-01 136417E+00 142000E+00
FIND 140125E+00 800000E-01 150333E+00 742500E-01 146917E+00 142000E+00
SOLVE 731240E-01 139740E+00 723125E-01 147817E+00 649333E+00 -133775E+01 272575E+01 0
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SOLVE 473130E-01 127213E+00 114933E+00 13412E+00 126394E+00 142000E+00
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SOLVE 683768E-01 132344E+00 145014E+00 961702E+00 -136113E+01 243160E+01 12

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544754E+00	132417E+00	201667E-01	113363E+00	36708E+00	158000E+00	42	288643E+01	158000E+00
544754E+00	643646E-01	113020E+00	128250E+00	640000E-01	158000E+00	43	265737E+01	158000E+00
544754E+00	325219E+00	975785E+00	204760E-01	673199E+00	158000E+00	44	231266E+01	158000E+00
544754E+00	245561E+00	220672E+01	134163E-01	141565E-01	158000E+00	45	295221E+01	158000E+00
544754E+00	570000E-01	112083E+00	275001E-01	304474E-01	158000E+00	46	284789E+01	158000E+00
544754E+00	129333E+00	127333E+00	573167E-01	105333E+00	158000E+00	47	266462E+01	158000E+00
544754E+00	106571E+00	111750E+00	124625E+00	121317E+00	158000E+00	48	233845E+01	158000E+00
544754E+00	411667E-01	977500E-01	420000E-01	361558E+00	158000E+00	49	269386E+01	158000E+00
544754E+00	150250E+00	116833E+00	153333E+00	109500E+00	158000E+00	50	277174E+01	158000E+00
544754E+00	317537E-01	112752E+00	113166E+00	565000E-01	158000E+00			
544754E+00	120833E+00	647500E-01	118657E+00	613333E-01	158000E+00			
544754E+00	972080E-01	113745E+00	630406E-01	355543E+00	158000E+00			
544754E+00	133833E+00	640300E-01	130917E+00	625000E+00	158000E+00			
544754E+00	128250E+00	207500E-01	129333E+00	226333E-01	158000E+00			
544754E+00	626540E-01	128792E+00	217315E-01	672441E+00	158000E+00			
544754E+00	325080E+00	975625E+00	124716E-01	136845E-01	158000E+00			
544754E+00	295813E+00	220662E+01	28120E-01	309423E-01	158000E+00			
544754E+00	574167E-01	105333E+00	574167E-01	998633E-01	158000E+00			
544754E+00	17467E+00	12317E+00	134750E+00	116833E+00	158000E+00			
544754E+00	106614E+00	98833E-01	114525E+00	995547E+00	158000E+00			
544754E+00	820000E-01	103500E+00	157000E+00	102583E+00	158000E+00			
544754E+00	155333E+00	105611E+00	106247E+00	561951E+00	158000E+00			
544754E+00	830235E-01	96500E-01	163417E+00	536667E-01	158000E+00			
544754E+00	164250E+00	61333E-01	117750E+00	93500E-01	158000E+00			
544754E+00	944514E-01	118235E+00	548837E-01	338335E+00	158000E+00			
544754E+00	130917E+00	625000E-01	128917E+00	623333E-01	158000E+00			
544754E+00	62375E-01	226333E-01	128917E+00	231667E-01	158000E+00			
544754E+00	324862E+00	976174E+00	229900E-01	670043E+00	158000E+00			
544754E+00	296037E+00	220660E+01	28226E-01	315047E-01	158000E+00			
544754E+00	574167E-01	998633E-01	561667E-01	104417E+00	158000E+00			
544754E+00	134750E+00	116833E+00	137083E+00	11833E+00	158000E+00			
544754E+00	100001E+00	135777E+00	114633E+00	101655E-01	158000E+00			
544754E+00	441667E-01	604167E-01	460333E-01	784167E-01	158000E+00			
544754E+00	157000E+00	102543E+00	159667E+00	962503E-01	158000E+00			
544754E+00	790395E-01	158174E+00	99760E-01	552335E+00	158000E+00			
544754E+00	163417E+00	91667E-01	120833E+00	101667E+00	158000E+00			
544754E+00	117750E+00	582500E-01	118000E+00	553333E-01	158000E+00			
544754E+00	944514E-01	117460E+00	56865E-01	330531E+00	158000E+00			
544754E+00	128917E+00	62333E-01	127333E+00	705833E-01	158000E+00			
544754E+00	128917E+00	231667E-01	130500E+00	235833E-01	158000E+00			
544754E+00	680127E-01	129613E+00	23500E-01	678333E+00	158000E+00			
544754E+00	325218E+00	976271E+00	119595E-01	126211E-01	158000E+00			
544754E+00	295660E+00	220645E+01	287075E-01	313752E-01	158000E+00			
544754E+00	581667E-01	100417E+00	59000E-01	63000E-01	158000E+00			
544754E+00	137083E+00	111833E+00	135417E+00	106503E+00	158000E+00			
544754E+00	890040E-01	136395E+00	103645E+00	103234E+01	158000E+00			
544754E+00	460833E-01	784167E-01	502500E-01	572500E-01	158000E+00			
544754E+00	159667E+00	942500E-01	160667E+00	284167E-01	158000E+00			
544754E+00	665548E-01	160077E+00	930361E-01	551433E+00	158000E+00			
544754E+00	162083E+00	100667E+00	16417E+00	859167E-01	158000E+00			
544754E+00	118000E+00	553333E-01	119083E+00	52503E-01	158000E+00			
544754E+00	929721E-01	119444E+00	540691E-01	330144E+00	158000E+00			

FINO	.154643E+00	-.127333E+00	.705333E-01	-.112657E+00	.034167E-01	.165000E+00	
FINO	.165159E+00	-.130500E+00	.235333E-01	-.133417E+00	.236667E-01	.165000E+00	51
SOLVE	-.124932E+00	.039591E-01	-.131699E+00	.236175E-01	.507088E+00	.262793E+01	
CORR	-.590424E+00	-.325155E+00	.376169E+00	.118580E-01	.125143E-01		
FINO	.544774E+00	-.295552E+00	.226641E+00	.207203E-01	.313914E-01		
FINO	.166719E+00	.540000E-01	.030300E-01	.594333E-01	.752503E-01	.165000E+00	
FINO	.167219E+00	.135417E+00	.106500E+00	.134333E+00	.101373E+00	.165000E+00	
SOLVE	.583366E-01	.701925E-01	.135522E+00	.104726E+00	.121113E+01	.125215E+01	52
FINO	.166719E+00	.502500E-01	.572500E-01	.53333E-01	.44467E-01	.165000E+00	
FINO	.162162E+00	.160667E+00	.564167E-01	.51333E-01	.44467E-01	.165000E+00	
SOLVE	.162162E+00	-.161447E+00	.161332E+00	.040994E-01	.551136E+00	.165000E+00	53
FINO	.167219E+00	-.119083E+00	.522500E-01	.116333E+00	.600233E-01	.165000E+00	
SOLVE	.167219E+00	.071592E-01	.118748E+00	.506377E-01	.333712E+00	.165000E+00	54
FINO	.166719E+00	-.123667E+00	.604167E-01	.123033E+00	.601667E-01	.165000E+00	
FINO	.167219E+00	.133417E+00	.236667E-01	.112750E+00	.293333E-01	.165000E+00	
SOLVE	.123305E+00	.02617E-01	.133163E+00	.056136E-01	.120334E+00	.136143E+01	55
CORR	-.590313E+00	.113265E+00	.976495E+00	.118264E-01	.124742E-01		
FINO	.544300E+00	-.246265E+00	.220643E+01	.249580E-01	.31567E-01		
FINO	.160707E+00	.548333E-01	.752500E-01	.576667E-01	.675000E-01	.170000E+00	56
FINO	.169274E+00	.138333E+00	.101833E+00	.116500E+00	.945000E-01	.128603E+01	
SOLVE	.541466E-01	.707001E-01	.137691E+00	.932633E-01	.103438E+01	.170000E+00	
FINO	.166707E+00	.53333E-01	.444167E-01	.576667E-01	.314167E-01	.170000E+00	
FINO	.162707E+00	.162417E+00	.731667E-01	.161333E+00	.642503E-01	.170000E+00	
SOLVE	.559720E-01	.366006E-01	.162047E+00	.753408E-01	.539051E+00	.366286E+00	57
FINO	.160707E+00	-.159417E+00	.060833E-01	.159033E+00	.840833E-01	.170000E+00	
FINO	.163274E+00	-.118333E+00	.481667E-01	.113917E+00	.421667E-01	.170000E+00	
SOLVE	.153221E+00	.049117E-01	.118886E+00	.060664E-01	.342542E+00	.103278E+01	58
FINO	.160707E+00	-.123083E+00	.601667E-01	.121167E+00	.582503E-01	.170000E+00	
FINO	.169274E+00	.132750E+00	.29333E-01	.131667E+00	.316667E-01	.170000E+00	
SOLVE	.121960E+00	.590437E-01	.132331E+00	.701501E-01	.703453E+00	.136036E+01	59
CORR	-.590214E+00	-.226803E+00	.976580E+00	.11597E-01	.122368E-01		
FINO	.544300E+00	-.25685E+00	.220628E+01	.235514E-01	.320934E-01		
FINO	.170350E+00	.576667E-01	.675000E-01	.562500E-01	.613333E-01	.172000E+00	
SOLVE	.170350E+00	.135000E+00	.945000E-01	.135000E-01	.673333E-01	.172000E+00	60
FINO	.568951E-01	.640973E-01	.136019E+00	.922039E-01	.110170E+01	.230721E+01	
FINO	.170350E+00	.576667E-01	.314167E-01	.601667E-01	.223167E-01	.172000E+00	
FINO	.171340E+00	.161333E+00	.62500E-01	.157417E+00	.614167E-01	.172000E+00	
SOLVE	.530454E-01	.267291E-01	.160236E+00	.660603E-01	.547456E+00	.272033E+01	61
FINO	.170350E+00	-.159083E+00	.84083E-01	.159667E+00	.616667E-01	.172000E+00	
FINO	.171340E+00	-.119317E+00	.421667E-01	.113433E+00	.39000E-01	.172000E+00	
SOLVE	.153405E+00	.827506E-01	-.113890E+00	.603933E-01	.367755E+00	.252154E+01	62
FINO	.170350E+00	-.121167E+00	.582500E-01	.133667E+00	.576667E-01	.172000E+00	
FINO	.171340E+00	.131667E+00	.316667E-01	.135333E+00	.26333E-01	.172000E+00	
SOLVE	.113780E+00	.978252E-01	.132833E+00	.234604E-01	.712540E+00	.253127E+01	63
CORR	-.590138E+00	-.324423E+00	.976886E+00	.112161E-01	.113334E-01		
FINO	.544300E+00	-.546820E+00	.220614E+01	.297426E-01	.325696E-01	.174000E+00	
FINO	.172329E+00	.562500E-01	.613333E-01	.555667E-01	.565833E-01	.174000E+00	
SOLVE	.173402E+00	.135000E+00	.87333E-01	.135417E+00	.21667E-01	.126570E+01	64
FINO	.554482E-01	.588761E-01	.135121E+00	.853341E-01	.112417E+01	.239667E+01	
FINO	.172329E+00	.601667E-01	.229167E-01	.601667E-01	.145631E-01	.174000E+00	
FINO	.173402E+00	.157917E+00	.614167E-01	.155167E+00	.54000E-01	.174000E+00	
SOLVE	.601667E-01	.186064E-01	.157118E+00	.532633E-01	.544671E+00	.268533E+01	65
FINO	.172329E+00	-.118667E-01	.365000E-01	.121563E+00	.610833E-01	.174000E+00	
FINO	.173402E+00	-.159667E+00	.945000E-01	.121563E+00	.367503E-01	.174000E+00	
SOLVE	.153365E+00	.813650E-01	.585000E-01	.374924E-01	.394540E+00	.110562E+01	66
FINO	.172329E+00	-.135333E+00	.263333E-01	.139417E+00	.563167E-01	.174000E+00	
FINO	.173402E+00	.572704E-01	.136516E+00	.264541E-01	.267503E-01	.174000E+00	
SOLVE	-.113322E+00	.124313E+00	.977046E+00	.109037E-01	.714834E+00	.137262E+01	67
CORR	-.590065E+00	-.324313E+00	.977046E+00	.109037E-01	.115087E-01		
FINO	.644364E+00	-.296965E+00	.220603E+01	.300833E-01	.325015E-01	.176000E+00	
FINO	.175000E+00	.556667E-01	.548333E-01	.54333E-01	.505167E-01	.176000E+00	
FINO	.175464E+00	.135417E+00	.821667E-01	.131583E+00	.77333E-01	.176000E+00	
SOLVE	.550226E-01	.536460E-01	.134419E+00	.113155E-01	.115909E+00	.227276E+01	68
FINO	.175000E+00	.601667E-01	.165833E-01	.57533E-01	.50000E-02	.176000E+00	
FINO	.175464E+00	.155167E+00	.540000E-01	.150063E+00	.448333E-01	.176000E+00	

SOLVE	.501335E+01	.995645E+02	.153035E+00	.525545E+01	.544775E+00	.364135E+00	.244615E+01	69
FIND	.175000E+00	-.159000E+00	.067500E+01	-.150500E+00	.730000E+01	.176000E+00		
FIND	.179400E+00	-.121500E+00	.367500E+01	-.153000E+01	.365000E+00	.176000E+00		
SOLVE	.193000E+00	.003931E+01	.122100E+00	.366500E+01	.411630E+00	.176000E+00	.232995E+01	70
FIND	.175000E+00	-.118000E+00	.563100E+00	-.116000E+00	.564160E+00	.176000E+00		
FIND	.179400E+00	-.139417E+00	.267500E+01	-.135000E+00	.319335E+01	.176000E+00		
SOLVE	.117074E+00	.566752E+01	.113430E+00	.200000E+00	.729395E+00	-.137300E+01	.250226E+01	71
CORR	.503935E+00	-.324310E+00	.477250E+00	.105500E+01	.111303E+01			
FIND	.175000E+00	.543335E+01	.225915E+01	.304435E+01	.333000E+01	.176000E+00		
FIND	.175000E+00	.543335E+01	.225915E+01	.304435E+01	.333000E+01	.176000E+00		
SOLVE	.534335E+01	.491217E+01	.131410E+00	.772197E+01	.116715E+01	.176000E+00	.227015E+01	72
FIND	.177071E+00	.150683E+00	.466335E+01	.537500E+01	.103000E+02	.176000E+00		
FIND	.177071E+00	.150683E+00	.466335E+01	.537500E+01	.103000E+02	.176000E+00		
SOLVE	.556335E+01	.120521E+02	.143527E+00	.477374E+01	.559310E+00	.176000E+00	.263335E+01	73
FIND	.177171E+00	.156250E+00	.739567E+01	.157500E+00	.739535E+01	.176000E+00		
FIND	.177171E+00	.156250E+00	.739567E+01	.157500E+00	.739535E+01	.176000E+00		
SOLVE	.157951E+00	.746231E+01	.124031E+00	.366341E+01	.428951E+00	.176000E+00	.234194E+01	74
FIND	.177071E+00	.116000E+00	.564160E+01	.115635E+00	.569335E+01	.176000E+00		
FIND	.177071E+00	.116000E+00	.564160E+01	.115635E+00	.569335E+01	.176000E+00		
SOLVE	.115300E+00	.119500E+00	.315435E+01	.139175E+00	.289167E+01	.176000E+00	.249565E+01	75
CORR	.509310E+00	.324022E+00	.977440E+00	.102500E+01	.108133E+01			
FIND	.173142E+00	.523335E+01	.499157E+01	.517500E+01	.420000E+01	.180000E+00		
FIND	.173142E+00	.523335E+01	.499157E+01	.517500E+01	.420000E+01	.180000E+00	.226000E+01	76
SOLVE	.523194E+01	.440791E+01	.133550E+00	.744661E+01	.119459E+01	.180000E+00		
FIND	.179142E+00	.537500E+01	.100000E+02	.566667E+01	.430000E+02	.180000E+00		
FIND	.179142E+00	.537500E+01	.100000E+02	.566667E+01	.430000E+02	.180000E+00		
SOLVE	.543541E+01	.224258E+02	.147550E+00	.443667E+01	.558703E+00	.180000E+00	.258150E+01	77
FIND	.179142E+00	.157500E+00	.739535E+01	.147000E+00	.445000E+00	.180000E+00		
FIND	.179142E+00	.157500E+00	.739535E+01	.147000E+00	.445000E+00	.180000E+00		
SOLVE	.157410E+00	.793071E+01	.122950E+00	.371000E+01	.439220E+00	.180000E+00	.232012E+01	78
FIND	.179142E+00	.116583E+00	.269367E+01	.113951E+00	.268667E+01	.180000E+00		
FIND	.179142E+00	.116583E+00	.269367E+01	.113951E+00	.268667E+01	.180000E+00		
SOLVE	.113651E+00	.562116E+01	.139717E+00	.113335E+00	.563335E+01	.180000E+00	.249337E+01	79
CORR	.589335E+00	.323810E+00	.977171E+00	.992000E+02	.104736E+01			
FIND	.181213E+00	.123417E+00	.220568E+01	.312180E+01	.361543E+01	.182000E+00		
FIND	.181213E+00	.123417E+00	.220568E+01	.312180E+01	.361543E+01	.182000E+00	.226340E+01	80
SOLVE	.514016E+01	.405429E+01	.124261E+00	.703153E+01	.120139E+01	.182000E+00		
FIND	.181213E+00	.123417E+00	.220568E+01	.312180E+01	.361543E+01	.182000E+00		
FIND	.181213E+00	.123417E+00	.220568E+01	.312180E+01	.361543E+01	.182000E+00		
SOLVE	.592300E+01	.327207E+02	.146303E+00	.446266E+01	.564525E+00	.182000E+00	.254801E+01	81
FIND	.181213E+00	.123417E+00	.220568E+01	.312180E+01	.361543E+01	.182000E+00		
FIND	.181213E+00	.123417E+00	.220568E+01	.312180E+01	.361543E+01	.182000E+00		
SOLVE	.153913E+00	.789483E+01	.125764E+00	.373500E+01	.869002E+00	.186000E+00	.231555E+01	82
FIND	.181213E+00	.123417E+00	.220568E+01	.312180E+01	.361543E+01	.182000E+00		
FIND	.181213E+00	.123417E+00	.220568E+01	.312180E+01	.361543E+01	.182000E+00		
SOLVE	.113270E+00	.557450E+01	.113894E+00	.249215E+01	.766325E+00	.182000E+00	.249112E+01	83
CORR	.589779E+00	.323776E+00	.977803E+00	.957870E+02	.101037E+01			
FIND	.183884E+00	.504335E+01	.220568E+01	.312180E+01	.361543E+01	.184000E+00		
FIND	.183884E+00	.504335E+01	.220568E+01	.312180E+01	.361543E+01	.184000E+00		
SOLVE	.509486E+01	.367259E+01	.142675E+00	.433780E+01	.785838E+00	.184000E+00	.251671E+01	84
FIND	.183884E+00	.504335E+01	.220568E+01	.312180E+01	.361543E+01	.184000E+00		
FIND	.183884E+00	.504335E+01	.220568E+01	.312180E+01	.361543E+01	.184000E+00		
SOLVE	.633064E+01	.156500E+00	.790000E+01	.155167E+00	.871306E+00	.184000E+00		
FIND	.183884E+00	.504335E+01	.220568E+01	.312180E+01	.361543E+01	.184000E+00		
FIND	.183884E+00	.504335E+01	.220568E+01	.312180E+01	.361543E+01	.184000E+00		
SOLVE	.155033E+00	.748559E+01	.125670E+00	.393983E+01	.555000E+00	.184000E+00	.229143E+01	86
FIND	.183884E+00	.504335E+01	.220568E+01	.312180E+01	.361543E+01	.184000E+00		
FIND	.183884E+00	.504335E+01	.220568E+01	.312180E+01	.361543E+01	.184000E+00		
SOLVE	.113590E+00	.560997E+01	.136940E+00	.301667E+01	.773233E+00	.184000E+00	.243213E+01	87
CORR	.589707E+00	.323632E+00	.977566E+00	.934206E+02	.945353E+02			
FIND	.183884E+00	.504335E+01	.220568E+01	.312180E+01	.361543E+01	.186000E+00		
FIND	.183884E+00	.504335E+01	.220568E+01	.312180E+01	.361543E+01	.186000E+00		







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**INFORMATION**

6 March 1980

# ERRATA STATEMENT

AMRL-TR-78-94, "Photometric Methods for the Analysis of Human Kinematic Responses to Impact Environments", October 1978 is revised as follows:

1. Page 11 - First complete paragraph, sixth and seventh sentences,

"The resultant displacement . . . and in G's.",  
is changed to read,

A moving eleven point quadratic least square fit is then applied to these smoothed x and z-axis displacement data to obtain the x and z components of velocity. Next this same smoothing routine is applied to these x and z-axis velocity data to compute the x and z components of acceleration. The resultant displacement, velocity, and acceleration data are then computed using these smoothed x and z component data.

2. Page 15 - The equation used to calculate resultant displacement is changed to read:

$$RES(I) = \sqrt{XD(I)^2 + ZD(I)^2}$$

The second sentence following this equation,  
"Subroutine DERIV1 . . . in each case.", is changed to read,

Next subroutine DERIV1 is called to compute the X and Z components of velocity from the X and Z displacement data and then to compute the X and Z components of acceleration from the X and Z velocity data. In each case an eleven point quadratic smoothing

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function is applied to the input displacement or velocity data. The velocity components are stored in arrays VX(I) and VZ(I) and the acceleration components in arrays AX(I) and AZ(I). The resultant velocity and acceleration data are computed as follows:

$$VEL(I) = \sqrt{VX(I)^2 + VZ(I)^2}$$

$$ACC(I) = \sqrt{AX(I)^2 + AZ(I)^2}$$

3. Appendix C - as follows:

Page 130 ---

Insert line 125:

2, VX(302), VZ(302), AX(302), AZ(302)

Insert line 185:

2, (XX(1,1), VX(1)), (XX(1,2), AX(1)), (ZZ(1,1),  
VZ(1)), (ZZ(1,2), AZ(1))

Page 143 ---

Change Line 4480 to:

CALL DERIV1 (T, XD, VX, N, NP, 1)

Change Line 4500 to:

CALL DERIV1 (T, VX, AX, N, NP, 2)

Insert Line 4485:

CALL DERIV1 (T, ZD, VZ, N, NP, 1)

Insert Line 4505:

CALL DERIV1 (T, VZ, AZ, N, NP, 2)

Insert Line 4525:

VEL(I) = SQRT(VX(I) \* VX(I) + VZ(I) \* VZ(I))

Insert Line 4527:

ACC(I) = SQRT(AX(I) \* AX(I) + AZ(I) \* AZ(I))

4. Appendix D - Disregard tabular listings and plots of Resultant Velocity and Resultant Accelerations.

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